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# Check for updates **Discovery of Ternary Silicon Titanium Nitride with Spinel-Type Structure**

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**Here we report on the discovery of a ternary silicon titanium nitride with the general composition**   $(Si_{1-x}Ti_x)$ <sub>3</sub>N<sub>4</sub> with  $x = 0 < x < 1$  and spinel-type crystal structure. The novel nitride is formed from an **amorphous silicon titanium nitride (SiTiN) precursor under high-pressure/high-temperature conditions in a large volume high-pressure device. Underthe conditions of 15–20 GPa and 1800–2000 °C, spinel**type  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and rock salt-type c-TiN are formed. In addition, crystals of the discovered nano-sized ternary phase  $(Si_{1-x}Ti_x)$ <sub>3</sub>N<sub>4</sub> embedded in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> are identified. The ternary compound is formed due to **kinetically-controlled synthesis conditions and is analyzed to exhibitthe spinel-type structure with ca.** 8 atom% of Ti. The Ti atoms occur in both Ti<sup>3+</sup> and Ti<sup>4+</sup> oxidation states and are located on the Si sites. **The ternary nano-crystals have to be described as (Si,Ti)3N4 with N-vacancies resulting in the general**   ${\rm composition\,}({\sf Si}^{4+}_{1-x}{\sf Ti}^{4+}_{x-\delta}{\sf Ti}^{3+}_{\delta})_{3}{\sf N}_{4-\delta}.$ 

Spinel-type silicon nitride  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> is a high-pressure phase of silicon nitride and has been discovered in 1999<sup>1</sup>. In the same year, from the group 14 element, spinel type  $Ge_3N_4^2$  and  $Sn_3N_4^3$  have been found afterwards. Based on these experimental fndings, Ching *et al*. predicted a variety of binary and ternary nitrides including nitrides of transition metal elements<sup>4</sup>. In Fig. 1, an updated selection of prominent high-pressure nitrides experimentally accomplished (blues background) and those theoretically predicted (white background) but not achieved yet are listed.

According to their calculations, 39 spinel-type nitrides are characterized by interesting functional and structural features ranging from super-hardness via semiconducting to metallic properties<sup>5</sup>. Later on, it has been found experimentally, that the transition metal high-pressure nitrides of  $M=Ti$ , Zr and Hf with the stoichiometry  $M_3N_4$ do not show the spinel-type structure as forecasted, but appear in the cubic  $Th_3P_4$  structure-type<sup>6</sup>. Experimental studies verified that spinel nitride  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> in particular, but also the transition metal nitrides M<sub>3</sub>N<sub>4</sub> with M = Zr, Hf combine ultra-high hardness with high thermal stability against decomposition in diferent environments. This suggests their promising use in potential applications such as cutting tools<sup>7-9</sup>. Due to their predicted semiconducting behaviour, calculations showed that spinel-type nitrides exhibit interesting optoelectronic properties, which may lead to applications such as light-emitting diodes $4,10$ .

Figure 1 impressively reveals that the majority of the predicted ternary nitrides have not been synthesized yet. To the best of our knowledge, the spinel-type  $\text{GeSi}_2\text{N}_4$  is the solitary ternary nitride successfully synthesized<sup>11,12</sup>. Other ternary nitrides remained unknown yet though projected in various studies. There are even more theoretical studies predicting the existence of ternary nitrides e.g. with perovskite-type-based structures<sup>13</sup> and others<sup>14</sup> which could further immensely extend the field of unknown nitrides. Recently, a few new ternary nitrides with diferent structure types were synthesized by Sun *et al*. 15,16 based on a calculated large stability map of the inorganic ternary metal nitrides. They reported thin films of Zn-based and Mg-based ternary nitrides with wurtzite-type and rock salt-type structures, respectively<sup>16</sup>.

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Figure 1. Overview of some high-pressure nitrides experimentally synthesized and theoretically predicted, after W.-Y. Ching et al.<sup>4</sup>.

The forecasted ternary nitrides open up further numerous scientific questions related to synthesis, chemistry and properties of this interesting family of new materials. Novel synthesis approaches including high-pressure methods in combination with theoretical calculations ofer a chance to fnd correct pressure/temperature conditions to realize the synthesis of the exemplarily mentioned and calculated nitrides<sup>17</sup>.

In the present study, we report on a discovery of a ternary nitride formed between  $Si_3N_4$  and  $Ti_3N_4$  synthesized under high-pressure/temperature conditions, namely at pressures of 15–20GPa and temperatures of 1800– 2000 °C in a large volume press. While the binary nitrides crystallize in diferent structure types (spinel-type for  $Si_3N_4$ <sup>1</sup> and  $Th_3P_4$ -type for  $Ti_3N_4$ <sup>18</sup>), the formed ternary nitride reveals a spinel-type structure and it is, therefore, considered that Si in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> is substituted by Ti. In addition, the ternary (Si,Ti)<sub>3</sub>N<sub>4</sub> crystals are nano-sized and are embedded in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> single crystals.

#### **Results**

**Single-source-precursor synthesis.** High-pressure synthesis of inorganic metal nitrides requires appropriate precursor compounds, which contain all the elements of the targeted material. In our study we first synthesized a single-source precursor (SSP) by the reaction of perhydropolysilazane (PHPS) with tetrakis(dimethylamido)titanium (TDMAT) according to the scheme given in Fig. 2<sup>19,20</sup>. For this reaction, we choose a Si:Ti atomic ratio of 5.

The obtained SSP formed via the reaction of N-H- (dimethylamine release) and Si-H- (methane release) bonds from PHPS with the ligands of TDMAT is denoted as polytitanosilazane (PHPTiS5) and the following composition was obtained by chemical analysis: 38.4wt% Si, 17.2wt% Ti, 7.3wt% H, 16.0wt% N, 21.1wt% C and 0.9wt% O. By neglecting the oxygen contamination, a formal composition is derived from the analytical values:  $Si<sub>1.0</sub>Ti<sub>0.25</sub>C<sub>1.2</sub>N<sub>0.8</sub>H<sub>5.2</sub>$ 

The SSP is finally converted to an amorphous/nanocrystalline SiTiN ceramic (labelled as PHPTiS5\_1000) in ammonia atmosphere at 1000 °C with a ceramic yield of 73.25 wt%. Along with the amorphous background, the X-ray powder pattern of the synthesized SiTiN shows nanocrystalline features, which ft to the rock salt phase of TiN with a  $\sim$ 4.3 Å and a crystallite size of 2–3 nm. A quantitative elemental analysis of the SiTiN material revealed a composition of Si – 44.2 wt%; Ti – 18.9 wt%; N – 33.1 wt%; C – 0.02 wt%; O – 3.8 wt%. The values are used to calculate a formal composition of the synthesized powder by neglecting the carbon contamination:  $Si_{1,0}Ti_{0,2}N_{1,5}O_{0,15}$ that represents the presence of 0.3  $Si_3N_4 + 0.2$  TiN + 0.07  $SiO_2$  of the respective thermodynamically phase compositions. Tus, the Si:Ti ratio in the ammonolyzed and pyrolyzed material amounts ca. 5 and refects that of the molar ratio used for the synthesis of the SSP.

**High-pressure synthesis.** In the second step, the acquired SiTiN powder (PHPTiS5\_1000 sample) is subjected to a high-pressure/high-temperature treatment. The high-pressure experiments were performed in a large volume press under pressures between 16 and 20GPa and temperatures between 1800 and 2000 °C. Afer pressure release, a compact and sintered body is isolated from the reaction chamber. A SEM image of a fracture surface of the sample exhibits a composite microstructure with dark and bright contrasted nanocrystals (see Fig. 7). X-ray difraction analysis of the powdered sample revealed the presence of spinel-type γ-Si3N4 and rocksalt-type *c*-TiN as well as residual stishovite  $SiO<sub>2</sub>$  (Fig. 3).

The fraction of the crystalline phases was obtained by Rietveld refinement of the XRD data. The fractions were 72.6 wt%  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, 20.2 wt% of c-TiN and 7.1 wt% Stichovite (SiO<sub>2</sub>) together with <0.1 wt% Pt from the capsule material of the high-pressure experiment. The Si:Ti ratio thus remained ca. 5, and the bulk sample composition of



**Figure 2.** Synthesis procedure for the preparation of the SiTiN single-source precursor (SSP) according to reference<sup>19</sup>.



Figure 3. X-ray powder diffraction of SiTiN-run HH112 (λ = 0.207109 Å) and Rietveld refinement.

the SiTiN starting material therefore did not signifcantly change during experimental high-pressure/temperature treatment.

**Structural analysis via XRD and electron microscopy.** The average sizes of the synthesized  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and *c*-TiN were derived from the peak widths of the XRD pattern, and found both 260 ± 90 nm. Since these grain sizes are too small for chemical composition analysis by SEM-EDX, the samples were observed using ADF-STEM. As shown in Fig. 4(a), the sample consisted of two phases with diferent brightnesses. Since the brightness increases with increasing average atomic number, the brighter contrast grains should contain heavier elements, i.e. Ti. It is therefore concluded that the bright- and dark-contrast grains are c-TiN and  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, respectively. This evaluation was also confrmed by electron difraction and EDX mapping (Fig. 4c) of this region.

On the close inspection of the grains, we found a third type of nanocrystals inside of the  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> grains that can be seen as a brighter dot contrast in the ADF-STEM image of Fig. 4(b), suggesting that the nanocrystal should contain Ti atoms. The embedded nanocrystals are around 10-20 nm in size and occur in the majority of the silicon nitride host crystals. The distribution of nanoparticles in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> grain can be found in the low-magnification of annular bright-feld (ABF) STEM image (see Supplementary Note 1). To directly confrm the validity of Ti-concentration at the nano-particle, we performed STEM-EDX mapping and the map of Ti-K edge is shown in Fig.  $4(c)$ . On the basis of the STEM-EDX mapping, we elucidate that the nanocrystal contains Si, N and Ti atoms, and moreover the concentration of Si atoms is smaller than that in the vicinity of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>. Thus, Ti atoms are considered to be in the substitutional form at Si atomic sites. It is important to note that no significant oxygen is found in the nanocrystals. Figure  $4(d)$  shows an atomic-resolution ADF-STEM image viewed along the [110] orientation of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, including the interface between the nanocrystal and  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>. As indicated by the dotted line in Fig. 4(d), the nanocrystal (right-side) shows slightly brighter Z-contrast than that in the bulk of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, suggesting that the nanocrystal contains Ti atoms but the structure retains spinel-type with the coherent interface between the host  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and the nanocrystal: the discovery of the ternary (Si,Ti)<sub>3</sub>N<sub>4</sub>. We note that although the boundary between the nanoparticle and  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> may be difficult to realize from the weak Z-contrast difference,





it is most evident in the Z-contrast intensity profle across the grain boundary and the simultaneously recorded ABF-STEM image (see Supplementary Note 2). For further investigation, we performed EELS analysis across the nanocrystal as shown in Fig.  $4(e)$ , where the blue-, black- and red-colored profiles are related to the nanocrystal,  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, and c-TiN, respectively. The pink colored profiles are obtained from the bulk of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and the nanoparticle (average for Ti-*L*<sub>2,3</sub> edge). The Si-*L*, and N-*K* edges of the nanocrystal are basically similar to those in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, which is well compatible with the observed atomic structure. The Ti-*L*<sub>2,3</sub> edges are localized within the nanocrystal, and the peak positions of the Ti-*L*2,3 edge show slight upward shif compared with that in c-TiN, suggesting that Ti occurs in two oxidation states in the nanocrystal, namely  $Ti^{3+}$  and  $Ti^{4+}$ . In spinel-type structure, there are two atomic sites for cations, namely octahedral and tetrahedral coordination, and the Ti oxidation states for the sites have to be considered as  $Ti^{3+}$  and  $Ti^{4+}$ . For the compensation of the total charge, the nanocrystal requires N vacancies, and we conclude that the formed ternary spinel structure has to be described as  $(\rm{Si^{4+}}_{1-x})$  $Ti^{4+}$ <sub>x-δ</sub> $Ti^{3+}$ <sub>δ</sub>)<sub>3</sub>N<sub>4-δ</sub>, where we could not determine the Ti content (x) because the experimental spectroscopic information (EDX and EELS) is in 2D projection (the nanocrystal is embedded in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> grain). However, from EELS we can roughly estimate the following ratio  $Ti^{4+}: Ti^{3+} = (x - \delta): \delta \sim 0.7: 0.3$ , which leads to  $\delta \sim 0.3x$ .

**Thermodynamic considerations.** The composition of the synthesized ternary silicon titanium nitride solid solution is located on the tie line between the binary subsystems  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and Ti<sub>3</sub>N<sub>4</sub> as illustrated in the isothermal section of the phase diagram Fig. 5.

Accordingly, under the applied high-pressure/high-temperature conditions, amorphous SiTiN produced three phases, namely submicron-sized c-TiN with rocksalt-type structure and  $\gamma$ -Si<sub>3</sub>N<sub>4</sub><sup>1</sup> grains with nano-sized inclusions of a ternary  $\gamma$ -(Si,Ti)<sub>3</sub>N<sub>4</sub> phase, both with spinel-type structure. With respect to the phase diagram we may hypothesize that the ternary  $\gamma$ -(Si,Ti)<sub>3</sub>N<sub>4</sub> phase partitions first into  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and Ti<sub>3</sub>N<sub>4</sub> (along the yellow colored tie line in Fig. 5). However,  $Ti<sub>3</sub>N<sub>4</sub>$  is thermodynamically unstable under our experimental conditions of 15–20 GPa and 1800–2000 °C<sup>21</sup>. Thus, Ti<sub>3</sub>N<sub>4</sub> readily decomposes into the thermodynamically stable phases c-TiN



**Figure 5.** SiTiN ternary composition diagram with the known binary subsystems and the novel ternary SiTiN phase located on the tie line between  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and Ti<sub>3</sub>N<sub>4</sub>.

and gaseous  $N_2$  along the red colored tie line of the binary Ti-N subsystems presented in Fig. 5 and according to the following reaction equation:

$$
3\; Ti_3N_4 \rightarrow 9\; TiN\,+\,1.5\; N_2
$$

Moreover, crystalline Ti<sub>3</sub>N<sub>4</sub> cannot be recovered at ambient pressure<sup>18,21</sup>, while the high-pressure phase of silicon-nitride shows an enormous metastability even at ambient pressure and can be heated up to 1400 °C without any phase transformation<sup>22</sup>. Finally, once TiN is formed from the ternary  $\gamma$ -SiTiN phase, the resulting  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>/c-TiN composite is thermodynamically stable at P > 10 GPa and metastable under ambient pressure.

**Computation ofTi site preference and structure search.** Guided by the experimental data we started exploring spinel-type SiTiN. A first task was to evaluate site preference of Ti<sup>4+</sup> substituting for Si<sup>4+</sup> in  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>. We chose to work in the conventional unit cell of the spinel structure comprising 56 atoms. In a structure model of  $Si_{23}TiN_{32}$  at ambient pressure, Ti prefers substitution of the octahedral site over a tetrahedral site. The energy diference we compute, however, is very small – only 0.01 eV. Increasing pressure increases slightly the preference for Ti to occupy the octahedral site to 0.07 eV at 15GPa.

In a next step, we computed substitution of three Si by Ti simultaneously, still keeping  $Ti^{4+}$ . Thus, within the conventional unit cell we considered  $Si_{21}Ti_3N_{32}$  and performed a structure search over all possible combinations of three Ti on cation sites. The model with the lowest enthalpy that emerged displays three Ti in octahedral sites coordinating to the same N (see Fig. 6a,b). The small cluster formed by three fused  $TiN_6$ -octahedra resembles a fragment of the rock-salt TiN structure, albeit in this case with  $Ti^{4+}$  rather than  $Ti^{3+}$  as in TiN. The next lowest enthalpy model, still containing only Ti<sup>4+</sup> in octahedral sites, is already 0.19 eV higher in energy (for the full 56 atom unit cell). The first model comprising Ti in a tetrahedral site comes out 0.28 eV higher in enthalpy than the ground state model of  $Si_{21}Ti_{3}N_{32}$ . Interestingly, the model of  $Si_{21}Ti_{3}N_{32}$  with highest enthalpy (about 3 eV higher than the ground state model) also comprises all Ti in octahedral sites, but arranged with maximum distance from each other.

Introducing an anion vacancy does not change the picture of preferred cation arrangements in structures. Note that in models of  $Si_{21}Ti_{3}N_{31}$  all three Ti are (formally)  $Ti^{3+}$ . Again, we found that Ti prefers octahedral sites and tends to cluster. With the vacancy in the model, the lowest enthalpy structure displays all Ti adjacent to the defect as **Ti**N<sub>5</sub>V-octahedra (see Fig. 6c). Alternative arrangements are now a bit closer in energy, the second lowest-enthalpy structure is only 0.12 eV higher than the lowest-enthalpy model. Among all combinations, the highest enthalpy structure is still one in which all Ti are octahedral, but maximally dispersed in the structure.

We finally expanded our search to  $Si_{18}Ti_6N_{31}$ . This model displays half of Ti as Ti<sup>4+</sup> and the other half as Ti<sup>3+</sup>. We limited our combinatorial search on Ti in octahedral sites, and computed only a few models explicitly considering tetrahedral Ti as well. The lowest enthalpy configuration of  $Si_{18}Ti_6N_{31}$  then shows only octahedral Ti, with three Ti in octahedral sites adjacent to the vacancy and the other Ti in diferent octahedral sites. Within the unit cell we considered, there now appears a chain of connected  $TiN_6$ - $TiN_5V$ -octahedra sharing edges along the [110] direction. Alternatives with more dispersed arrangements are less favorable in energy. This indicates once again the preference of Ti to cluster (see Fig. 6d).

**Enthalpy of formation.** To compute enthalpies of formation,  $\Delta H_p$  of the ternary SiTiN compounds we use  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, TiN (for Ti<sup>3+</sup>), and spinel-type Ti<sub>3</sub>N<sub>4</sub> as reference models. Note that a spinel-type Ti<sub>3</sub>N<sub>4</sub> is not known, and only a Th<sub>3</sub>P<sub>4</sub>-type Ti<sub>3</sub>N<sub>4</sub> has been synthesized at 72 GPa <sup>18</sup>. The lowest energy structure of Ti<sub>3</sub>N<sub>4</sub> comprising  $\rm Ti^{4+}$  is predicted to adopt a monoclinic structure, as earlier studies have shown<sup>23,24</sup>.

Despite the fact that spinel-type  $Ti_3N_4$  is not the ground state of  $Ti_3N_4$ , we nevertheless find only positive values for Δ*H*<sup>f</sup> of spinel-type SiTiN. Tis implies that its decomposition into binary compounds is favored by enthalpy. An anion vacancy and presence of some  $Ti^{3+}$  only increases the trend and so does pressure. With the  $\Delta H_{\rm f}$  spinel-type SiTiN being positive, we turn to estimate the entropy of mixing,  $\Delta S_{\rm mix}$ , arising from distributing



**Figure 6.** (a) Lowest-enthalpy structure of  $Si_{21}Ti_{3}N_{32}$  and (**b**) its arrangement of fused TiN<sub>6</sub>-cluster. (**c**) Local environment of vacancy site in  $Si_{21}Ti_{3}N_{31}$  exhibiting TiN<sub>5</sub>V-octahedra (**d**) Lowest-enthalpy structure of  $Si_{18}Ti_{6}N_{31}$  highlighting the chain of edge-sharing TiN<sub>6</sub>-/TiN<sub>5</sub>V-octahedra. Green spheres represent N, red and dark blue spheres tetrahedral and octahedral Si, respectively, and light blue (cyan) spheres Ti.



Figure 7. SEM micrographs (run# HH112) showing (left) an overview of the sample pellet after HP-HT and (right) a fracture surface with spinel-type  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> and rock salt-type c-TiN crystals.

Ti among the cation sites and a vacancy among anion sites<sup>25,26</sup>. Neglecting site preferences, which will only reduce our estimate of Δ*S*<sub>mix</sub>, we estimate an upper bound of Δ*S*<sub>mix</sub> of 749, 1160, 1430 J/(K·mol), for Si<sub>21</sub>Ti<sub>3</sub>N<sub>32</sub>, Si<sub>21</sub>Ti<sub>3</sub>N<sub>31</sub>, and  $Si_{18}Ti_{6}N_{31}$ , respectively. Since less vacancies are present than Ti cations, the cation mixing contributes to the total entropy of mixing more than the anion mixing. With ∆*G*=∆*H*<sup>f</sup> − *T*∆*S*mix, we estimate that it would require temperatures greater than 5000 K to "stabilize"  $\rm Si_{21}Ti_{3}N_{31}$  and  $\rm Si_{18}Ti_{6}N_{31}$  against decomposition into the ternary



**Table 1.** Bulk modulus B, shear modulus G, and Vickers hardness  $H_V$  of  $Si_3N_4$  and SiTiN compounds with the spinel structure type at ambient pressure using SCAN functional.

system  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>, TiN, and spinel-type Ti<sub>3</sub>N<sub>4</sub>. We also considered a superstructure of *α*-Si<sub>3</sub>N<sub>4</sub> and substituted Si partially by Ti. This structure, thus, comprises tetrahedrally coordinated Ti<sup>4+</sup> and may serve as a model for the precursor used during synthesis of spinel-type SiTiN. Not surprisingly, the lowest enthalpy structure of such a  $\alpha$ -Si<sub>21</sub>Ti<sub>3</sub>N<sub>32</sub> displays all Ti clustered and bonding to the same N. Moreover, we find that incorporation of Ti slightly reduces the pressure of the  $\alpha-\gamma$  transition by 0.4 GPa, if we compare our models of  $\alpha$ -Si<sub>21</sub>Ti<sub>3</sub>N<sub>32</sub> and  $\gamma$ - $\overline{Si}_{21}Ti_3N_{32}$  discussed above relative to pure  $Si_3N_4$  structures.

In summary, the occurrence of spinel-type SiTiN cannot be attributed to thermodynamical stability. A spinel-type  $(Si, Ti)_{3}N_{4}$  solid solution is less favorable than assemblages of separated phases of  $Si_{3}N_{4}$ , TiN, and  $Ti_3N_4$ . However, the spinel-type  $(Si,Ti)_3N_4$  solid solution is more favorable than the precursor system with tetrahedral Ti<sup>4+</sup> mixed into a silicon nitride at 15 GPa. Therefore, formation of spinel-type  $(S_i, Ti)_3N_4$  should be due to the sluggish kinetics, because formation of separate phases from the uniform precursor is a slower process than formation of a single phase of the spinel-type  $(Si, Ti)_{3}N_{4}$  solid solution.

**Ti oxidation state.** An interesting question is related to the different charge states identified for Ti in spinel-type  $(Si,Ti)_{3}N_{4}$ . The compound comprises both  $Ti^{3+}$  and  $Ti^{4+}$ . For a characterization of charges, we computed the lowest energy configuration of  $Si_{21}Ti_{3}N_{32}$ ,  $Si_{21}Ti_{3}N_{31}$ , and  $Si_{18}Ti_{6}N_{31}$ , and used Bader charge analysis<sup>27,28</sup>. In  $Si_{21}Ti_{3}N_{32}$ , which displays Ti<sup>4+</sup>, we find 2.8 e<sup>-</sup> around the Ti according to the Bader charge analysis. On the other hand, Ti<sup>3+</sup> in Si<sub>21</sub>Ti<sub>3</sub>N<sub>31</sub> exhibits higher Bader charges of 3.2 e<sup>−</sup>. In Si<sub>18</sub>Ti<sub>6</sub>N<sub>31</sub>, which formally has equal proportions of Ti<sup>3+</sup> and Ti<sup>4+</sup>, we indeed find half of the Ti with Bader charges of 2.0 e<sup>-</sup>, while the other half displays Bader charges between 2.6 and 2.9 e<sup>-</sup>. This allows us to identify the two cohorts as Ti<sup>4+</sup> and Ti<sup>3+</sup>, respectively. Noteworthy is that  $Ti^{3+}$  appears adjacent to the vacancy as  $TiN<sub>5</sub>V$ -octahedra, while  $Ti^{4+}$  appears within TiN<sub>6</sub>-octahedra.

**Elastic properties.** We also computed elastic constants for all compounds and estimate elastic moduli (B, G) as well as Vickers hardness H<sub>V</sub>, see Table 1. The  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> is a notably hard material<sup>29</sup>, but adding Ti reduces elastic properties and decrease hardness. The estimated hardness of  $Si_{18}Ti_{6}N_{31}$  comes out to be close of half of that of  $\gamma$ - $Si_{3}N_{4}$ .

**Electronic properties.** We computed the band gap of  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> to 4.95 eV using the screened hybrid HSE-functional<sup>30</sup>. This aligns with previous calculations and available experimental data<sup>31</sup>. Replacing Si<sup>4+</sup> by Ti<sup>4+</sup> introduces localized unflled d-states below the conduction band, ultimately decreasing the width of the band gap. Introducing a single nitrogen vacancy creates an odd number of  $Ti<sup>3+</sup>$  and results in a partially filled band in the middle of the gap.

#### **Discussion**

In summary, an amorphous SiTiN labelled PHPTiS5\_1000 compound was synthesized by the reaction of perhydropolysilazane with tetrakis(dimethylamido)titanium and subsequent heat-treatment in ammonia at 1000 °C. The SiTiN PHPTiS5\_1000 was exposed to 15-20 GPa pressure and 1800-2000 °C in a large volume press to form a high-pressure  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>/c-TiN composite material for the first time. The special feature of the obtained composite is due to the discovery of an additional nanocrystalline ternary  $\gamma$ -(Si,Ti)<sub>3</sub>N<sub>4</sub> phase with spinel-type structure embedded within the majority of the submicron  $\gamma$ -Si<sub>3</sub>N<sub>4</sub> crystals. The  $\gamma$ -(Si,Ti)<sub>3</sub>N<sub>4</sub> phase was analyzed in detail by TEM and EELS and the results clearly showed the presence of two types of Ti atoms, namely  $Ti^{3+}$  and  $Ti^{4+}$ , which in turn requires the formation of vacancies in the anion lattice. Therefore, the general formula of the discovered ternary spinel-type SiTiN has to be described as  $(Si^{4+}_{1-x}Ti^{4+}_{x\cdot\delta}Ti^{3+}_{\delta})_3N_{4-\delta}$ . According to theoretical calculations, Ti3<sup>+</sup> appears adjacent to the vacancy as **Ti**N5V-octahedra, while Ti4<sup>+</sup> appears within **Ti**N6-octahedra. Moreover, all of the ternary SiTiN compounds have been calculated to be thermodynamically unstable with respect to the binary phases, which is in accordance with the experimental result, that finally a binary  $\gamma$ -Si<sub>3</sub>N<sub>4</sub>/c-TiN high-pressure composite is formed.

In consequence, it has to be noted that the synthesis of the ternary spinel-type SiTiN phase is kinetically controlled and requires an appropriate precursor material (SSP) with Ti<sup>4+</sup> atoms in tetrahedral coordination together with tetrahedrally coordinated Si in amorphous silicon nitride. A direct reaction of  $Si<sub>3</sub>N<sub>4</sub>$  with TiN to form a ternary high-pressure SiTiN phase is thermodynamically impossible and has not been observed yet experimentally. The present work encourages to study other SSP-derived Si-based systems containing transition metal atoms other than Ti to form innovative high-pressure composite materials and novel inorganic ternary metal nitrides.

#### **Methods**

**Single-source-precursor synthesis.** A titanium-modifed perhydropolysilazane (PHPS) as single source precursor (SSP) was synthesized by a reaction between PHPS and tetrakis(dimethylamido)titanium (TDMAT) with a molar Si:Ti ratio 5:1 (labelled as PHPTiS5) according to our previous reports<sup>19,20</sup>.

Run No	<b>Sample</b>	Assembly	Pressure (GPa)	Temperature $(^{\circ}C)$	Heating duration (min)	Capsule material
HH113	SiTiN-PHPTiS5 1000	14/7	16	1800	30	Pt
HH109	SiTiN-PHPTiS5 1000	10/4	20	1800	30	Pt
HH112	SiTiN-PHPTiS5 1000	10/4	20	2000	20	Pt

**Table 2.** Overview of HP-HT experiments with run number, assembly, pressure, temperature, heating duration and capsule materials.

The manipulation of the PHPTiS5 sample was made in an argon-filled glove box (Jacomex, Campus-type;  $O_2$ ) and H2O concentrations kept at 0.1 ppm and 0.8 ppm, respectively) to be ground in an agate mortar and then placed in alumina boats. Alumina boats containing the polymers were introduced in tubes under protective atmospheres (argon) to be transferred under argon fow into a silica tube inserted in a horizontal furnace [THERMOCONCEPT OS50/450/12]. Afer evacuation of the furnace under dynamic vacuum (0.1 mbar), the tube was reflled with ammonia up to atmospheric pressure and a continuous fow of ammonia was maintained through the tube. Subsequently, the samples were pyrolyzed at a heating rate of 5 °C min<sup>-1</sup> to 1000 °C (dwell time for 2h) in order to produce the SiTiN precursor (labelled as PHPTiS5\_1000). After cooling at a rate of 2°C min<sup>−1</sup> under nitrogen flow, the PHPTiS5\_1000 was used as a starting material for the subsequent high pressure synthesis.

The silicon and titanium contents of the synthesized PHPTiS5\_1000 sample powders were measured by inductively coupled plasma/optical emission spectroscopy (ICP/OES) [Optima 8300 optical emission spectrometer Perkin Elmer, USA]. The carbon and the oxygen, nitrogen and hydrogen contents of the powders were determined by combustion elemental analysis [Carbon (EMIA-321V), O/N/H analyzer (EMGA-830) Horiba, Japan].

The phase composition of PHPTiS5\_1000 sample was determined by powder X-ray diffraction (XRD) with a Bruker AXS D8 Discover and Cu*K*<sub>α</sub> radiation. The scans were performed in the range of  $2\theta \in (15^{\circ}, 90^{\circ})$  with a step of  $0.015^{\circ}$  and an exposure time of 0.7 s. The diffraction patterns were analyzed using the Diffrac + EVA sofware with the JCPDS-ICDD database.

**High-pressure synthesis.** High-pressure high-temperature experiments were performed in a Hall-type six-ram LVP (mavo press LPQ6 1500–100; Max Voggenreiter GmbH, Germany) installed at the P61B beamline at DESY, Hamburg<sup>32</sup>. The samples were synthesized in a 14/7 or 10/4 assembly of eight tungsten carbide cubes (32 mm Fujilloy TF08) at the target pressures. A  $Cr_2O_3$ -doped MgO octahedron was used as the pressure-transmitting medium. The starting material was cold pressed into pellet form  $(h=1.6\,\text{mm}, \varphi=1.9\,\text{mm})$ using a platinum foil before placing in the MgO tube. The octahedral assembly was compressed to a pressure of 16 and 20 GPa and, at pressure, heated to a chosen temperature in the range of 1800–2000 °C and held for 30 min. Pressure was calibrated at room temperature using the semiconductor to metal transition of GaP at 22 GPa33. Sample temperatures were estimated using power-temperature relations calibrated in a separate run using a W5%Re/W26%Re thermocouple (C-type). Overview of experimental conditions with the corresponding run numbers are given in Table 2.

Afer recovery, each sample was found dense and fne-grained in appearance (see Fig. 7).

XRD of crushed samples was obtained using synchrotron radiation at the high-resolution powder difraction beamline P02.1 of PETRA-III, DESY, Hamburg. The XRD pattern was quantitatively analyzed by Rietveld refinement with the program GSAS-II<sup>34</sup>.

**Electron microscopy.** For the preparation of electron transparent thin specimen, the synthesized bulk sample was processed by focused ion beam (Helios G4, Termo Fisher Scientifc) and subsequently, to clean the specimen, Ar ion beam milling was performed at 0.5 kV in the fnal step. For the atomic and electronic structure analysis, we used an aberration-corrected STEM (JEM ARM-200CF, JEOL Ltd.), equipped with an annular dark-feld (ADF) and annular bright-feld (ABF) detectors, EEL spectrometer (Enfnium, Gatan Inc.) and dual electron dispersive X-ray (EDX) spectrometers. The electron microscope was operated at 200 kV. For atomic-scale imaging and spectroscopy, the illumination semi-angle was 24 mrad, and the ABF and ADF detectors span from 12 to 24 and 64 to 200 mrad, respectively, where a typical beam current was 20 pA.

**Computational method.** All calculations were performed using density functional theory (DFT) as implemented in the Vienna *ab initio* simulation package (VASP)<sup>35–38</sup>. For correlation and exchange we use the Strongly Conserved and Appropriately Normed (SCAN) functional together with the projector-augmented-wave (PAW) method<sup>39–41</sup>. Reported results were obtained using a plane wave cut-off energy of 500 eV. We sample the Brillouin zone of the conventional unit cell and all derived structures using a  $2 \times 2 \times 2$  k-point mesh. With parameters reported above, enthalpy diferences between structures are converged to better than 0.005 eV per conventional unit cell.

Different models of spinel-type  $Si_{21}Ti_{3}N_{32}$  and  $Si_{21}Ti_{3}N_{31}$  were investigated by testing all the possible combinations of Ti at Si octahedral and tetrahedral sites. We frst identifed lowest enthalpy structures by static calculations without further relaxation. Structures with low enthalpies were further optimized until forces converged to 0.01 eV/Å and residual stresses are below 0.01GPa. It turned out that this optimization does not change the ranking of the models to a signifcant extent. Lowest enthalpy models of each composition were further optimized (forces converged to 5 meV/Å) and used for subsequent calculations. The lowest enthalpy model of  $Si_{18}Ti_{6}N_{31}$ attained monoclinic structure (SpGr. *C*1*m*1 (8); a=7.905Å, b=7.905Å, c=7.923Å, α=89.94°, β=89.94°,  $\gamma$  = 89.68°), but displayed only small distortion away from a pseudo-cubic cell. Substituting Ti for Si increases the cell volume relative to spinel- $Si_3N_4$  even in models with a vacancy.

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#### **Author contributions**

Abhijeet Lale and Samuel Bernard synthesized the single-source precursor and characterized the composition and molecular structure. Shrikant Bhat designed and performed the high-pressure experiments. Robert Farla supported and helped the high-pressure study. Ryo Ishikawa and Wei Zhang investigated the high-pressure samples by electron microscopic methods. Shariq Haseen and Peter Kroll worked on the computational part and Leonore Wiehl on the crystal structure analysis via Rietveld refnement. Ralf Riedel, Yuichi Ikuhara and Tomoo Katsura conceived the project and wrote the paper with input from the other authors.

#### **Competing interests**

The authors declare no competing interests.

#### **Additional information**

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