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Ab initio diabatic and adiabatic calculation for the francium hydride FrH

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Abstract

Explicitly ab-initio diabatic and adiabatic calculations of potential energy curves (PECs) of the states ${}^{1,3}\Sigma^+$, ${}^{1,3}\Pi$, and ${}^{1,3}\Delta$ of francium hydride FrH have been carried out with several approaches. We determined for both representations, the Permanent and Transition Dipole Moment (PDM and TDM) and the vibrational levels. The calculation was based on the Configuration Interaction (CI) method, which includes the Effective Core Potentials (ECP) and Core Polarization Potentials (CPP). The FrH system is considered as an effective two-electron system, permitting calculation of structural and electronic properties with Full Configuration Interaction (FCI). For the diabatisation method, we perform an efficient diabatization approach, which depends on the variational effective Hamiltonian theory (VEH) and a dynamic overlap matrix. This work finishes the diabatic and adiabatic ab-initio spectroscopic investigations of all the alkali hydrides series. In addition, we present our adiabatic results of FrH by comparing it with the other alkali hydrides systems (Li-Cs)H. This study is essential for a wide range of theoretical and experimental work.

I-Introduction

Many theoretical¹⁻²⁴ and experimental²⁵⁻³¹ researchers have studied the alkali-metal hydrides for many years. The investigation of the chemistry compounds in the early universe and the resolution of the abundances of these compounds in stellar atmospheres needed a thorough understanding of the cross sections for many collisional processes¹⁷. For example, inelastic collisions between alkali-metal atoms (Li and Na) and hydrogen^{32,33}, radiative charge transfer

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between alkali-metal atoms and H⁺³⁴, neutralization collisions between H⁻ and alkali iont^{35,36}cte Online or dissociative recombination³⁷. Adopting the ideas of ref.³⁸ concerning the manipulating molecules via combined laser and static fields, alkali-metal hydrides could be a beneficial for such experiments.

Interestingly, the francium

is the heaviest alkali-metal atom. Further, the francium exists only thirty grams in the earth crust. It is the longest-lived isotope lasts only 20 minutes and it is the most unstable element of the first 103 in the periodic table. The francium gives a sensible test of the influence of Quantum and relativistic Electro-dynamic effects on the atomic composition³⁹. In addition, the francium is also a very good compound for examining feeble interactions in atoms, for example atomic Parity Non-Conservation (PNC)⁴⁰⁻⁴². One of the most important discoveries of the 1939s was the francium by Perey of the curie institute located in Paris by observing the β decay of ²²³Fr in the natural actinium radioactive decay chain⁴³. All its isotopes have short half-lives (maximum 21.8 min, for ²²³Fr), that is why this element was the second-most rare natural compound on earth after astate 'At'44-45. It was not until 1978 that the group guided by Sylvan Liberman at ISOLDE in CERN manage to find the D2 resonant line of the spectrum of Fr, leading the way for many spectroscopic investigations. Meanwhile, the evolution of tunable lasers had allowed the trapping and cooling of alkali atoms involving resonance light in combination with magnetic fields, indeed all the parts obligatory for cooling and trapping francium were there at Stony Brook in the early 1990s⁴⁴. Indeed, this rarity is due to its transient existence, as a decay product of actinium⁴⁶. The main cause of the order of the francium of the least studied element is the experimental difficulties^{40, 47}. The francium is never found outside nuclear facilities or research laboratories, being potentially dangerous because of its intense radioactivity and its natural occurrence in uranium mineral but at any one time, there is one francium atom per one billion atoms of uranium⁴⁸. When the rats were injected with francium, it concentrated in the bladder, gut, kidneys, saliva and liver. In those rats with cancer, it also concentrated in the tumor, raising hopes that francium might have medical uses in treating this disease. For reasons given below, this was a forlorn hope⁴⁹.

The topic of this work is to investigate the electronic, vibrational and dipolar electric properties for the francium hydride system including: (i) the PECS of several symmetries ${}^{1,3}\Sigma^+$, ${}^{1,3}\Pi$, and ${}^{1,3}\Delta$ and their spectroscopic constants (R_e : Equilibrium distance, D_e : Well depth, T_e : Transition energies, $\omega_e \chi_e$: Anharmonic constant, ω_e : vibrational constant and B_e : rotational constant). (ii) The vibrational properties. (iii) The PDM and TDM functions.

As we know that there are no previous experimental studies have yet been published for the decommendation of the studies of th

This work is outlined as follows: Section II introduces our methodology based on ab-initio diabatic and adiabatic calculation. In Section III, we present the molecular diabatic and adiabatic PECs, their spectroscopic constants together and the vibrational level properties. In section IV, we give our numerical data of the permanent and transition dipole moments (PDM and TDM) for both representation. Section V contains the conclusions.

II-Ab inito calculations

1. Calculation Details

Many studies have focused on the electronic structure by using ab initio method of alkali-metal hydrides^{3,7,13,14}. In this calculation, the polarizable core of Fr^+ is substituted by a semi-empirical pseudo-potential put forward by Barthelat and Durand^{58, 59}, completed by both approach Core Polarization Potentials and Effective Core Potentials. The semi-local form of the Fr core is taken from the paper studied by M. Aymar et al.⁴⁹. In this framework, the electronic properties were investigated first at the Self-Consistent Field (SCF) based on Full Configuration Interaction (FCI) applicated the Toulouse package code^{3-7, 13, 14, 60-79}. Moreover, the interaction between the polarizable core Fr⁺ with the hydrogen nucleus and the valence electrons is treated using the core polarization potential V_{CPP} given by Müller et al.⁸⁰ which is written as:

$$V_{CPP} = -\frac{1}{2} \sum_{\gamma} \alpha_{\gamma} \vec{f_{\gamma}} \vec{f_{\gamma}}$$
(1)

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Where α_{γ} is the γ core's dipole polarizability and $\overrightarrow{f_{\gamma}}$ represents the electrostatic field proposed by the other cores on the γ and the valence electron:

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$$\vec{f}_{\gamma} = \sum_{i} \frac{\vec{R}_{\gamma i}}{R_{\gamma i}^{3}} F_{l}(R_{\gamma i}, \rho_{\gamma}^{l}) - \sum_{\gamma \neq \gamma} Z_{c} \frac{\vec{R}_{\gamma'\gamma}}{R_{\gamma'\gamma}^{3}}$$
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DOI: 10.1039/C9NJ06391A
(2)

 $\vec{R}_{\gamma i}$ is the core-electron vector, the $\vec{R}_{\gamma'\gamma}$ vector is the core-core and $F_1(R_{\gamma i}, \rho_{\gamma})$ is the cut-off operator corresponding to the operator expression of Foucault et al.⁸¹, which is written as follows:

$$F(R_{\gamma i}, \rho_{\gamma}) = \begin{cases} 0; & R_{\gamma i} < \rho_{\gamma} \\ 1; & R_{\gamma i} > \rho_{\gamma} \end{cases}$$
(3)

Furthermore, the cut-off radius is given by a function of (l) according to:

$$F(R_{\gamma i}, \rho_{\gamma}) = \sum_{l=0}^{\infty} \sum_{m=-l}^{+1} F_l(R_{\gamma i}, \rho_{\gamma}) |lm\gamma\rangle \langle lm\gamma|$$
(4)

 $|lm\gamma\rangle\langle lm\gamma|$ is a spherical harmonic in the center of the γ core.

In this framework, the core polarizability of the francium is taken from Ref.⁸² where $\alpha_{Fr}=20.38$ a_0^3 . The optimized cut-off parameters are $\rho_s = 3.1629$, $\rho_p = 3.027$ and $\rho_d = 3.1068$ Bohr.

To have a best representation of the atomic levels (7s, 7p, 6d, 8s, 8p, 7d, 9s and 9p) of the Fr atom, we optimized a large Gaussian-Type Orbital (GTO) basis set 8s/6p/5d (see **Table S1 in the supporting information**). While for the hydrogen atom, we have re-optimized the basis set studied by Zrafi et al.⁷ to be (7s/3p/2d). Therefore, we have improved the variation between our result and the experimental one, which is less than 47 cm⁻¹ for 1s level (see **Table S2 in the supporting information**).

Our selection of the basis set globally ameliorates the investigated francium atomic level energies compared with preceding works like the work of Aymar et al.⁴⁹ on the francium atom. In **Table S3**, we display the atomic spectrum of Fr of our work and those of Aymar et al.⁴⁹ which are compared with the experimental ones⁸³. The analysis of the experimental and our theoretical energies shows a good concordance between them⁸³ where the largest difference is 88 cm⁻¹. We display in **Table S4**, our energies of the asymptotic limits with the experimental ones, which dissociate bellow the ionic limit (Fr⁺ + H⁻). This limit is described as IP_{Fr}–EA_H where IP_{Fr} (=32848 cm⁻¹) is the ionization potential of the francium and EA_H (=6083 cm⁻¹) is

the electronic affinity of hydrogen. Our values are in very good accord with the experimental tele Online DOI: 10.1039/C9NJ06391A data. In addition, we can see in **Table S4** that the relative errors between the experimental and theoretical energies do not exceed 0.094 %.

2. Diabatic Calculation Details

We used here the same method used for full alkali hydride series (LiH³, NaH⁴, KH⁵, RbH⁶, CsH⁷), the alkaline earth hydride (CaH⁺⁶⁵) and mixed alkali (KLi⁷⁰ and RbLi⁷²). The strategy of the diabatisation method is to determine theoretical approximation of the non-adiabatic coupling between the pertinent adiabatic states and to make it disappear by a suitable unitary transformation relative to Variational Effective Hamiltonian theory (VEH)⁸⁴. In the actual performance of the VEH at each distance the target space (adiabatic states, Ψ_i) and the model space (reference states, Φ_i) need to be exactly defined now.

The model space noted S₀ is crossed by n orthogonal vectors{ $|R_i\rangle$, i = 1,...n}. The associated projector is P₀:

$$P_{S_0} = P_0 = \sum_{i=1}^n |R_i\rangle \langle R_i| \tag{5}$$

In this work we choose the large inter-atomic distance interval used in the adiabatic work where all inter-atomic interaction disappears.

The target space S is clearly formed by the "n" adiabatic functions " Ψ_i " at inter-atomic distance "R" and the projector "P":

$$P = \sum_{i=1}^{n} |\Psi_i\rangle\langle\Psi_i| \tag{6}$$

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Moreover, the projection matrix of the model space vectors on the target space is made unitary by symmetrical orthogonalization^{13, 84-87} as in the des cloiseaux formulation of VEH approach. First, we used an effective overlap matrix A that defined as following:

$$A_{ij} = \langle R_i \mid P_0 \Psi_j \rangle = \langle \Psi_i \mid \rangle \tag{7}$$

Then, the n diabatic states (D_i) are orthonormal linear combinations of the "n" adiabatic states, which the matrix formulation is written as:

$$U^{ij} = \langle \Psi_i \mid D_j \rangle, \qquad U'U = \mathbb{1}$$
(8)

Since the matrix diagonal of the electronic Hamiltonian (H) in the adiabatic representation be noted as:

$$\mathbf{E} = \langle \Psi_i \mid \mathbf{H} \mid \Psi_j \rangle = \mathbf{E}_i \delta_{ij} \tag{9}$$

It is "de-diagonalised" in the diabatic representation where H is now written U E $U_{DOI: 10.1039/C9NJ06391A}^{View Article Online}$

As mentioned in the paper of Romero et al.⁸⁶, in all dibatisation procedures, the interference between a molecular orbital at a specified point (named R) and another specified point (named R_0) plays a key role. Moreover, the overlap matrix A depends on the movement of the atoms when passing from R to R_0 . The choice of the lower half diagonal section from one distance and the superior section from the another distance for a diatomic molecule, related to fix the common origin of coordinates in one of the atoms precisely at the heavier and assuming a diagonal 1 matrix in each of the diagonal blocks. In a way to reduce the remaining coupling between the quasi-diabatic states, from A the unitary adiabatic-diabatic transformation matrix U is making as:

$$U = A (A'A)^{-\frac{1}{2}}$$

The Hamiltonian "H" in the diabatic basis is obtained as:

$$\langle D | H | D \rangle = U'EU = (A'A)^{-\frac{1}{2}} A'E A (A'A)^{-\frac{1}{2}}$$
 (11)

III- Results and interpretation

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1. Adiabatic and diabatic PECs and their Spectroscopic constants

In our study, we realize an adiabatic and diabatic calculation of the francium hydride by employing the pseudo-potential for the Fr core supplemented by CPP, ECP, FCI and the method of diabatisation. We investigated the PECs for various states of ${}^{1,3}\Sigma^+$, ${}^{1,3}\Pi$, and ${}^{1,3}\Delta$ symmetries beneath the ionic limit (Fr⁺+ H⁻) for both representations. These curves are shown in **Figures 1-7** for a large number of grid points with R varying from 2.5 to 200 a.u. The PECS are investigated by FCI, which have been used to derive the spectroscopic constants of whole the states via Nvib program (The program is restricted to the harmonic expression of the vibrational problem (i.e. just the quadratic force field)). The obtained spectroscopic parameters are reported in **Table 1**.

Table 1. Spectroscopic constants	for ^{1,3} Σ^+ , ^{1,3} Π and ^{1,3} Δ states of FrH.
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States	$R_{e}(a.u.)$	D_e (cm ⁻¹)	T_e (cm ⁻¹)	ω_{e} (cm ⁻¹)	$\omega_e \chi_e(cm^{-1})$	B_e (cm ⁻¹)				
	(a) ${}^{1}\Sigma^{+}$ States									
$X^1\Sigma^+$	4.43	14041	0	802	1.34	0.31				
$A^1\Sigma^+$	7.31	9842	19572	211	4.04	0.07				
$C^{1}\Sigma^{+}$	5.65	2566	28433	47	1.34	0.01				
2 nd min	14.14	2278								
${ m D}^1\Sigma^+$	6.06	588	34197	94	0.74	0.03				
2 nd min	18.07	3214	_	_	_	_				
$E^{1}\Sigma^{+}$	5.76	1302	37156	$\overline{22}$	0.80	0.01				
2 nd min	14.32	3383	_			_				

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$F^1\Sigma^+$	5.79	886	38445	20	0.41	0.01 View Article C DOI: 10.1039/C9NJ06
2 nd min	9.69	1372				
$G^1\Sigma^+$	6.20	596	40289	$\overline{2}$	0.14	0.001
2 nd min	8.65	1408	_	_	_	
3 th min	38.65	1271				
$\mathrm{I}^{1}\Sigma^{+}$	7.72	374	44289	149	5.95	5.75
		(b)	${}^{3}\Sigma^{+}$ States			
$a^{3}\Sigma^{+}$	10.63	110	16601	54	6.90	0.13
$c^{3}\Sigma^{+}$	5.43	52	27890	175	37.5	2.61
2 nd min	16.75	31				
$d^3\Sigma^+$	5.98	2472	33949	266	40.5	3.16
2 nd min	14.48	17				
$e^{3}\Sigma^{+}$	5.30	1442	36108	168	49.4	3.98
2 nd min	8.87	123				
$\mathrm{f}^{3}\Sigma^{+}$	5.74	125	38182	277	47.7	3.49
2 nd min	8.24	606				
$\mathrm{g}^{3}\Sigma^{+}$	5.00	939	40217	607	169.9	21.23
2 nd min	7.26	789				
3 th min	25.0	49	_	_	_	_
$h^3\Sigma^+$	6.43	580	41256	292	55.97	3.87
$i^3\Sigma^+$	6.55	714	43199	261	31.31	1.28
		(c)	^{1,3} ∏ States			
B ¹ Π	6.15	546	27974	184	20.61	0.77
b³П	5.71	787	27723	236	22.96	0.72
$1^{1}\Pi$	6.56	330	31389	145	21.13	1.03
$1^{3}\Pi$	5.15	1620	29156	308	11.97	0.24
$2^{1}\Pi$	6.16	574	38072	194	20.82	0.68
2 ³ П	6.04	624	37997	214	24.62	0.96
3 ¹ П	6.23	571	39142	190	19.29	0.51
3 ³П	5.84	682	38724	229	27.99	1.24
		(d)	$^{1,3}\Delta$ States			
$1^{1}\Delta$	6.26	460	31102	181	23.47	1.01
$1^{3}\Delta$	6.22	471	31069	185	23.77	1.02
$2^{1}\Delta$	6.17	559	39082	197	22.21	0.79
$2^{3}\Delta$	6.16	561	39075	198	22.47	0.81

1.1. $^{1}\Sigma^{+}$ Symmetry

The adiabatic PECS for the ${}^{1}\Sigma^{+}$ molecular states of FrH are graphically depicted in Figure 1.

These curves have the same shape like those of LiH³, NaH⁴, KH⁵, RbH⁶ and CsH⁷. Therefore, the potential well of the ground state was practically profound at a short inter-nuclear distance R_e =4.43a.u, which has a depth D_e =14041 cm⁻¹. The first excited state $A^1\Sigma^+$ presents a flat potential well explained by the largeness of the avoided crossing between the repulsive section of the $X^1\Sigma^+$ curve at the short distance and the attractive part of $A^1\Sigma^+$ about R= 17 a.u. In addition, the next excited state ($C^1\Sigma^+$), shows two minimum; the first is at about R= 5.65 a.u., and the second is at about R= 14.14 a.u., following the neutral-ionic avoided crossing with $A^1\Sigma^+$.

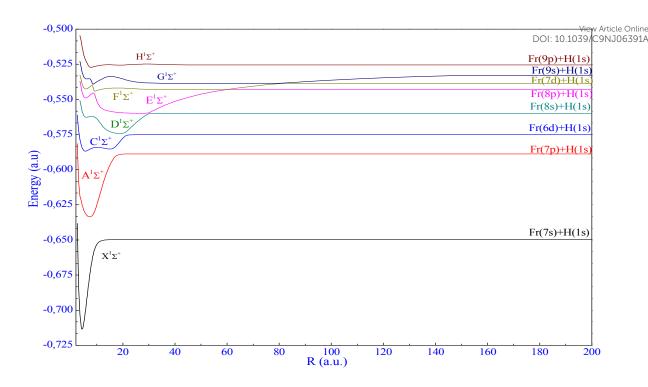


Figure 1. Adiabatic PECs ${}^{1}\Sigma^{+}$ dissociating below the ionic limit Fr⁺ + H⁻.

For the most excited states, we can note that the appearance of double and triple wells. We can see that the D, E and F states shows double minima: The first one at a short distance that could be corresponding to an avoided crossing between neutral-neutral states, and the second at large distance corresponding to the ionic–neutral states and only the $G^{1}\Sigma^{+}$ have a triple minima.

As far as we know, the theoretical values are obtainable only for the ground state studied by Hill and al.¹ and Noro et al.². The MOLPRO procedure of *ab initio* programs was used for all computation in their works. As seen in **Table 2**, we have listed the two available theoretical spectroscopic constants, which are studied with a different basis. Notably, our results correlate with Hill et al.¹ data for the basis of cc-pV5Z-PP for D_e , where the difference less than 75cm⁻¹. Moreover, we can see that the equilibrium distances R_e got by Noro et al.² for the basis of wCVQZ-DK3 is larger than our results around 0.4 a.u.

		-	
Basis sets	R _e (a.u.)	D _e (cm ⁻¹)	ω _e (cm ⁻¹)
This work	4.43	14041	802
Dzp ¹	4.943	-	833
Tzp1	4.858	-	902
Qzp1	4.849	-	901
cc-pVDZ-PP1	5.157	11171	811
cc-pVTZ-PP1	5.119	13378	836
cc-pVQZ-PP1	5.128	13955	833
cc-pV5Z-PP1	5.134	14116	828
CBS1	5.142	14228	823
wCVDZ-DK3 ²	4.941	10710	846
wCVTZ-DK3 ²	4.854	12892	885
wCVQZ-DK3 ²	4.840	13455	893

Table 2. Main spectroscopic constant for the ground state of the molecules FrH.

We list in **Table 3** the positions of some avoided crossings, which were located in the PECS with the corresponding main energy difference for the FrH. Similarly to the alkali hydrides series³⁻⁷, these crossings corresponding to the excitation or charge transfer efficiency between the Fr and H atoms and the presence of numerous avoided crossings at a short and a long distance come from the unusual undulating behavior of (-1/R). In this framework, these crossings are accountable for the particular behaviors of PECs such as the presence of multiple wells as for $G^1\Sigma^+$ and the appearance of a wave feature in PECs.

Table 3. Avoided crossing positions and energy difference between two states.

States	Positions (a.u.)	$\Delta E (cm^{-1})$
$X^1\Sigma^+/A^1\Sigma^+$	10.5	6575.5
$A^{1}\Sigma^{+}/C^{1}\Sigma^{+}$	17	1512.18
$C^1\Sigma^+/D^1\Sigma^+$	21	531.57
$D^{1}\Sigma^{+}/E^{1}\Sigma^{+}$	10.5/29.5	2558.20/219.40
$E^{1}\Sigma^{+}/F^{1}\Sigma^{+}$	9/60	425.78/12.07
$F^1\Sigma^+/G^1\Sigma^+$	8.3/81.5	302.22/63.36
$G^{1}\Sigma^{+}/H^{1}\Sigma^{+}$	15.5	1799.033
$d^3\Sigma^+/e^3\Sigma^+$	7.5	1437.12
$e^{3\Sigma^{+}}/f^{3\Sigma^{+}}$	8.3	2958.29

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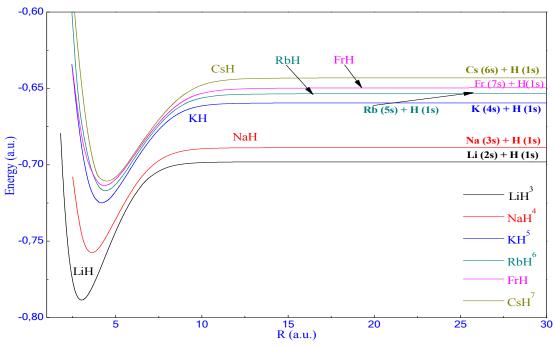
$f^{3}\Sigma^{+}\!/\ g^{3}\Sigma^{+}$	6.9	277.85	View Article Online DOI: 10.1039/C9NJ06391A
$g^3\Sigma^+\!/\;h^3\Sigma^+$	5.9	426.66	

We plotted the PECS for the ground state $X^{1}\Sigma^{+}$ for all the alkali-metal hydrides XH systems (where X=Li, Na, Cs, Rb, and Fr) that are given in **Figure 2**, which are similar to the origin of energies attached to the limit X+H(1s). In addition, their spectroscopic constants are presented in **Table 4** with the accessible work found in the litterature^{16, 88, 89}.

		,	
Molecules	References	$R_e(u.a.)$	$D_e(cm^{-1})$
T :TT	Ref ³	3.003	20350
LiH	Ref 17	3.002	20167
	Ref ⁴	3.507	15489
NaH	Ref 88	3.572	15970±403
	Ref 17	3.54	15671
	Ref ⁵	4.19	14365
КН	Ref 88	4.265	14776
	Ref 17	4.168	14500
	Ref ⁶	4.40	13940
RbH	Ref 88	4.53	14599±565
	Ref 17	4.395	14099
	Ref ⁷	4.47	14 879
	Ref 88	4.78	14809
CsH	Ref ¹⁶	4.7	15083
	Ref ⁹⁰	4.71	14791
	Ref 17	4.464	15019
FrH	This work	4.43	14041

Table 4. Main spectroscopic constant for the ground state of the XH molecules (X= Li, Na, K, Rb, Cs
and Fr).

As we can see in **Figure 2** and **Table 4**, the profound wells are corresponding to the LiH¹ and NaH² ones (D_e = 20350 cm⁻¹ and 15489 cm⁻¹, respectively) whereas the well depths of KH³, RbH⁴, CsH⁵ and FrH are significantly smaller.



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 Note that for alkali metal atoms (Li-Cs), the smaller ionization potential (43 487, 41 449, 35 009, 33 691, and 31 406 cm⁻¹) is related to the heavier alkali atom and has the larger electron affinity (experimental values are 4984, 4403, 4043, 3920 and 3803 cm⁻¹ for Li, Na, K, Rb and Cs, respectively⁹⁰). Whereas, the ionization potential IP (Fr) = 32 848 cm⁻¹ exceeds the IP(Cs) by 1442 cm⁻¹ and the EA (Fr)⁹¹ = 3678 cm⁻¹ (see also⁹²) is larger by only 117 cm⁻¹ than the one of Cs, nearly half-way between IP (Cs) and IP (Rb). Clearly, the mean error for the ionization potentials is 9 cm⁻¹ and for excitation energies 20 cm⁻¹. Especially for the heavier atoms, the electron affinities are less accurate, with errors from 4 to 9% for K, Rb, and Cs⁹⁰.

The PECS for all the ${}^{1}\Sigma^{+}$ states of the francium hydride have the same shape with the other alkali-metal hydrides (Li-Cs) H³⁻⁷.

In **Figure 3**, we have drawn the adiabatic potential curves for the eight ${}^{3}\Sigma^{+}$ states into the ionic limit Fr⁺+H⁻.

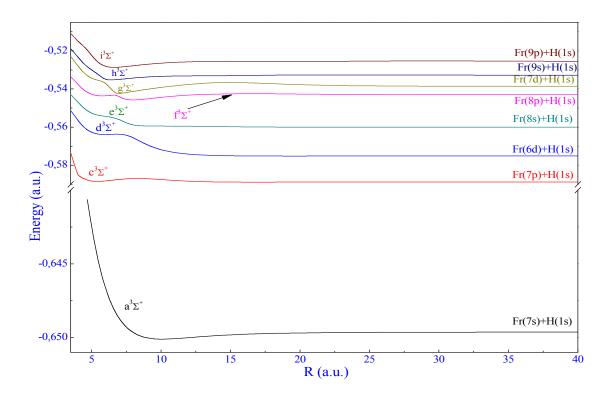


Figure 3. Eight adiabatic ${}^{3}\Sigma^{+}$ potential energy curves for the FrH molecule.

The first state $a^{3}\Sigma^{+}$ presents a shallow well at a remarkable large distance (R_e=10.63 a.u.), while the higher states (c, d, e and f) ${}^{3}\Sigma^{+}$ show two minima, the first one is between R= 5 a.u and 6 a.u, the other one at large distance has as origin the existence of the ionic–neutral avoided crossing. The different avoided crossing positions are given in **Table 3**. As an example, we can

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see an avoided crossing between $f^{3}\Sigma^{+}$ and $g^{3}\Sigma^{+}$ states at $R_{e}=6.9$ a.u. which explains the the contract of the double well depth for the $f^{3}\Sigma^{+}$ state.

Moving to the diabatic representation, we have displayed in **Figures 4 and 5** the diabatic PECs for the ${}^{1,3}\Sigma^+$ states, which are named as D₁₋₉ and d₁₋₈, respectively.

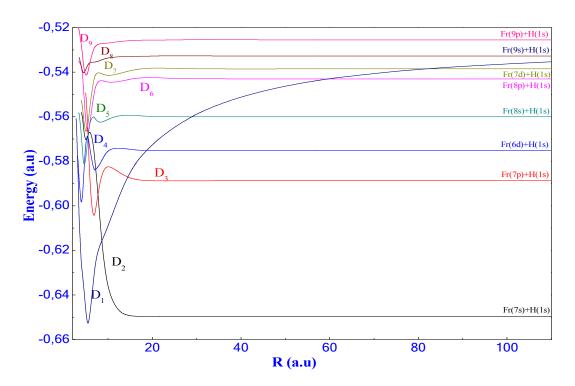


Figure.4. Diabatic ${}^{1}\Sigma^{+}$ potential energy curves dissociating below the ionic limit Fr⁺H⁻.

As we can see in the **Figure 4**, the avoided crossings in the adiabatic representation are changed into real crossings in the diabatic one. More clearly, the first diabatic PECs D₁ corresponding to the Fr⁺H⁻ ionic state crosses all the other states D₂₋₉ at different distances and conducts as -2/R behaviour. Moreover, the other states show lower polarization and van der Waals interactions. Therefore, the same interpretation mentioned in LiH³, NaH⁴, KH⁵, RbH⁶ and CsH⁷, the lower states for the diabatic potential energy curves have strongly repulsive forms at short distance corresponding to the nature of Rydberg states, which can enlarged to large distances for the high-excited states. The diabatic state D₂ crosses D₃ at R= 7.72 a.u., D₄ crosses D₅ around 5.5 a.u. and D₆ crosses D₇ near 5.25 a.u. In addition, **Figure 1** shows that the first diabatic ionic curve D₁ (Fr⁺H⁻) has a well depth at short distance R= 5.5 a.u. and crosses the 7s state at about 8.5 a.u. the 7p state approximately at 14.45 a.u. and the 7d around at 18.65 a.u. also this curve crosses the higher states at very large distances.

As we can see in **Figure 5**, the diabatic PECs of the ${}^{3}\Sigma^{+}$ states have the same interpretation of the Online DOI: 10.1039/C9NJ06391A the diabatic PECs of the ${}^{1}\Sigma^{+}$ states.

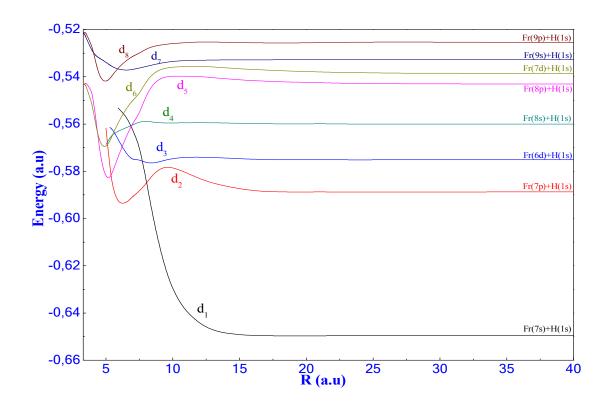


Figure.5. Diabatic ${}^{3}\Sigma^{+}$ potential energy curves dissociating below the ionic limit Fr⁺H⁻.

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We note that the first diabatic ionic curve d_1 (Fr⁺H⁻) has a well depth at the distance R= 10.8 a.u. and crosses the states 7p, 6d, 8s, 8p and 7d at about 8 a.u, 7.5 a.u, 6.8 a.u, 6.8 a.u and 6 a.u, respectively. As mentioned in the alkali hydride series¹⁻⁵, we found that the interaction of the singlet states is strong with the possible charge transfer states, which are usually not present in triplet states. Furthermore, we can see that the lower ${}^{3}\Sigma^{+}$ diabatic states present a strong repulsive behavior at short distances like for ${}^{1}\Sigma^{+}$ ones. We note that, we observe the diabatic crossings between two successive states of ${}^{3}\Sigma^{+}$ like d₁-d₂ are almost the same positions than the related ${}^{1}\Sigma^{+}$ ones.

1.2. The symmetries ${}^{1,3}\Pi$ and ${}^{1,3}\Delta$

For Π symmetry, the adiabatic PECS of $10^{1,3}\Pi$ for the francium hydride are presented in **Figure 6** and their spectroscopic constants are displayed in **Table 1 (c)**. Like for alkali-metal hydride¹⁻⁵, the ${}^{3}\Pi$ potential energy curves are a little deeper than ${}^{1}\Pi$ ones. Indeed, these states reach speedily to their asymptotic limit at around R=20a.u. Moreover, the $1{}^{3}\Pi$ have the deepest well

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at about 5.15 a.u and the potential depth De equals to 1620 cm⁻¹. It should be noted that all the cle Online states of Π symmetry have a single well depth.

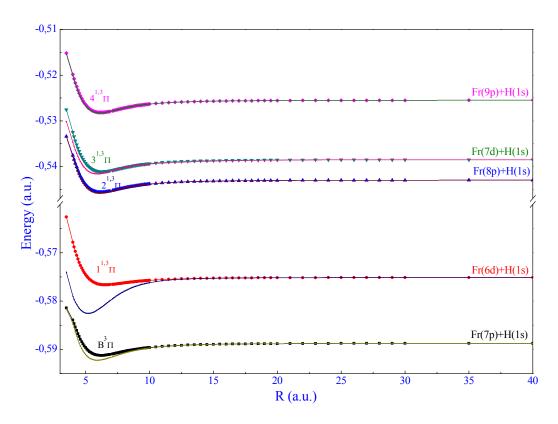


Figure 6.^{1,3}Π adiabatic potential energy curves for the FrH molecule.

Concerning the Δ symmetry, we have graphed the PECS of ^{1,3} Δ states in Figure S1 (Supporting Information) and their spectroscopic parameters are listed in Table 1(d). As usually observed for alkali-metal hydride³⁻⁷, the ¹ Δ and ³ Δ PECS, which tend rapidly to the same limit, are nearly degenerated. Obviously, the first states 1^{1,3} Δ have roughly the same value of the potential depth (De₁= 460cm⁻¹ and De₂= 471 cm⁻¹ for 1¹ Δ and 1³ Δ , respectively).

We have drawn in the diabatic representation the PEC_s for the symmetries ^{1,3} Π in **Figures 7** and for the ^{1,3} Δ symmetry in **Figure S2 (Supporting Information)**. Interestingly, the Singlet and Triplet states of Π and Δ symmetries are practically degenerate. As we can see in the **Figures 6-7 and S1-S2**, the curves of Π and Δ symmetries show smooth variations and are quite similar in their behavior. However, we observe that the wells of the diabatic representation are somewhat less deep than the adiabatic ones. There are no avoided crossing that can be seen in the adiabatic PEC_s, which is related to the small non-adiabatic interaction. Except for the first diabatic state of the Π symmetry crosses the second at around R= 5 a.u. is because of the

 nearly avoided crossing in the adiabatic PEC_S. To sum up, the diabatic curves have not a strong DOI: 10.1039/C98 JO6391A variation for the adiabatic one.

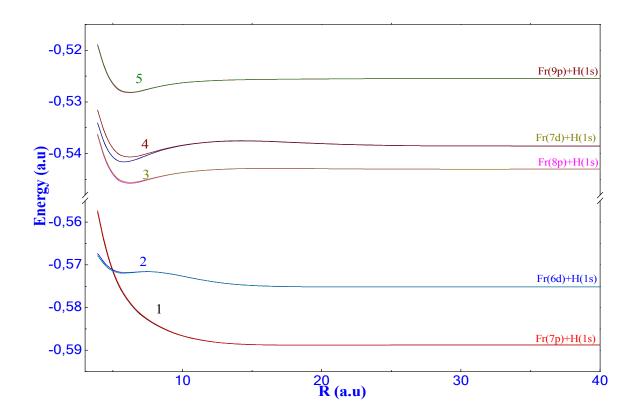


Figure.7. Diabatic ^{1,3}Π potential energy curves dissociating below the ionic limit Fr⁺H⁻.

2. Adiabatic and diabatic electric dipole moments

2.1. Adiabatic and diabatic Permanent Dipole Moment

The adiabatic PDM from the symmetries ${}^{1,3}\Sigma^+$, ${}^{1,3}\Pi$ are reported in **Figures 8-10** and for ${}^{1,3}\Delta$ Symmetry in **Figure S3 (Supporting Information)**. In fact, the PDM gives a direct picture of the ionic character in ${}^{1}\Sigma^+$ of the electronic wave function. This physical property has been shown in the alkali hydride series in the same symmetries **[1-5]**. Taken the work of the calcium hydride ion (CaH⁺)⁶⁵, the comportment of their PDM significantly can be a support for the identification of the various adiabatic electronic states below Ca²⁺+H⁻ and Ba²⁺+H⁻, respectively. As we can see in **Figure 8**, the PDM functions of ${}^{1}\Sigma^+$ states vary slowly at the short internuclear distances, which is shown in the zoom of this figure whereas at large distances, they present abrupt variations. We notice that one after one; each adiabatic state leads to a maximum and after that drops to zero. In addition, these curves reproduce by piece the (-R) function like a linear behavior of the ionic state (Fr⁺+H⁻) and pass through forming nodes between successive pieces when combined. Moreover, the avoided crossings are very weak that explain the sharpness of

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the slopes around the crux of the dipole. Whereas, we have seen the same behavior in the otherice Online alkali-metal hydride series³⁻⁷ whether, the avoided crossings in the potential energies curves and the crossings in the PDM figures were produced by the ionic curve.

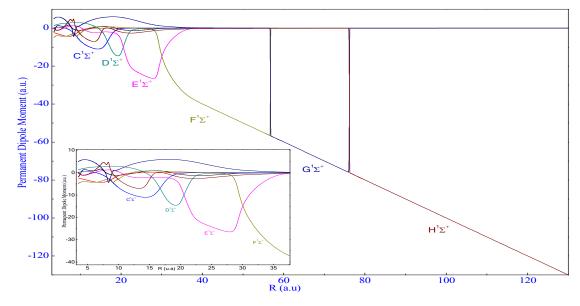


Figure 8. Permanent dipole moment for the ${}^{1}\Sigma^{+}$ states for the FrH with zoom for the PDM at short distance.

The important consequences of these crossings concern the efficiency of the charge transfer or the excitation, for instance, neutralization cross sections essentially relied on these crossing series, therefore, their important field for charge transfers in many astrophysical conditions^{31, 93-95}. This physical property has been shown in the alkali hydride series in the same symmetries³⁻⁷.

The Permanent Dipole Moment figures for ${}^{3}\Sigma^{+}$, ${}^{1,3}\Pi$ and ${}^{1,3}\Delta$ are shown in **Figures 9** and **10**. Let us begin by the PDM curves for ${}^{3}\Sigma^{+}$ symmetry; **Figure 9** indicates the significant variations at short distances before 20a.u. These functions are not negligible and have considerable influence on higher excited states.

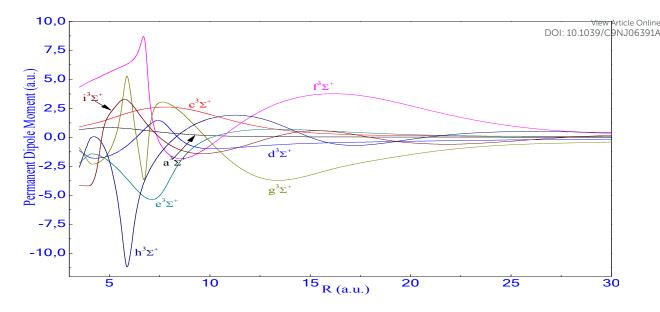


Figure 9. Permanent dipole moment for ${}^{3}\Sigma^{+}$ as a function of the internuclear distance for the FrH.

Then, they increase and vanish at a large distance. For instance, $h^{3}\Sigma^{+}$ and $g^{3}\Sigma^{+}$ states present maxima (μ_{max} = -11.58a.u. and -3.73a.u.) respectively, at the distance R= 5.9 a.u. and 13.5a.u, respectively. Then it slowly decreases. These positions correspond to the avoided crossing in their potential energies curves. The PDM curves of symmetry ^{1,3} Π show an important variation at short distances and tend rapidly to zero (see **Figure 10**).

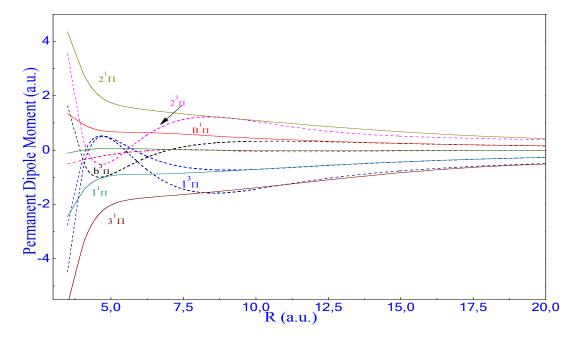


Figure 10. Permanent dipole moment for the $^{1,3}\Pi$ states for the FrH.

In the **Supporting Information (Figure S3)**, we observe that PDM functions of ${}^{1}\Delta$ are identical to the ${}^{3}\Delta$ ones, which explains the degeneracy in their PECs.

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Concerning the diabatic representation, the curves of the PDM are displayed in Figures 11/iant tele Online 12 for $^{1,3}\Sigma^+$ states.

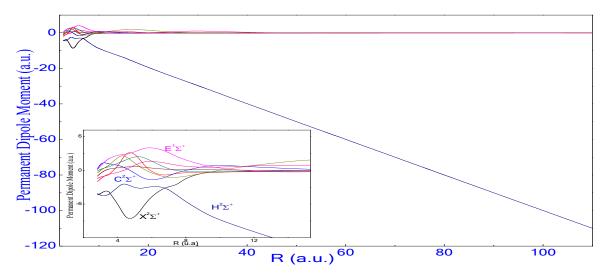


Figure.11. Permanent dipole moment for the ${}^{1}\Sigma^{+}$ diabatic states of FrH.

As shown for the all alkali hydride series (LiH, NaH, KH, RbH and CsH)³⁻⁷, the diabatic PDM curves allow important information on these molecules. As we can see in **Figure 11**, we obtain a straight line, while the neutral diabatic dipole of the states decreases rapidly to zero when R increases. Interestingly, this simple shape reflecting the physics expected for the PDM of the various diabatic states is in uniformity with basic electrostatic considerations and gives strong support to the diabatisation method used.

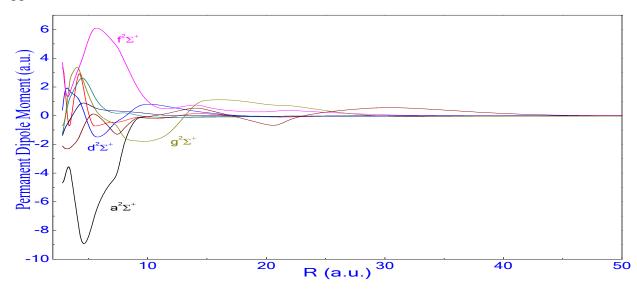


Figure.12. Permanent Dipole Moment for ${}^{3}\Sigma^{+}$ diabatic states of FrH.

2.2. Adiabatic and diabatic TDM

It is attractive to exemplify the curves of the TDM in the adiabatic and diabatic representation sticle online which help us to make the information for future photo-association experiments. The adiabatic curves have been presented in the **Figures 12** and **13** for ${}^{1}\Sigma^{+}$ and ${}^{3}\Sigma^{+}$, respectively, and they have been investigated for the first time.

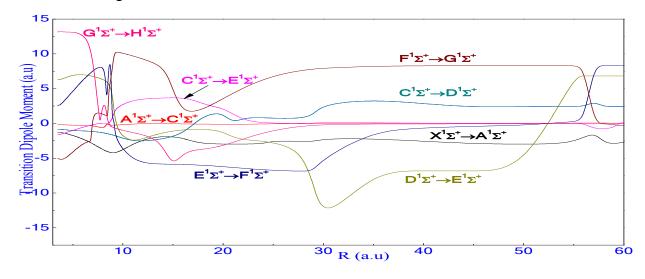


Figure 13. Transition dipole moment for selected excited states for symmetry ${}^{1}\Sigma^{+}$.

We observe in the **Figures 12** many peaks that are corresponding to the avoided crossings in the PECS at these distances. To explain more, the D-E TDM present a peak around 30 a.u. which corresponds to the avoided crossing between D and E electronic states. In addition, the large peak is detected for the E-F TDM curves, which correspond to the crossing of the E-F PECS at the distance 60 a.u. Interestingly, when the peak is higher and less wide, the avoided crossing was less compared to the A-C case. Similarly, the same remark is found in the work of the other alkali-metal hydride³⁻⁷. We have also conveyed in **Figures 13 and 14** the TDM curves for symmetry ${}^{1,3}\Sigma^+$. Noteworthy, most of the TDM curves do not have a peak, which is related to the repulsive shape in their PECS and the lack of the avoided crossing. Furthermore, the (g-h) ${}^{3}\Sigma^+$ present clearly a peak at R= 6.9 a.u, which corresponds to the position of the avoided crossing between g and h states in their PECS.

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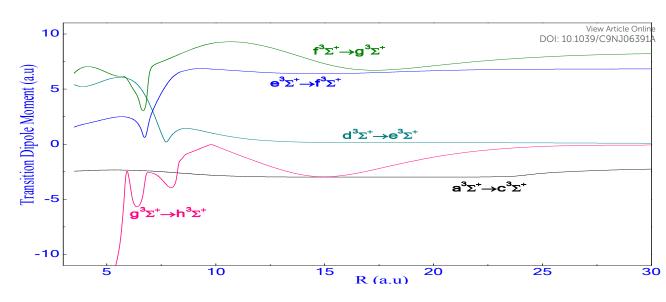


Figure 14. Transition dipole moment for selected excited states for symmetry ${}^{3}\Sigma^{+}$.

In general, the corresponding avoided crossings in the PECs are then displayed around the large internuclear distances and the related maximum values in the TDM functions. Moreover, the most significant transitions which are between two successive states, for example, the transitions between (F-G) ${}^{1}\Sigma^{+}$ and (G-H) ${}^{1}\Sigma^{+}$ states are more important than the others.

Indeed, for the first time, we have investigated the diabatic curves of the TDM for the first state ${}^{1}\Sigma^{+}$, which are showed in **Figures S4 (Supporting Information)**. Furthermore, the diabatic curves show smoother variations of their physical characteristics at a short inter-nuclear distance while the adiabatic states present strong variations; it is difficult to pursue their physical acumen with a very limited number of states. As mention before, the avoided crossing in the adiabatic curves can be showed as peaks in their curves of TDM.

At large distances, the diabatic representation drops to zero and does not have any variation, while, in the adiabatic representation their variation continue to R=60 a.u.

3. Vibrational levels of FrH

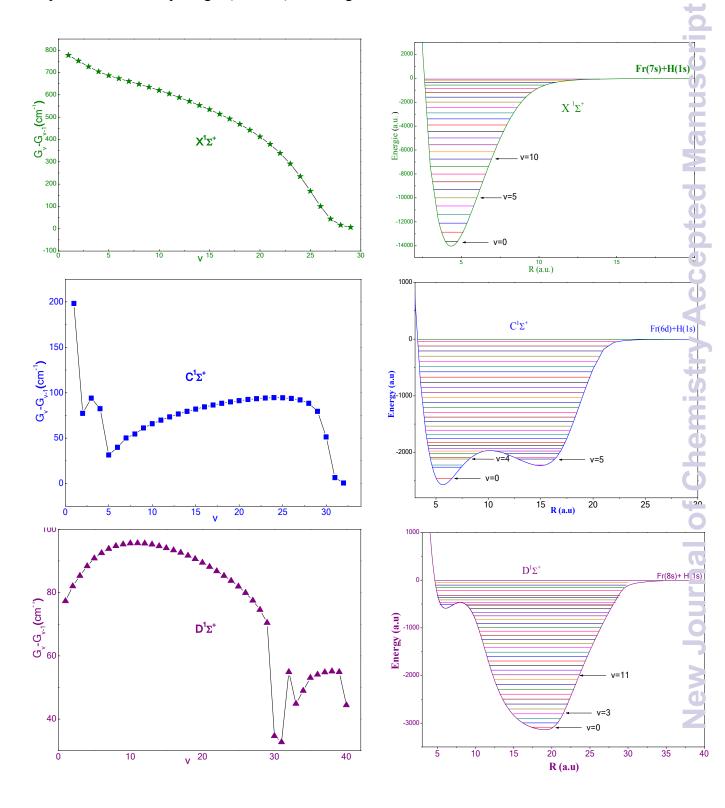
In this section, we have studied the spacing of the vibrational level for $^{1,3}\Sigma^+$, $^{1,3}\Pi$ and $^{1,3}\Delta$ symmetries, for the first time. We have interpolated the vibrational levels by least-squares method (Numerov Program), which is written as following:

$$E_{v} = V(R_{e}) + \omega_{e}(v + \frac{1}{2}) - \omega_{e}\chi_{e}(v + \frac{1}{2})^{2}$$
(12)

The NUMEROV program is prepared to determine the spectroscopic constants ω_e and $\omega_e \chi_e$ from vibrational energy levels G_v . The equilibrium distance R_e and B_e are deduced at the minimum of the V(R) potential. Since the vibrational wave functions can be calculated at the

same moment for the two different electronic states, we can also get the quantities to representicle Online the vibronic transition like an oscillator strength.

As shown in **Figure 15**, the adiabatic PECS for the (X, C, D) ${}^{1}\Sigma^{+}$ and their vibrational levels are plotted with their spacing's (G_{v} - G_{v-1}) awarding to the vibrational levels' number v.



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Figure 15. Vibrational spacing (left) and potential energy curves (right) for (X, C and D) $^{1\Sigma^{+}}_{DOI: 10.1039/C9NJ06391A}$ FrH.

Therefore, $X^{1}\Sigma^{+}$ shows a deep potential well, which contains 27 vibrational levels. For the first vibrational levels, we observe a linear behavior reflecting an anharmonic form like Morse in their PECS. The spacing's become smaller and disappear at the dissociation limit (Fr (7s) + H(1s)). The same remark is applicable to the states that have a single well depth. The spacing for the C¹\Sigma⁺ shows a sudden variation that indicates the presence of a second well. Then, we can see a slow variation from v=3 to v=5 considering that the second well is wider. It is worth noting that, accidental quasi-degeneracy appears one time (v= 4, 5) and related to states, which are suitable to different wells. The D¹\Sigma⁺ state has 41 vibrational levels which begin with an abrupt behavior up to v=29 then, a sudden change emerges from v=30 to v=33 reflecting a second wide anharmonic well.

In **Figure 16**, we have traced the vibrational level spacing for the other states of symmetries ${}^{1}\Sigma^{+}$. The E, F and G states trap various vibrational levels and quasi-degeneracies corresponding to deep potential wells and the appearance of the second well. We notice that the $G^{1}\Sigma^{+}$ state has 146 vibrational levels, which are plentiful, and very tight, explained by the appearance of three depth wells.

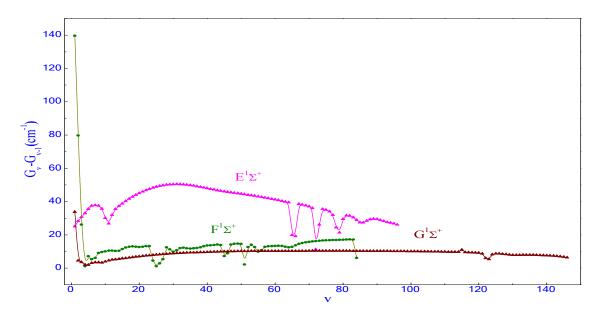


Figure 16. Vibrational level spacing for (E, F and G) ${}^{1}\Sigma^{+}$ states of FrH.

We listed in **Table 5** and **6**, the vibrational levels for other states of ${}^{3}\Sigma^{+}$, ${}^{1,3}\Pi$ and ${}^{1,3}\Delta$ symmetries, which have a fewer vibrational level number. Therefore, that is explained by the repulsive shape in their potential curves. The most of these spacings are constant and linear; this is correlated with the anharmonicity of the potential wells.

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V	$a^{3}\Sigma^{+}$		$a^{3}\Sigma^{+}$ $c^{3}\Sigma^{+}$ $f^{3}\Sigma^{+}$		h $^{3}\Sigma^{+}$		i ³ Σ ⁺			
	Energy	Spacing	Energy	Spacing	Energy	Spacing	Energy	Spacing	Energy	Spacing
0	-89.99		-18.56		-482.68		-439.75		-585.79	
1	-51.45	38.54	-5.02	13.54	-288.90	193.78	-251.17	188.58	-397.58	188.21
2	-20.45	30.99	-0.40	4.62	-162.70	126.2	-130.91	120.26	-245.11	152.47
3	-8.06	12.4			-74.53	88.17	-69.31	61.6	-128.77	116.34
4	-1.63	6.43			-12.01	62.52	-43.22	26.08	-45.79	82.99
5							-15.67	27.56	-11.17	34.62
6									-0.82	10.35
7									14.48	15.3
8									31.44	16.96

 $\textbf{Table 5. Vibrational level spacing } (G_{v+1}-G_v) \text{ of } (a, c, f, h \text{ and } I) \ {}^{3}\Sigma^{+} \text{states } (\text{in } cm_{\text{DOI: 10.1039/C9NJ06391A}}^{-1}) \\ \overset{\text{View Article Online Control of Con$

As we can see in **Table 5**, the vibrational level of symmetry ${}^{3}\Sigma^{+}$ does not exceed eight levels and shows a linear behavior that is reflected the simple wells in their PECs. The same analysis for the symmetries ${}^{1,3}\Pi$ and ${}^{1,3}\Delta$ (see **Table 6**). More clearly, the vibrational levels of ${}^{1}\Delta$ are roughly identical to the one for ${}^{3}\Delta$ that is related to the degeneracy in their PECs. In summary, the spacing vibrational levels are investigated here for the first time for all symmetries and present important information considering the shape of the PECS.

V	$B^{1}\Pi$	1 ¹ Π	2 ¹ Π	3 ¹ Π	b ³ П	1 ³ П	2 ³ Π	3 ³ П	$1^{1}\Delta$	$1^{3}\Delta$	$2^{1}\Delta$	$2^{3}\Delta$
1	143.14	105.71	153.21	152.23	184.66	270.24	164.22	177.01	136.38	138.73	152.87	153.71
2	113.25	73.01	121.01	120.47	156.93	258.03	131.41	135.66	100.79	103.35	120	120.02
3	81.69	46.98	87.54	88.87	119.05	235.04	93.86	92.15	69.37	70.54	85.38	85.5
4	56.7	24.32	60.61	61.63	86.34	203.64	62.31	62.64	41.72	43.05	57.42	57.46
5	34.8	11.87	35.38	33.13	59.26	170.79	39.67	42.87	20.95	21.74	31.85	32.01
6	21.09		19.34	16.71	34.76	135.57	23.13	30.41	11.05	11.53	18.36	18.42
7	10.27				18.46	101.88	12.55	22.89				
8					10.42	67.21						
9						24.82						
10						12.79						

IV Conclusion

This study is an investigation of the diabatic and adiabatic electronic properties of FrH molecule, including PECs for all symmetries ${}^{1,3}\Sigma^+$, ${}^{1,3}\Pi$ and ${}^{1,3}\Delta$, vibrational level spacing and the PDM and the TDM functions. The adiabatic calculation method is carried out in the Born-Oppenheimer approximation. The pseudo-potentials and the Full Configuration Interaction

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methods are applied here. Moreover, we have studied a diabatic study for this molecule/ PTHCle Online DOI: 10.1039/C9NJ06391A using the theory of the variational effective Hamiltonian combined to an active overlap matrix. The most striking result to emerge from the data is that the $1\Sigma^+$ states show a significant series of avoided crossing. We observe that the highly potential part is related to the Fr^++H^- ionic state similarly to the XH systems where X= Li, Na, K, Rb, Cs³⁻⁷. These curves have the same behavior with the PECS of the other alkali-metal hydride. The PECs for the 1.3Π symmetries present a similar shape and for 1Δ and 3Δ are roughly identical.

The diabatic survey produces huge acumen into the strong interactions between the adiabatic states. From our results, we can see the ionic-neutral crossings at intermediate and large distances, exactly in the ${}^{1}\Sigma^{+}$ states. Moreover, the PDM functions show the appearance of (-R) curve for the ionic limit (Fr⁺+H⁻). The various crossings in PECs result from the unusual shapes with multiplicity wells that are related to the linear behavior in PDM curves and the peaks in TDM curves. More clearly, the PDM curves reproduce by piece the (-R) function like a linear behavior of the ionic state (Fr⁺+H⁻) and pass through forming nodes between successive pieces when combined. The important consequences of these crossings are for the photo-association and spontaneous emission or the radiative charge exchange^{31, 94}. In fact, the PDM functions give a direct explanation of the ionic character of the electronic wave function for FrH. These new results are very important for further theoretical and experimental researches, for example in spectroscopy⁹⁶ or collision⁹⁷⁻¹⁰¹ fields.

These diabatic results can be applied to calculate the vibronic shifts and radiatives as well as non-radiative lifetimes¹⁰²⁻¹¹⁰. In addition, inelastic collision cross sections studies could be made for instance for the process of charge transfer, which can be interesting for many fields in physics or maybe in astrophysics.

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References

- ¹J. G. Hill, K. A Peterson. J. Chem. Phys. 147, 244106 (2017).
- ²T. Noro, M. Sekiya, and T. Koga, Theor. Chem. Acc. 121, 289 (2008).
- ³F.X. Gadéa and T. Leininger, Theor. Chem. Acc. 116, 566–575 (2006).
- ⁴N. Khelifi, J. Phys. Chem. A, **113**, 8425–8433 (2009).
- ⁵N. Khelifi, B. Oujia, and F. X. Gadea, J. Chem. Phys. **116**, 2879 (2002).
- ⁶N. Khelifi, W. Zrafi, B. Oujia, and F. X. Gadea, Phys. Rev. A 65,042513 (2002).

⁷W. Zrafi, N. Khelifi, O. Brahim, and F. X. Gadea, J. Phys. B: At. Mol. Opt. Phys. **39**, 3815 (2006).

⁸T. Noro, M. Sekiya, T. Koga, Theor Chem Acc 109,85 (2003).

- ⁹W. C. Stwalley and W. T. Zemke, J. Phys. Chem. Ref. Data 22, 87 (1993).
- ¹⁰V. M. Garcia, R. Caballol, and J. P. Malrieu, J. Chem. Phys. 109, 504 (1998).
- ¹¹A. Boutalib and F. X. Gadea, J. Chem. Phys. **97**, 1144 (**1992**).
- ¹²B. Lepetit, M. Le Dourneuf, J. M. Launay, and F. X. Gadea, Chem. Phys. Lett. **135**, 377 (1987).
- ¹³F. X. Gadea and M. Pelissier, J. Chem. Phys. **93**, 545 (1990).
- ¹⁴F. Gemperle and F. X. Gadea, J. Chem. Phys. **110**, 111 97 (**1999**).
- ¹⁵M. Dolg, Mol. Phys. **93**, 141 (**1996**).
- ¹⁶P. Fuentealba, O. Reyes, H. Stoll, and H. Preuss, J. Chem. Phys. 87, 5338 (1987).
- ¹⁷M. Aymar, J. Deiglmayr and O. Dulieu, Can. J. Phys. **87**, 543–556 (**2009**).

New Journal of Chemistry Accepted Manuscript

¹⁸R. L. Stephen, W. B. Charles, and H. Partridge, J. Chem. Phys. 85 (9) (1986).

¹⁹J. Hooper, P. Baettig, and E. Zurek, J. Applied Phys. **111**, 112611 (2012).

²⁰G. Moritz, A. Wolf, and M. Reihera, J. Chem. Phys., 123, 184105 (2005).

²¹K. Boguslawski, P. Tecmer, G. Barcza, Ö. Legeza and M. Reiher, Chem. Theory Comput. 9, 2959-2973 (2013).

²²K. R. S. Chandrakumar* and Swapan K. Ghosh, Nano Letters Vol. 8, No. 1, 13-19 (2008).

²³ L. Yan; Y. Qu; C. Liu; J. Wang; R. J. Buenker, Ab Initio Many-Electron Study for the

Low-Lying States of the Alkali Hydride Cations in the Adiabatic Representation. J. Chem. Phys., 136, 124304 (2012).

²⁴ M. Carnell; S. D. Peyerimhoff; B. A. Hess, Ab Initio MRDCI Calculations on the Cesium

Hydride (CsH) Molecule. Z. Phys. D. At., Mol. Clusters, 333, 317-333 (1989).

²⁵R. S. Ram and P. F. Bernath, J. Mol. Spectrosc. 283, 18 (2013).

- ²⁶J. Zhang, L. Zhang, T. Cui, Y. Li, Z. He, Y. Ma, and G. Zou, Phys. Rev. B 75, 104115 (2007).
- ²⁷G. Roma, C. M. Bertoni and S. Baroni, Solid State Commun. 98 203 (1996).

²⁸C. Crepin, J. Verges, and C. Amiot, Chem. Phys. Lett. 112, 10 (1984).

²⁹R. W. Numrich and D. G. Truhlar, J. Phys. Chem. **79**, 2745 (**1975**).

³⁰G. D. Barrera, D. Colognesi, P. C. H. Mitchell and A. J. Ramirez-Cuesta, J. *Chem. Phys.* **317**, 119 (2005).

³¹D. R. Stephens and E. M. Lilley, J. Appl. Phys. **39**, 177 (1968).

³²A.K. Belyaev, J. Grosser, J. Hahne, and T. Menzel. Phys. Rev. A, 60, 2151 (1999).

- ³³A.K. Belyaev and P.S. Barklem. Phys. Rev. A, **68**, 062703 (**2003**).
- ³⁴C.M. Dutta, P. Nordlander, M. Kimura, and A. Dalgarno. Phys. Rev. A, 63, 022709 (2001).
- ³⁵L. Mendez, I.L. Cooper, A.S. Dickinson, O. Mo, and A. Riera. J. Phys. B, 23, 2797 (1990).

³⁶H. Croft, A.S. Dickinson, and F.-X. Gadéa. J. Phys. B, **32**, 81 (1999).

³⁷R. Curik and C.H. Greene. Phys. Rev. Lett. **98**, 173201 (2007).

³⁸B. Friedrich and D. Herschbach. J. Phys. Chem. A, **103**,10280 (1999).

³⁹P. Indelicato, P. J. Mohr, Theor. Chem. Acta **80**, 207-214 (1991).

⁴⁰J. A. Behr, S. B. Chahn, S. B. Dutta, A. Görlitz, A. Ghosh, G. Gwinner, L. A. Orozco, G. D.

Sprouse and F. Xu Hyperfine Interact. 81 197 (1993).

⁴¹M. A. Bouchiat and C. Bouchiat Rep. Prog. Phys. **60** 1351 (1997).

⁴²J. Zhang (张颉颃), M. Tandecki, R. Collister, S. Aubin, J. A. Behr, E. Gomez, G. Gwinner,

- L. A. Orozco, M. R. Pearson, and G. D. Sprouse Phys. Rev. Lett. 115, 042501 (2015).
- ⁴³C. Fry and M. Thoennessen, Atomic Data and Nuclear Data Tables **99**, 497–519 (2013).

60

1

View Article Online DOI: 10.1039/C9NJ06391A

3 4

5 6

7 8

9

10

11

12 13

17:40 17:40 17:40 17:40

2020 Downloaded by 4

bilished 139

Ä1

42

43 44

45 46

47

48 49

50 51

52 53

54

55 56

57 58

59 60 ⁴⁴J. P. Adolff, G. B. Kauffman, Francium (Atomic Number 87), the Last Discovered Natural Cle Online DOI:10:1039/C9NJ06391A Element. Chem. Educ. **10**, 387–394–1430–4171 (**2005**).

- ⁴⁵J. E. Sansonetti, J. Phys. and Chem. Ref. Data, **36** 497-507 (**2007**).
- ⁴⁶L. H. Delmau, J. Moine, S. Mirzadeh and B. A. Mayer, J. Phys. Chem. B **117**, 9258-9261 (2013).
- ⁴⁷I. Budincevic, J. Billowes, M. L. Bissell, T. E. Cocolios, R. P. de Groote, S. De Schepper, V.
- N. Fedosseev, K. T. Flanagan, S. Franchoo, R. F. Garcia Ruiz, H. Heylen, K. M. Lynch, B. A.
- Marsh, G. Neyens, T. J. Procter, R. E. Rossel, S. Rothe, I. Strashnov, H. H. Stroke and K. D. A. Wendt, PHYS. REV. C **90**, 014317 (**2014**).
- ⁴⁸J. Singh Jaggi, S. V. SESHAN, M. R. MCDEVITT, G. SGOUROS, E. ,HYJEK, and D. A. SCHEINBERG, Int. J. Radia. Oncolo. Biol. Phys., **64**, 1503–1512, **(2006)**.
- ⁴⁹M. Aymar, O. Dulieu and F. Spiegelman, J. Phys. B: At. Mol. Opt. Phys. **39**, S905–S927 (2006).
- ⁵⁰W. Kutzelnigg and W. Liu, J. Chem. Phys. **123**, 241102 (2005).
- ⁵¹D. Peng and M. Reiher, Theor. Chem. Acc. **131**, 1081 (**2012**).
- ⁵² L. Wenjian, Handbook of Computational Chemistry (2017).
- ⁵³ L.L.Foldy, SA. Wouthuysen On the Dirac theory of spin 1/2 particles and its nonrelativistic limit. Phys Rev 78:29 (1950).
- ⁵⁴Douglas M, Kroll NM (1974) Quantum electrodynamical corrections to the fine structure of helium. Ann Phys 82:89
- ⁵⁵W. Kutzelnigg, Relativistic one-electron Hamiltonians 'for electrons only' and the variational treatment of the Dirac equation. Chem Phys 225:203 (1997).
- ⁵⁶ T. Nakajima, K. Hirao, J Chem Phys 113:7786 (2000).
- ⁵⁷J. Deiglmayr, M. Aymar, R. Wester, M. Weidemüller, and O. Dulieu, J. Chem. Phys. **129**, 064309 (2008).
- ⁵⁸Ph. Durand, J. C. Barthelat, Theor. Chim. Acta, **38**, 283 (**1975**).
- ⁵⁹Ph. Durand, J. C. Barthelat, Chem. Phys. Lett., 27, 191–194 (1974).
- ⁶⁰H. Habli, H. Ghalla, B. Oujia, F. X. Gadea, Eur. Phys. J. D 64, 5 (2011).
- ⁶¹W. Gaied, H. Habli, B. Oujia, F. X. Gadea, Eur. Phys. J. D, 62, 371 (2011).
 ⁶²W. Gaied, B. Oujia, Int. J. Nanoparticles, 3, 160 (2010).
- ⁶³L. Mejrissi, H. Habli, H. Ghalla, B. Oujia, F. X. Gadea, J. Phys. Chem. A, **117**, 5503 (**2013**).
 ⁶⁴K. Abdesslem, L. Mejrissi, N. Issaoui, B. Oujia, F.X. Gadéa, J. Chem. Phys. **36**, 117, 8925-8938 (**2013**).
- ⁶⁵H. Habli, R. Dardouri, B. Oujia, F.X. Gadéa. J. Chem. Phys. 115, 14045-14053 (2011).

⁶⁶M. Chaieb, H. Habli, L. Mejrissi, B. Oujia, and F. X. Gadea, J. Quantum Chem <u>114</u> 73 Price Online 747 (2014).

⁶⁷H. Habli, L. Mejrissi, N. Issaoui, S. J. Yaghmour, B. Oujia, and F. X. Gadea, Int. J. of Quantum Chem., **115**, 172-186 (**2015**).

⁶⁸R. Guérout, M. Aymar, and O. Dulieu, Phys. Rev. A 82, 042508 (2010).

1 2

3 4

5 6

7 8

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10

11

12 13

17:40 Md 17:

2020 Downloaded by 4

bilished 139

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43 44

45 46

47

48 49

50 51

52 53

54

55 56

57 58

59 60 ⁶⁹R. Dardouri, K. Issa, B. Oujia and F. Xavier Gadéa, Int. J. of Quant. Chem. **112**, 2724-2734 (2012).

⁷⁰R. Dardouri, H. Habli, B. Oujia, F. X. Gadéa, Chem. Phys., **399**, 65–79 (2012).

- ⁷¹N. Khémiri, R. Dardouri, B. Oujia, and F. X. Gadea, J. Phys. Chem. A. **117** 8915-8924 (**2013**).
- ⁷²R. Dardouri, H. Habli, B. Oujia, F.X. Gadéa. J. of Comp. Chem. 34, 2091-2099 (2013).
- ⁷³N. Khelifi, B. Oujia, F.X. Gadea, J. of Phys. and Chem. Ref. Data. 36, 191-202 (2007).
- ⁷⁴H. Habli, L. Mejrissi, H. Ghalla, S. J. Yaghmour, B. Oujia and F. X. Gadéa. Mol. Phys. **114**, 1568-1582 (**2016**).
- ⁷⁵S. Jellali, H. Habli, L. Mejrissi, M. Mohery, B. Oujia, F. X. Gadéa J. Mol. Phys. **114**, 2910 (2016).
- ⁷⁶H. Souissi, L. Mejrissi, H. Habli, At. A. Al-Ghamdi, B. Oujia, F. X. Gadea, Chem. Phys. 490, 19–28 (2017).
- ⁷⁷H. Souissi, S. Jellali, M. Chaieb, H. Habli, B. Oujia and F. X. Gadéa, J. of Quan. Spect. & Rad. Tran., **200**, 173-189 (**2017**).
- ⁷⁸Mtiri, S., Mejrissi, L., Habli, H., Al-Ghamdi, A.A., Oujia, B., Gadéa, F.X., Comput. and Theo. Chem. **1114, 15** 33-46 (**2017**).
- ⁷⁹R. Hamdi, K. Abdessalem, R. Dardouri, At. A Al-Ghamdi, B. Oujia and F. X. Gadéa, J. Phys.
 B: At. Mol. Opt. Phys., **51**, 025004 (2017).
- ⁸⁰W. Müller, J. Flesh, W. Meyer, J. Chem. Phys., 80, 3297 (1984).
- ⁸¹M. Foucrault, Ph. Millie, J. P. Daudey, J. Chem. Phys. 96, 1257 (1992).

⁸²I. S. Lim, J. K. Laerdahl and P. Schwerdtfeger J. Chem. Phys. **116**, 172 (2002).

⁸³Yu. Ralchenko, A. Kramida, Reader J and NIST ASD Team 2011 NIST Atomic Spectra

Database (version 4.1). Available at: http://physics.nist. gov/asd/.

- ⁸⁴F.X. Gadea, Phys. Rev. A. **36**, 2557 (**1987**).
- ⁸⁵F.X. Gadea, Phys. Rev A **43** 1160 (1991).
- ⁸⁶Romero, T.; Aguilar, A.; Gadea, F.X. J.Chem. Phys., **110**, 16219 (**1999**).
- ⁸⁷Gadea, F. X.; Kuntz, P. J. Mol. Phys., 63, 27 (1988).
- ⁸⁸S R. Langhoff, C W Bauschlicher and H Jr Partridge, J. Chem. Phys. 85, 5158 (1986).
- ⁸⁹W. C. Stwalley, W. T. Zemke and S. C. Yang, J. Chem. Ref. Data 20, 153 (1991).

4

5 6

7 8

9

10 11

12 13

17:40 Md 17:

2020 Downloaded by 4

bilished 139

Ä1

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43 44

45 46

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48 49

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52 53

View Article Online DOI: 10.1039/C9NJ06391A

- ⁹¹ E. Eliav, M. J. Vilkas, Y. Ishikawa and U. Kaldor J. Chem. Phys. 122, 224113 (2005).
- ⁹²C. H. Greene Phys. Rev. A 42, 1405 (1990).
- ⁹³A.S. Dickinson, R. Poteau, F.X. Gadea, J. Phys. B 32,5451 (1999).
- ⁹⁴A.K. Belyaev, P.S. Barklem, A.S. Dickinson, F.X. Gadea, Phys. Rev. A 81, 032706 (2010).
- ⁹⁵P.S. Barklem, A.K. Belyaev, A.S. Dickinson, F.X. Gadea, Astron. Astrophys. **519**, A20 (2010).
- ⁹⁶O.L. Malta, H.F. Britob, J.F.S. Menezesb, F.R. Gongalves e Silva, S. Alves Jr., F.S. Farias Jr., A.V.M. de Andrade, J. of Lumi. **75**, 255-268 (**1997**).
- ⁹⁷ P. S. Barklem and P. J. O'Mara, Mon. Not. R. Astron. Soc. 311, 535 (2002).
- ⁹⁸N. Zahzam, T. Vogt, M. Mudrich, D. Comparat, and P. Pillet, Phys. Rev. Lett. **96**, 023202 (2006).
- ⁹⁹P. Staanum, S. D. Kraft, J. Lange, R. Wester, and M. Weidemüller, Phys. Rev. Lett. **96**, 023201 (2006).
- ¹⁰⁰E. R. Hudson, N. B. Gilfoy, S. Kotochigova, J. M. Sage, and D. De Mille, Phys. Rev. Lett. **100**, 203201 (2008).
- ¹⁰¹M. T. Hummon, T. V. Tscherbul, J. Klos, H.-I. Lu, E. Tsikata, W. C. Campbell, A. Dalgarno, and J. M. Doyle, Phys. Rev. Lett. **106**, 053201(**2011**).
- ¹⁰²F. Gemperle, F. X. Gadea, Europhys. Lett. 48, 513 (1999).
- ¹⁰³A. Yiannopouplou, G. H. Jeung, H. S. Lee, Y. S. Lee, Phys. Rev. A. **59**, 1178 (**1999**).
- ¹⁰⁴T.V. Tscherbul, Buchachenko, A.A. New Journal of Physics .17, 1, (2015).

¹⁰⁵A. S. Dickinson, F. X. Gadéa. Mont. Not. Roy. Astr. Soc. **318**, 1227 (2000).

- ¹⁰⁶H. Croft, A.S. Dickinson, F.X. Gadéa, Monthly Notices of the Royal Astronomical Society.**304**, 327 (1999).
- ¹⁰⁷Y .L. Huang, W. T. Luh, G. H. Jeung, F. X. Gadea, J. Chem. Phys. 113, 683 (2000).
- ¹⁰⁸F.X Gadéa. T. Leininger. A.S. Dickinson. European Physical Journal D. 15, 251 (2001).
- ¹⁰⁹C. Y. Wu, W. T. Luh, F. X. Gadéa, W. C. Stwalley. J. Chem. Phys. **128**, 064303 (2008).
- ¹¹⁰R.F. Garcia Ruiz, R. Berger, J. Billowes, C.L. Binnersley, M.L. Bissell, A.A. Breier, A.J. Brinson, K. Chrysalidis, T. Cocolios, B. Cooper, K.T. Flanagan, T.F. Giesen, R.P. de Groote, S.Franchoo, F.P. Gustafsson....., Nuclear Theory, **(2019)**.

View Article Online DOI: 10.1039/C9NJ06391A