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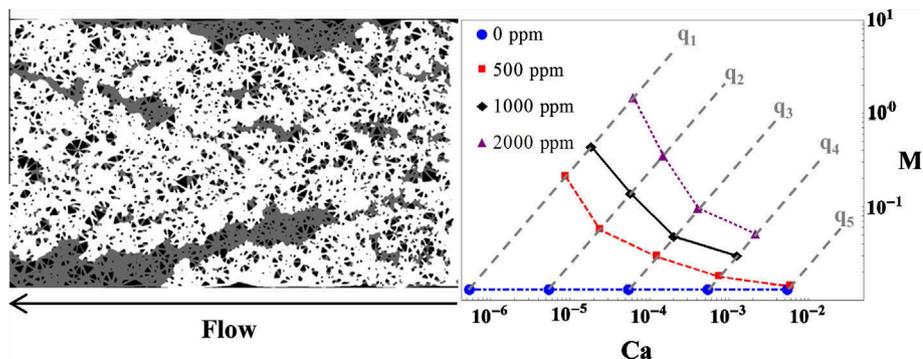
# Effects of shear-thinning fluids on residual oil formation in microfluidic pore networks

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## GRAPHICAL ABSTRACT



## ABSTRACT

Two-phase immiscible displacement in porous media is controlled by capillary and viscous forces when gravitational effects are negligible. The relative importance of these forces is quantified through the dimensionless capillary number  $Ca$  and the viscosity ratio  $M$  between fluid phases. When the displacing fluid is Newtonian, the effects of  $Ca$  and  $M$  on the displacement patterns can be evaluated independently. However, when the injecting fluids exhibit shear-thinning viscosity behaviour the values of  $M$  and  $Ca$  are interdependent. Under these conditions, the effects on phase entrapment and the general displacement dynamics cannot be dissociated. In the particular case of shear-thinning aqueous polymer solutions, the degree of interdependence between  $M$  and  $Ca$  is determined by the polymer concentration. In this work, two-phase immiscible displacement experiments were performed in micromodels, using shear-thinning aqueous polymer solutions as displacing fluids, to investigate the effect of polymer concentration on the relationship between  $Ca$  and  $M$ , the recovery efficiency, and the size distribution of the trapped non-wetting fluid. Our results show that the differences in terms of magnitude and distribution of the trapped phase are related to the polymer concentration which influences the values of  $Ca$  and  $M$ .

**Keywords:**  
Shear-thinning fluids  
Microfluidic analysis  
Polymer flooding  
Oil recovery  
Immiscible displacement

## 1. Introduction

On average, two-thirds of the original oil in geological reservoirs remains unrecovered, even after waterflooding [1,2]. The unrecovered oil becomes trapped in the reservoir forming discontinuous or continuous phase in swept or unswept reservoir zones,

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respectively [1,3]. Reducing the amount of trapped oil is economically very important and is a subject of ongoing research. The amount of trapped oil and the size of the trapped blobs depend on a variety of parameters including (but not limited to) transport properties of porous media and the physical and chemical properties of the displacing and displaced fluid [4–9].

When gravitational forces are negligible, the two-phase immiscible displacement at the pore level is controlled by the competition between capillary and viscous forces whose relative importance is quantified through two dimensionless numbers: the capillary number  $Ca$  and the viscosity ratio  $M$ .  $Ca$  is often defined as:

$$Ca = \frac{q\mu_1}{\sigma} \quad (1)$$

where  $q$  is the Darcy velocity,  $\mu_1$  the viscosity of the displacing fluid, and  $\sigma$  the interfacial tension between displacing and resident phases [10,11]. The Darcy velocity  $q$  is obtained by dividing the flow rate of the invading fluid ( $Q$ ) by the cross-sectional area of the porous medium ( $A$ ). The viscosity ratio  $M$  is defined as:

$$M = \frac{\mu_1}{\mu_2} \quad (2)$$

where  $\mu_2$  is the viscosity of the resident fluid. The displacement is considered to be favourable if  $M > 1$  and unfavourable if  $M < 1$ . Depending on the values of  $Ca$  and  $M$ , capillary fingering, viscous fingering, or stable displacement may be observed, influencing flow patterns and phase entrapment during immiscible two-phase flow in porous media [12–16].

The effect of  $M$  and  $Ca$  on the residual oil saturation at macro-scale has been extensively discussed in literature [12,17]. At small  $Ca$ , when viscous forces are negligible and capillary fingering prevails, the patterns described by the invading fluid during imbibition will follow the percolation pathways without any specific direction compared to the flow direction [13]. These patterns are described through the invasion percolation statistical approach [18]. On the other hand, viscous fingering is often modelled through diffusion-limited aggregation [19] and gives rise to tree-like fingers oriented in the direction of flow [13]. Viscous fingers are common features of unstable displacements in which water is more mobile than oil [20]. Since  $Ca$  has a significant impact on the amount of trapped fluid, often the residual saturation  $S_{ro}$  is experimentally measured as a function of  $Ca$  to obtain the so-called Capillary Desaturation Curve (CDC) [14], with  $S_{ro}(Ca) = (\text{volume of the residual oil at the given } Ca) / (\text{total pore volume})$ . The CDC is one of the most important input parameters in the reservoir simulation software for enhanced oil recovery [9,21].

Some of the most popular injecting fluids used in Enhanced Oil Recovery (EOR) and in soil remediation practices are non-Newtonian such as polymer solutions, foams or emulsions, and present shear-thinning behaviour, i.e. the viscosity of the fluid decreases as the applied shear stress increases. One of the main purposes of applying these complex fluids is to reduce mobility ratio [22]. This results in viscous fingering reduction and therefore improved sweep efficiency in the reservoir [23]. When a shear-thinning fluid is used as a displacing fluid, both  $Ca$  and  $M$  are functions of  $Q$  (note that  $\mu_1$  used in the definition of  $Ca$  and  $M$  stands for the apparent viscosity of the displacing fluid in the porous medium at a given flow rate). As a consequence, an evaluation of the effects of  $Ca$  on  $S_{ro}$  and trapped blob sizes assuming a constant  $M$  is not acceptable for most shear-thinning fluid displacements.

Several groups investigated the non-Newtonian fluid flow in porous media and its potential application for oil displacement [24–26]. For example, flooding experiments using shear-thinning polymer solutions were previously conducted [20,27] in order to analyse the effect of polymer concentration on front stabilisation

and recovery efficiency at a unique flow rate. Other authors [28] carried out computational fluid dynamics simulations using a digitalised pore network to investigate the non-Newtonian fluid displacement at the microscale and compared their results with the flooding experiments [20]. In previous work [2], a micromodel study was performed to investigate the effects of rheological properties of several complex fluids used in EOR on oil recovery.

In subsurface remediation, shear-thinning fluids have been used to create hydraulic stable zones [29] and to force chemical amendments into low permeability zones [30–33]. Although most remediation studies using shear-thinning fluids consist of laboratory experiments, a recent field implementation was reported [34]. Emplacement of amendments into low permeability zones is of particular interest because contaminants in such zones might sustain persistent plumes in adjacent transmissive zones due to diffusion-controlled release processes [35]. Injection of a shear-thinning fluid into a heterogeneous subsurface induces cross-flow between higher- and lower-permeability layers. Mobility reduction behind the polymer solution in a higher-permeability layer then creates a transverse pressure gradient that promotes fluid migration into less permeable layers [32]. In most remediation studies, the shear-thinning fluid contained the biopolymer xanthan [33,34].

Motivated by the widespread use of shear-thinning fluids in porous media and its great potentials in enhanced oil recovery and soil remediation, the specific objectives of the present study are to investigate how  $Ca$  and  $M$  affect  $S_{ro}$  and trapped blob distributions during immiscible two-phase flow in porous media involving shear-thinning fluids. To do so, a comprehensive series of polymer waterflooding displacement experiments were conducted using micromodels with well-defined characteristics to quantitatively investigate the effects of the polymer concentration  $C_p$  on oil entrapment patterns, visualised by means of a high resolution microscope at different flow rates. The findings of this paper extend our understanding of the physics governing two-phase flow in porous media using shear-thinning fluids.

## 2. Materials and methods

### 2.1. Micromodel

A series of experiments was conducted displacing resident silicone fluid by aqueous polymer solutions in a micromodel. The micromodel was fabricated in a silicon wafer using standard photolithography and inductively coupled plasma–deep reactive ion etching (ICP-DRIE) methods. Details of the fabrication process can be found elsewhere [36]. After the incorporation of nanopores serving as the inlet and outlet of the micromodel, the micromodel was chemically treated to be cleaned and to acquire uniform wettability. After the cleaning procedure, micromodels have a uniform and stable hydrophilic behaviour with contact angles  $< 16^\circ$  [37]. The pore-network compartment of the micromodel has a length of 1.4 cm, a width of 0.7 cm, and a thickness of  $29 \pm 1 \mu\text{m}$ . The flow network had approximately 3000 pore bodies and 9000 pore throats, resulting in a porosity  $\varepsilon$  of 0.6. The topology of flow network was based on truncated log-normal for the pore-body distribution and is considered to be a good approximation for pore size distribution in natural porous media [38]. The size of the pore throats was assigned by employing a concept previously proposed in the literature [7], where the size of a pore throat is a function of the dimensions of the connecting pore bodies. The width of the pore bodies varied from 80 to 160  $\mu\text{m}$ , while the width of the pore throats varied from 56 to 159  $\mu\text{m}$ . The pore bodies are cylinders and the pore throats are parallelepipeds. In planar view, pore bodies are circular while pore throats are rectangular, with a minor

deviation from this arrangement due to overlapping. The pore and throat size distribution of the micromodel together with the patterns of channels' distribution have been recently presented [9] thus it is not repeated here. The permeability of the micromodel  $k$ , determined by injecting water with different flow rates and measuring the pressure drop, was  $2.87 \times 10^{-12} \text{ m}^2$ .

## 2.2. Fluid properties

The used resident fluid was Xiameter<sup>®</sup> PMX – 200 Silicone Fluid (Dow Corning, UK) with a dynamic viscosity of  $1 \times 10^{-1} \text{ Pa s}$  (provided by Dow Corning), and an oil–water interfacial tension of  $31 \pm 1 \text{ mN/m}$ , measured by a digital tensiometer (Krüss, K11MK4). The displacing fluids were aqueous solutions with dissolved xanthan gum powder concentrations of 0, 500, 1000, and 2000 ppm. The solutions were prepared by dissolving xanthan in de-ionized and filtered water containing 400 ppm of  $\text{NaN}_3$  as a bactericide. Xanthan gum is a commonly used viscosifier [39,40] especially in manufacturing food grade products [41], and is obtained through fermentation of *Xanthomonas campestris* bacteria [39,41,42]. Additional information about its chemical composition, structure and other physico-chemical properties can be found elsewhere [43]. Its semi dilute xanthan solutions are known to develop a high viscosity level at low shear rates  $\dot{\gamma}$  before displaying a drastic decrease when the applied shear rate is increased, and are commonly classified as shear-thinning fluids. In the solution state, an isolated xanthan macromolecule is more or less rigid, its contour length is of typically  $1 \mu\text{m}$  [44], and its transverse size is approximately  $2 \text{ nm}$ . No plugging effect is expected in the case of micromodels, whose pores are typically larger than  $1 \mu\text{m}$ . Under high flow velocities the shear rate may be such that the xanthan molecules are oriented in the direction of the flow, resulting in a decrease in viscosity.

Addition of polymer did not significantly alter the interfacial tension within the range of concentrations  $C_p$  used in this study. The polymer solutions were characterized by means of a stress controlled rheometer (ARG2, TA Instruments) equipped with a cone-plate geometry, following a procedure previously presented in the literature [45,46]. Each shear rate corresponding to a specific shear stress was recorded when its variation was less than a prescribed tolerance (typically 3%) within a given time period. The obtained rheograms are displayed on Fig. 1(a) and the effective viscosities as a function of shear rate are shown in Fig. 1(b). The range of  $C_p$  and the measured rheograms in our experiments are similar to those presented by other authors [20], who used aqueous associative polymer solutions in their micromodel displacement experiments.

In the case of semi dilute aqueous xanthan polymer solutions, shear-thinning behaviour is often represented through the empirical Carreau model [47]. The Carreau equation is based on molecular network theory and is often presented as:

$$\frac{\mu - \mu_\infty}{\mu_0 - \mu_\infty} = \left[ 1 + (\lambda \dot{\gamma})^2 \right]^{\frac{n-1}{2}} \quad (3)$$

where  $\mu$  is the viscosity at a given shear rate  $\dot{\gamma}$ ,  $\mu_0$  and  $\mu_\infty$  are the zero shear rate and infinite shear rate viscosities, respectively,  $n$  is the power-law index, and  $\lambda$  is the time constant. The values of  $\mu_0$ ,  $\mu_\infty$ ,  $n$  and  $\lambda$  are determined by the polymer concentration under given pressure and temperature conditions. The Carreau model was fitted to the data shown in Fig. 1(b) by obtaining the values for  $\mu_0$ ,  $\mu_\infty$ ,  $n$ ,  $\lambda$ , and  $\delta$  that minimise the sum  $\sum_i [\bar{\tau}_i - \mu(\dot{\gamma}_i)]^2 \dot{\gamma}_i^\delta$  for each xanthan concentration [45]. In the expression for the sum,  $\mu(\dot{\gamma})$  is the Carreau viscosity according to Eq. (3) and  $\dot{\gamma}_i$  and  $\bar{\tau}_i$  are the steady state experimental shear stresses and the corresponding shear rates obtained by the rheometer, respectively. The

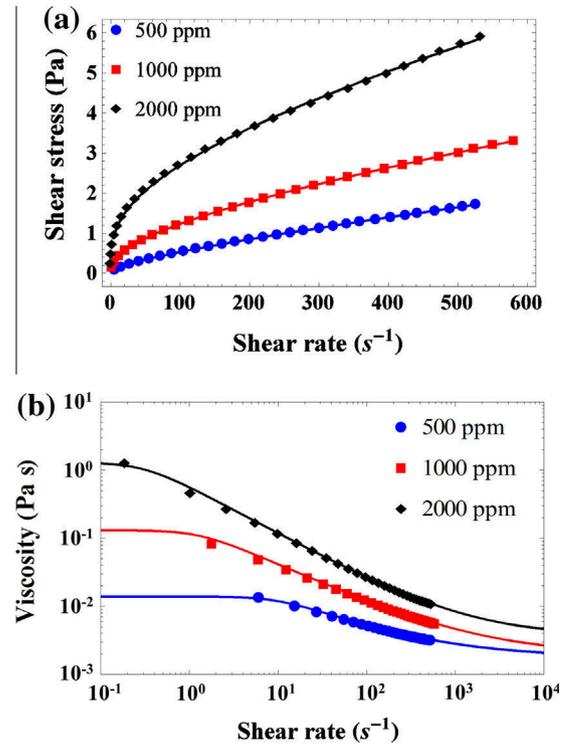


Fig. 1. (a) Rheograms and (b) effective viscosity vs. shear rate for the polymer concentrations of the injected fluid. The symbols represent experimental data and solid lines represent the fitted curves using the Carreau model (Eq. (3)).

corresponding values of Carreau parameters and  $\delta$  are presented in Table 1. The relations in Fig. 1(b) show that higher  $C_p$  values result in higher viscosities and that the measured data are well described by the Carreau model [47]. The data in Table 2 illustrate that the Newtonian viscosities of xanthan gum solutions increase with increasing  $C_p$ , while the onset of shear-thinning behaviour ( $1/\lambda$ ) decreases. Besides, the value of  $n$  decreases with increasing  $C_p$ , reflecting that the shear-thinning behaviour is more pronounced at higher  $C_p$ .

## 2.3. Displacement experiments

The experiments consisted of displacement of resident silicone fluid by four aqueous polymer solutions (0, 500, 1000, and 2000 ppm xanthan), at five flow rates. An overview of the displacement flow rates and associated Darcy velocities are presented in Table 2. The listed experiments were conducted for all four concentrations and were repeated five times. For each concentration, a total of 25 experiments (five repetitions for each of the five flow rates) were completed. The 25 experiments for a given concentration were considered to be an experimental set. The oil – water (0 ppm xanthan) fluid pair was considered to be a reference for comparison between waterflooding and polymer waterflooding using the 500, 1000, and 2000 ppm xanthan solutions. Single stage polymer waterflooding was used in this study. Other authors [2] showed that a single stage recovery with polymer waterflooding in micromodels can recover as much oil as the two-stage process where the polymer waterflooding is preceded by waterflooding.

For each experiment, the micromodel was initially fully saturated with oil at a flow rate of 100 ml/h. After that, the oil was displaced by injecting dyed (5 w/w%, Ecoline<sup>®</sup> 100, Royal Talens, The Netherlands) xanthan solution at a constant flow rate, using a syringe pump (PHD Ultra 3000, Harvard Apparatus), until steady state conditions were obtained.

**Table 1**

Carreau model [47] parameters and  $\delta$  values for the shear rate – viscosity relations shown in Fig. 2.

$C_p$ (ppm)	$\mu_0$ (Pa s)	$\mu_\infty$ (Pa s)	$\lambda$ (s)	$n$	$\delta$
500	$1.39 \times 10^{-2}$	$1.79 \times 10^{-3}$	$9.99 \times 10^{-2}$	$4.65 \times 10^{-2}$	$6.65 \times 10^{-12}$
1000	$1.31 \times 10^{-1}$	$1.98 \times 10^{-3}$	$7.55 \times 10^{-1}$	$4.16 \times 10^{-2}$	0.00728
2000	1.29	$3.72 \times 10^{-3}$	3.24	$3.05 \times 10^{-2}$	0

**Table 2**

Overview of flow rates and associated Darcy velocities for an experimental set, each conducted with 0, 500, 1000, and 2000 ppm dissolved xanthan gum injection solutions and repeated five times.

Experiment index $i$	Flow rate, $Q_i$ (ml/h)	Darcy velocity, $q_i$ (m/s)
1	$10^{-2}$	$1.368 \times 10^{-5}$
2	$10^{-1}$	$1.368 \times 10^{-4}$
3	$10^0$	$1.368 \times 10^{-3}$
4	$10^1$	$1.368 \times 10^{-2}$
5	$10^2$	$1.368 \times 10^{-1}$

Steady-state pressure drops  $\Delta P_i$  over the micromodel during monophasic flow of xanthan gum solutions were measured using a microfluidic pressure sensor (Elveflow, France) with a working range of 0–7 bars at  $q_1$ – $q_4$  for all values of  $C_p$  and at  $q_5$  for  $C_p = 0$  ppm and  $C_p = 500$  ppm. For the two larger concentrations at  $q_5$ , the pressure drops were larger than the sensor could measure. The obtained ( $q_i$ ,  $\Delta P_i$ ) data pairs for  $C_p = 0$  were used to calculate the network permeability ( $k$ ). The expression in Eq. (4), derived from the micromodel-specific Darcy equation, was used to compute the apparent viscosity ( $\mu_{app}$ ):

$$\mu_{app} = \frac{k \Delta P_i}{q_i L} \quad (4)$$

The effluent fluid was sampled during injection of 2000 ppm xanthan solution at the highest flow rate. The rheogram of this effluent fluid (results not shown) was very close to that of the injected polymer, demonstrating that mechanical degradation during transport through the pore-network was not significant. In addition, no considerable plugging due to the polymer macromolecules was observed during these experiments.

A cleaning procedure prior to each experiment set was completed to restore the original condition of the medium. This procedure consisted of five consecutive rinses in the following order: deionized water, isopropanol, deionized water, SC-1 and deionized water. SC-1 stands for the first step of a Standard Clean [48] and was carried out at  $\sim 80$  °C with a solution of 5 parts of deionized water, 1 part of aqueous  $NH_4OH$  (29 wt%  $NH_3$ ) and 1 part of aqueous  $H_2O_2$  (30 wt%). More than 100 pore volumes were injected at 100 ml/h during each rinse. After this cleaning step, the micromodel was dried by injecting pressurized air (1500 mbar) using a pressure generator (Elveflow, France). In addition, after each experiment, the micromodel was cleaned by completing three consecutive rinses with deionised water, isopropanol and deionised water, respectively, and then dried by injecting pressurized air.

#### 2.4. Imaging and analysis

The dynamics and patterns of the interface displacement as well as the size distribution of the trapped oil ganglia were visualised using an optical microscope (Leica M205C, 20.5:1 zoom, 0.952  $\mu m$  resolution, equipped with a Leica DFC 3000G high-resolution digital camera). Images were obtained before xanthan injection and after steady-state conditions were reached. Steady state was considered to have been reached once no significant fluid saturation changes were observed in the captured images. In these experiments, steady state was rapidly attained after xanthan breakthrough. In addition, complementary images were captured during displacement before breakthrough at flow rates  $Q_1$  and  $Q_3$

to investigate the patterns and morphology of the advancing front and the general dynamics of the displacement. The temporal resolution was 240 and 2 s for  $Q_1$  and  $Q_3$ , respectively.

To delineate the patterns and morphology of the trapped phase as well as the flow regime, the obtained grey-scale images were analyzed using ImageJ software. The procedure followed for image analysis is quite similar to what was used in previously published work [9] described briefly in the following. To minimise the wall effects on the reported analysis, a square window with the size of 3.92 mm  $\times$  3.92 mm in the centre of the micromodel was considered for the image analysis. Additional evaluation was performed by changing the position and size of this window to ensure that the results in terms of residual oil saturation and blob size are representative of the whole porous medium. As for the image analysis, the reference image, representing oil-saturated micromodel at the onset of each test, was subtracted from the steady-state image in order to obtain an image displaying only the polymer solution phase, referred to as a “p-image”. The p-image was then equalized to enhance its contrast, and two median filters (with the filtering radii of 2 and 3 pixels) were subsequently applied. After that, the filtered p-image was segmented using a variation of Yen Algorithm [49,50], giving the regions of the pore space filled with polymer solution at the steady state. The residual oil saturation ( $S_{ro}$ ) was then calculated as the percentage of the pore space which was not filled with polymer solution. Additionally, the filtered p-images were segmented using a variation of the IsoData algorithm [51] to obtain the size distribution of the trapped ganglia. Then, the oil phase distribution was deduced as being the complementary part of the pore space. A median filter with a filtering radius = 2 was also applied to the oil phase and the average ganglia size and the ganglia size distribution were computed from the resulting images.

### 3. Results and discussions

#### 3.1. Apparent and effective viscosity relations

Fig. 2(a) shows the measured pressure drop as a function of  $q$ . The pressure drops were then used to compute the apparent viscosity ( $\mu_{app}$ ) values with Eq. (4) and the results are shown in Fig. 2(b). The use of Eq. (4) is acceptable because no permeability reduction due to polymer retention was observed in our experiments. Indeed, xanthan gum macromolecules are flattened onto the surface so that the hydrodynamic thickness of the adsorbed layer is negligible [52]. Furthermore, the  $\mu_{app}$  values obtained for monophasic flow of xanthan were considered to have essentially the same value for the immiscible displacement due to the low values of  $S_{ro}$  obtained (see Section 3.4). The results in Fig. 2b clearly show the shear-thinning behaviour of the xanthan solutions as the apparent viscosity decreases with increasing  $q$ .

We compared the apparent viscosity  $\mu_{app}$  (Fig. 2b) with the effective viscosity  $\mu$  (measured using the rheometer (Fig. 1b) to assess the effect of fluid-solid interactions on the fluid viscosity. To do so, we define the apparent shear rate  $\dot{\gamma}_{app}$  in a porous medium as [52–54]:

$$\dot{\gamma}_{app} = \beta \frac{q}{\sqrt{kE}} \quad (5)$$

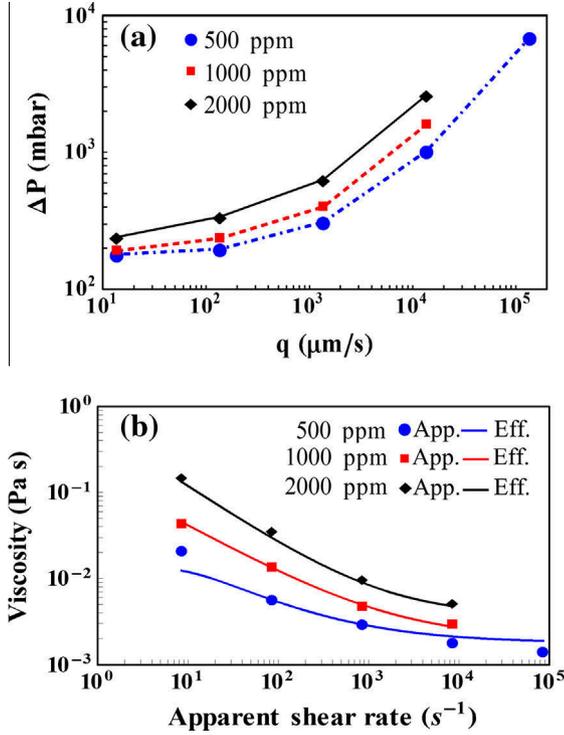


Fig. 2. (a) Pressure drop vs.  $q$ , (b) Apparent (symbols) and effective viscosity (solid lines) as a function of the shear rate for the 500, 1000, and 2000 ppm xanthan solutions.

where  $\beta$  is an empirical shift parameter which depends on the effective rheology and the pore structure. It has been reported that in spite of the diverse nature of the phenomena modifying rheology in porous media, the form of  $\mu(\dot{\gamma})$  obtained using a rheometer is quite similar to that of  $\mu_{\text{app}}(\frac{q}{\sqrt{k\epsilon}})$ , except from the shift parameter  $\beta$  in the case of some polymer solutions such as xanthan gum aqueous solutions [53]. Fig. 2(b) shows the computed  $\mu_{\text{app}}$  as a function of  $\dot{\gamma}_{\text{app}}$  (symbols) and the effective viscosity relation fitted to the rheometer data. Assuming  $\beta = 1$  a good correspondence between apparent and effective viscosities was obtained. In the case of  $C_p = 500$  ppm, the difference between apparent and effective viscosity are more visible. This may arise from the fact that the order of magnitude of viscosity is smaller for  $C_p = 500$  ppm (data are presented in logarithmic scale in Fig. 2) compared to the other concentrations, so eventual inaccuracies when approaching the limit of working range of the pressure sensor (0–7 bar) has a stronger impact on the apparent viscosity. This result means that the value of apparent viscosity at a given  $q$  in the used microfluidic device can be predicted from the effective viscosity as measured using the rheometer. Also, it shows that the effect of fluid-solid interactions (e.g. polymer mechanical degradation and apparent wall slip) on the relationship between viscosity and shear rate is negligible. Therefore, the same shear-thinning behaviour observed in the rheometer is reproduced during flow through the porous medium. Other researchers [30,31,33] found a good match between simulations and column and flow cell experiments by using  $\beta = 2.4$ . The good fit to experimental data provided by  $\beta = 1$  in the present case may be due to the lesser viscosity reduction in micromodels as the apparent slip effects are expected to be negligible.

### 3.2. Polymer concentration effects on flow patterns

The capillary numbers and viscosity ratios corresponding to each polymer concentration at different flow rates are shown in

Fig. 3. It should be noted that Ca and M values at the highest Darcy velocity ( $q_5$ ) were only calculated for  $C_p = 0$  ppm and  $C_p = 500$  ppm because the high pressure drops generated at the two highest concentrations were out of the measurable range of our pressure sensor. Also, it is worthwhile to mention that the relation between Ca and M is linear for a constant  $q$ , which follows directly from the Ca and M definitions.

Fig. 3 shows that the value of Ca increases for a constant  $q$  as  $C_p$  increases. For example, the Ca corresponding at  $q_1$  for  $C_p = 2000$  ppm ( $\text{Ca} = 6.31 \times 10^{-5}$ ) is two orders of magnitude larger than for  $C_p = 0$  ppm ( $\text{Ca} = 5.55 \times 10^{-7}$ ). When Ca increases (as a result of increasing  $C_p$ ), viscous forces dominate the interface displacement. Therefore, capillary fingering will be less significant as  $C_p$  increases. However, this dominance of viscous forces at high  $C_p$  does not necessarily entail generation of large blobs by viscous fingering. Indeed, the viscous pressure drop of the injected fluid through the porous medium is higher at high  $C_p$ , which increases the mobilisation and fragmentation of oil ganglia, thus preventing the formation of large blobs. Moreover, Fig. 3 shows that the resulting range of Ca is narrower at higher  $C_p$ .

Furthermore, according to Fig. 3, the value of M increases as  $C_p$  increases for a constant  $q$  (meaning  $\mu_{\text{app}}$  increases as  $C_p$  increases at a given value of  $q$  which is consistent with the results presented in Fig. 2(b)). In particular, this increase in M is more important at lower range of Ca as presented in Fig. 3. This is not a trivial conclusion, as it means that adding polymer to increase M is more effective at lower range of Ca or smaller  $q$ . In fact, the impact of  $C_p$  on M is relatively minor at high  $q$  as shown in Fig. 3. This is due to the orientation of xanthan macromolecules in the direction of flow, which leads to a reduced viscosity [53]. Therefore, the invasion front at high injection flow rates may not be stabilised by using polymer solutions. However, mobilisation and fragmentation of large ganglia may be still be enhanced by increasing  $C_p$  due to the higher viscous pressure drops of the invading fluid along the ganglia.

### 3.3. Interface displacement

The dynamics of the interface displacement as a function of  $C_p$  are shown in Fig. 4 for  $q_1$  and  $q_3$ . In this figure, fluid saturations at times  $t$ ,  $t + \Delta t$ ,  $t + 2\Delta t$  and  $t + 3\Delta t$  are presented, with  $\Delta t$  being 240 s for  $q_1$  and 2 s for  $q_3$ .  $t$  corresponds to the time at which the first image showing the invasion front is captured in each case, with the given temporal resolutions. Note that although the images are presented at the same flow rates, the corresponding capillary numbers are not the same (see Fig. 3). This Fig. shows that the invading front is stable at  $q_1$  for all values of  $C_p$ . Indeed, no capillary fingering is observed even at  $q_1$  and  $C_p = 0$  ppm, and Ca is low

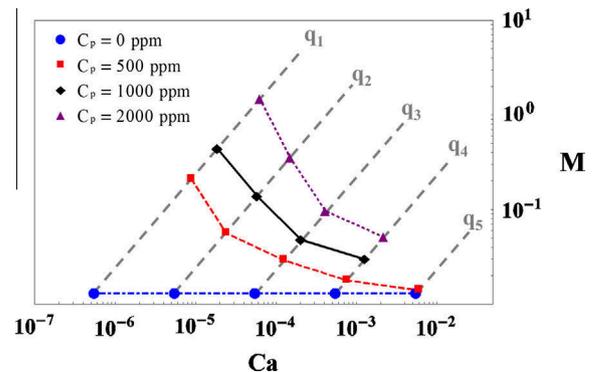
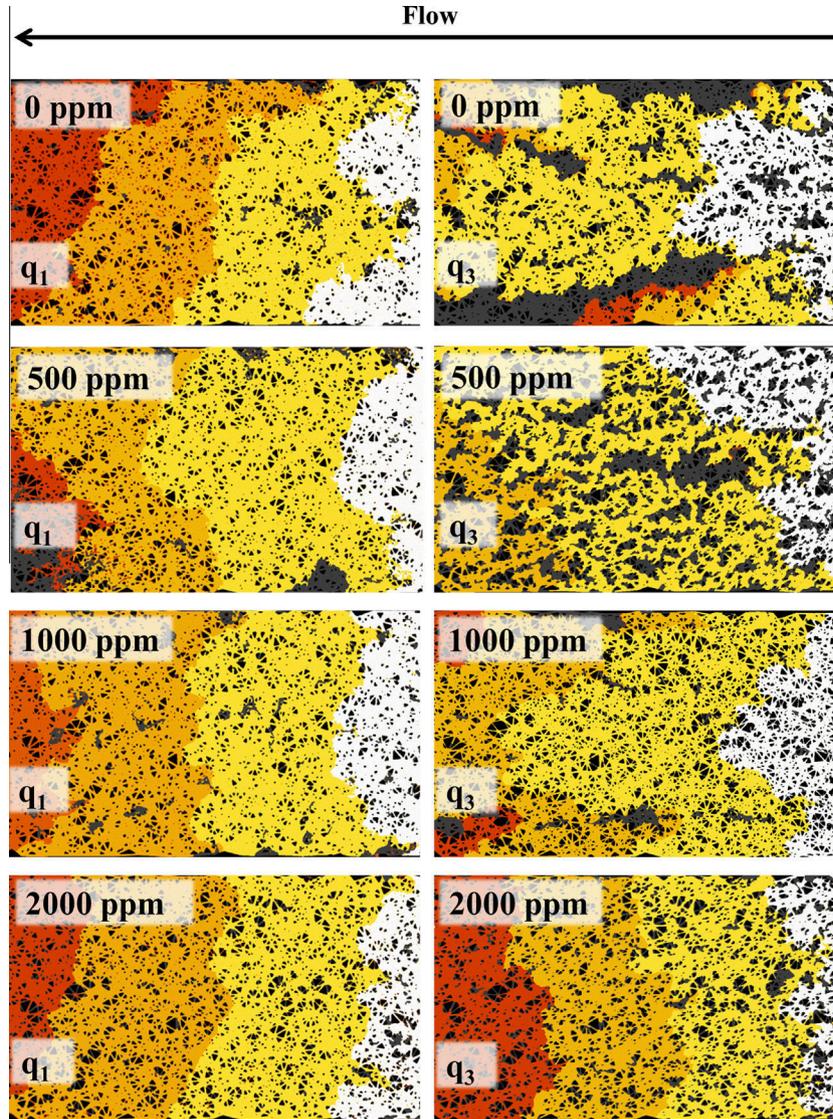


Fig. 3. Mobility ratio (M) as a function of the capillary number (Ca) for each  $C_p$  value.



**Fig. 4.** Temporal evolution of fluid saturation for  $q_1$  and  $q_3$ . The dark zones represent solid matter. White, light orange, dark orange and brown represent additional polymer solution saturations at times  $t$ ,  $t + \Delta t$ ,  $t + 2\Delta t$  and  $t + 3\Delta t$  respectively. Grey represents the regions of the pore space filled by oil at  $t + 3\Delta t$ .

enough so that viscous fingering is not important. Moreover, at the same low flow rate, the increase in Ca resulting from an increase in  $C_p$  is compensated by the simultaneous increase in M, ensuring the stability of the invading front. As a consequence, the number and size of ganglia trapped behind the front is small which leads to high oil recovery for all  $C_p$ . In contrast, viscous fingering leading to a large amount of bypassed oil is observed at  $q_3$  and  $C_p = 0$  ppm. At this higher flow rate, the increase of M with increasing  $C_p$  is more moderate than that for the displacement with  $q_1$  (Fig. 3). However, the corresponding increase in Ca is also more moderate, leading to the front being progressively stabilised as  $C_p$  increases (Fig. 4). Moreover, it is worthwhile to mention that more but shorter fingers are formed at  $C_p = 500$  ppm compared to waterflooding ( $C_p = 0$  ppm). It should be noted that although the values of Ca corresponding to the experiment with  $C_p = 0$  ppm at  $q_3$  and  $C_p = 2000$  ppm at  $q_1$  are similar (Fig. 3), the displacement patterns and the amount of trapped oil are significantly different.

### 3.4. Efficiency of polymer waterflooding

Fig. 5(a) displays the average area of the trapped ganglia, computed using the segmented images, as a function of Ca. Results

show that the average ganglia size at any Ca is effectively reduced by adding polymer to the injecting water. Indeed, the lowest average ganglia size was always obtained by the highest polymer concentration used in our experiments (2000 ppm). Also, it should be noted that within the  $q$  range imposed in our experiments, the variation in the ganglia size is lower at higher  $C_p$ . This may be, in part, a consequence of the narrower range of Ca covered for the same range of  $q$  at high  $C_p$  as mentioned in Section 3.2. Moreover, the maximum average ganglia size is lower at higher  $C_p$ . Fig. 5a shows that the largest blob sizes are obtained at intermediate values of Ca due to viscous fingering, dominating the propagation of the invading front, although M is unfavourable. It is also in this region that adding polymer to water is most effective in reducing the average ganglia size.

Residual oil saturations ( $S_{ro}$ ) were calculated from the segmented images and represented as a function of  $q$  in Fig. 5(b) showing that  $S_{ro}$  reduces in the case of polymer waterflooding compared to waterflooding for all  $q$  values. This is in good agreement with the work of other researchers [2], who presented the steady-state phase distribution during oil displacement by a shear-thinning fluid. Our results show that the recovery efficiency is improved at all polymer concentrations compared to

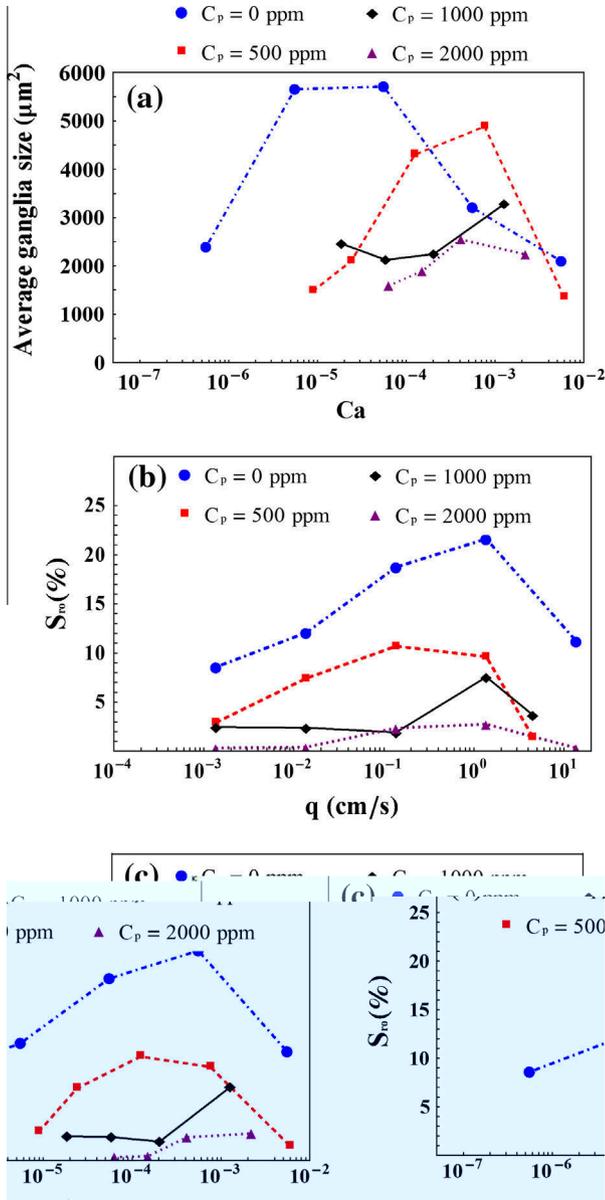


Fig. 5. (a) Average ganglia size as a function of Ca. (b)  $S_{ro}$  as a function of q, (c)  $S_{ro}$  as a function of Ca.

waterflooding and that the general trend of  $S_{ro}$  is to decrease as  $C_p$  increases. Indeed, the lowest  $S_{ro}$  values are obtained at the highest  $C_p$  for all q. One can relate the decrease of  $S_{ro}$  to the stabilisation of the invasion front induced by the higher viscosity ratios as  $C_p$  is increased. However, it should be noted that not only does M increase with  $C_p$  for a given flow rate, but also Ca (as shown in Fig. 3), which may in turn favour destabilisation of the front leading to higher  $S_{ro}$ . Therefore, in order to avoid misinterpretation of the results and to make an analogy with CDCs commonly used in the case of Newtonian fluids,  $S_{ro}$  is also represented as a function of Ca in Fig. 5c.

Fig. 5c shows that  $S_{ro}$  decreases with increasing  $C_p$  at every value of overlapping Ca values considered in our study. A possible interpretation is that the front-stabilising effect as a result of higher M (due to the higher polymer concentrations) overcomes the front-destabilising effect due to the increase in Ca, leading to less oil being trapped behind the front. Moreover, it should be noted that high viscosities of the concentrated polymer solutions generate high viscous pressure drops that are capable of mobilising

or fragmenting the large ganglia easier than diluted polymer solutions. In addition, Fig. 5(c) shows that the effect of Ca on  $S_{ro}$  is less pronounced at higher  $C_p$ . It should be noted that in the case of  $C_p = 1000$  ppm, average ganglia size increases at the lowest value of Ca, and  $S_{ro}$  slightly decreases at intermediate values of q, which is not the case for the other concentrations. This behaviour has been reported before [9,56,57], and requires further investigation. The results presented in Fig. 5 show that  $S_{ro}$ (Ca) curves (CDCs) are non-monotonic at every  $C_p$ , which is in agreement with recent findings [9,55].

The crossover between three regimes of fluid displacements, capillary-controlled displacement (capillary fingering), unstable viscous displacements (viscous fingering) and stable or compact viscous displacements, was investigated by several researchers [9,12–14] and results were typically presented in a M-Ca phase diagram. To map our results based on phase behaviour we present residual saturation of the experiments based on Ca and M in the three-dimensional plot shown in Fig. 6. One can observe that  $S_{ro}$  monotonically decreases with increasing M, attaining a plateau of very low  $S_{ro}$  above a critical value of roughly  $\text{Log } M > -1.5$ . Furthermore, once M is greater than this critical value and because Ca has limited influence on  $S_{ro}$ , a stable region with low  $S_{ro}$  values is observed. The reason is that in two-phase immiscible displacement with shear-thinning polymer solutions, the highest M are obtained at low values of Ca (see Fig. 3) when polymer molecules are not aligned in the direction of flow. This results in a “double stabilising effect” which impedes viscous fingering.

### 3.5. Ganglia size distribution and analysis

Ganglia size distributions were computed from the segmented images corresponding to the four values of  $C_p$  and three selected values of q ( $q_1, q_3, q_5$ ) as presented in Fig. 7. q was chosen instead of Ca because the values of Ca are different for each  $C_p$  whereas the values of q are identical, which facilitates comparison. Fig. 7 shows that in the case of  $C_p = 0$  ppm and  $C_p = 500$  ppm, the ganglia size increases from  $q_1$  to  $q_3$ , but decreases from  $q_3$  to  $q_5$ . This may stem from the fact that, at highly unfavourable viscosity ratios (low  $C_p$ ), viscous fingering becomes important at intermediate values of q leading to generation of larger ganglia. These large ganglia are fragmented or mobilised at high values of q, resulting in smaller trapped blobs. This confirms earlier numerical predictions [12,57]. In contrast for  $C_p = 1000$  ppm the range of ganglia sizes remain similar at  $q_1$  and  $q_3$  before decreasing at  $q_5$ . Ganglia sizes are roughly independent of q for  $C_p = 2000$  ppm, which may arise

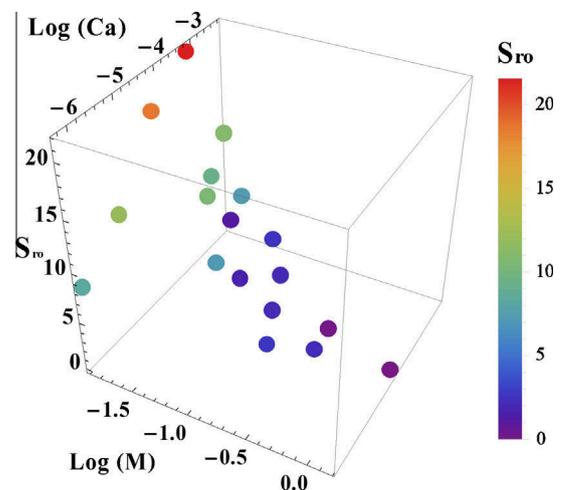


Fig. 6. Three-dimensional plot showing  $S_{ro}$ (%) as influenced by Ca and M.

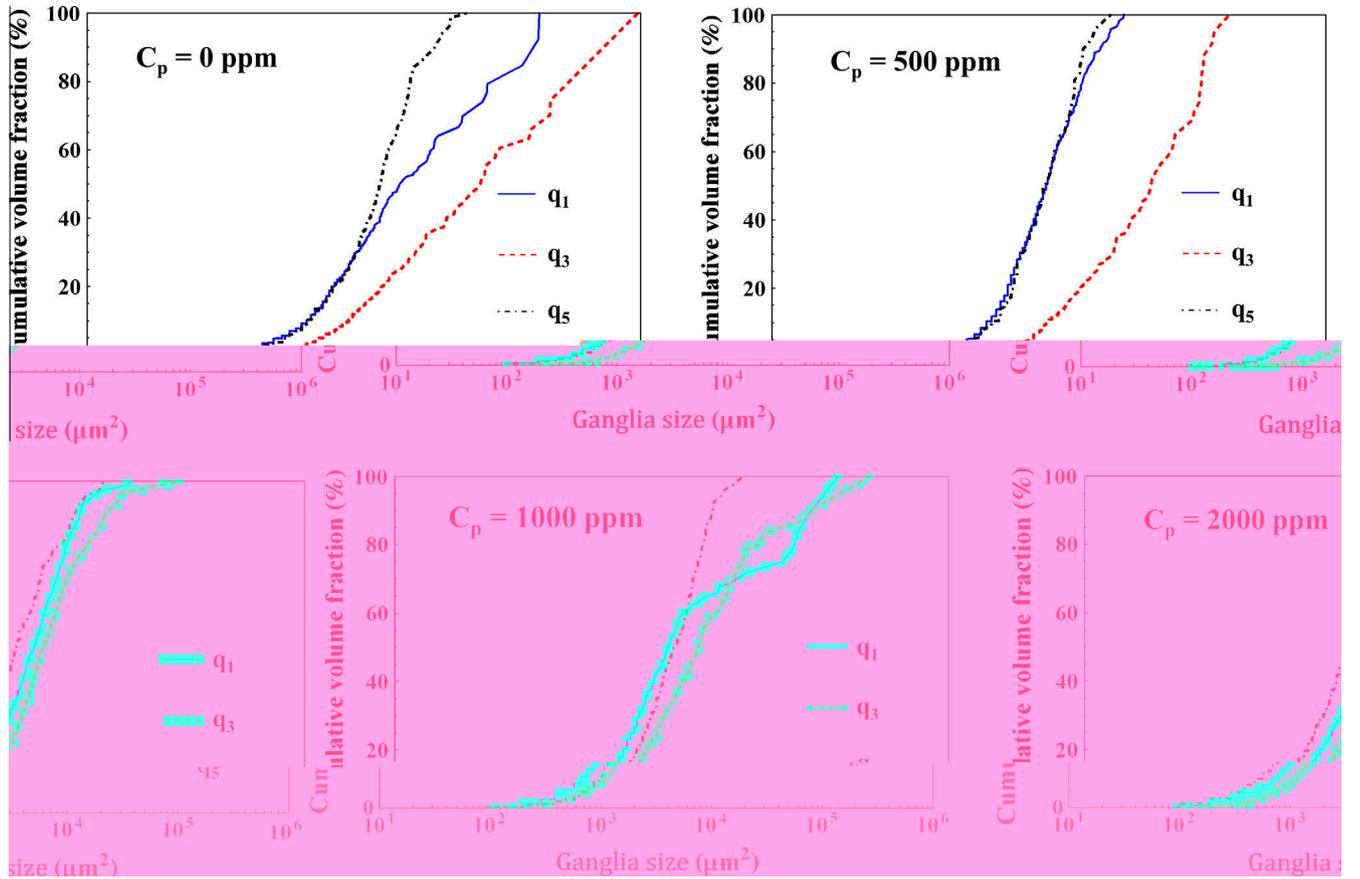


Fig. 7. Cumulative ganglia size distribution for all xanthan solutions injected with  $q_1$ ,  $q_3$ , and  $q_5$ .

from generation of more stable invading fronts as a consequence of the higher values of  $M$ . Closer inspection of Fig. 7 reveals that most ganglia sizes generated when viscous fingering is not important are comprised in the range  $\sim 10^2$  to  $10^4 \mu\text{m}^2$ , whereas the size distributions are wider when viscous fingering occurs. Also, it may be noted that the differences between size distributions at different  $q$  are less important as  $C_p$  increases.

According to the percolation theory, the size distribution of the trapped nonwetting phase in a porous medium after imbibition at infinitesimally low flow rates should scale as a power-law expressed as [8,58–60]:

$$N(s) \sim s^{-\tau} \quad (6)$$

where  $s$  is the number of the pores saturated by a trapped nonwetting ganglia,  $N$  is the number of ganglia whose size equals to  $s$  pores, and  $\tau$  is the power-law exponent. Values of  $\tau$  slightly  $< 2$  were obtained using numerical simulations in two-dimensional structures [59]. Using the images obtained in our experiments, we investigated the potential presence of such a power-law in our system in the case of the two lowest Darcy velocities ( $q_1$  and  $q_2$ ). The analysis was refined by only taking into account the ganglia sizes larger than 10 pixels, occurring more than once. It is noted that this scaling approach should be applied to the size of the ganglia in number of pores instead of their surface in pixels. However, given that the pore size distribution of our micromodel was relatively narrow and the depth of the channels was constant, both approaches are approximately equivalent. Other authors [8] followed a similar approach with three-dimensional images obtained by microtomography. We defined the normalized count as (number of ganglia with a given surface in pixels)/(number of smallest ganglia) and the normalized size as (surface)/(surface of the smallest ganglia).

The normalized count was represented as a function of the normalized size in all cases, and the corresponding power-law relations are shown in the electronic supporting materials section of this article, together with the best-fit  $\tau$  values.

The average of  $\tau$  values presented in Fig. 8 is 1.90, which is in agreement with the numerical predictions of 1.8–1.84 previously presented in the literature for two-dimensional networks based on the invasion percolation theory [59]. Also, in spite of the variations in  $Ca$  induced by the different  $C_p$  and  $q$  considered here, the obtained exponents are quite close as illustrated in Fig. 8. It must be mentioned that the exact value of  $\tau$  is influenced by how the curve fitting is performed and the range of ganglia sizes used for fitting the power law.

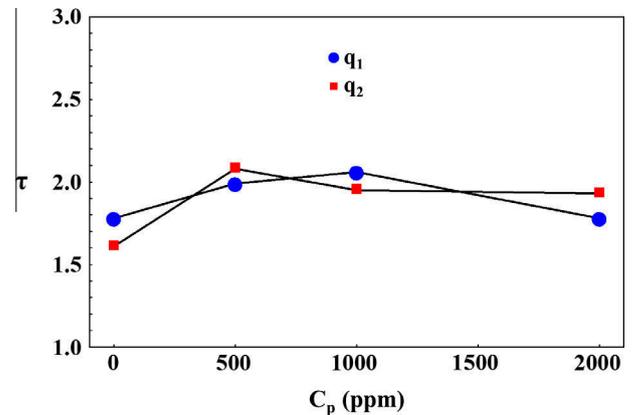


Fig. 8. Fitted power-law  $\tau$  values as a function of the polymer concentration  $C_p$  at the lowest Darcy velocities,  $q_1$  and  $q_2$  applied in our experiments.

#### 4. Summary and conclusions

Understanding the interfacial processes involved in multiphase flow of shear-thinning fluids in porous media at the pore scale is of vital importance in EOR, soil remediation, and other environmental and engineering applications. These fluids are characterized by the dependency of their apparent viscosity on the injection flow rate, leading to different values of  $M$  at different flow rates. For this reason, the Newtonian assumption used in the common approaches for the analysis of immiscible displacement in porous media and phase entrapment [9,12–14], e.g., stability diagrams, CDCs and ganglia size distributions as a function of  $Ca$ , do not apply when a shear-thinning fluid is used as the invading fluid. Moreover, flooding experiments with shear-thinning polymer solutions previously presented in the literature [20,27] have only analyzed the effect of polymer concentration on front stabilization and recovery efficiency at a single flow rate without evaluating the influence of  $Ca$ .

Previous works reported the need of studying the effects of polymer concentration on the oil recovery performance using laboratory experiments [61]. In particular, CDCs are essential inputs in typical reservoir simulation software for EOR [9,21]. In response to this need, we have now demonstrated that the polymer concentration  $C_p$  has a significant influence on the dynamics and patterns of interface displacement and phase distribution (even when the flowrate is kept constant) due to the effects of  $C_p$  on the effective viscosity of the polymer solution. In contrast to previous studies [2,20,24–28], the dependency of  $M$  and  $S_{ro}$  on  $Ca$  could be analyzed. Using a series of microfluidic experiments, we showed the capability of  $C_p$  to alter the value and range of  $Ca$  and  $M$ , which, in turn, determine the stability of the invasion front as well as the mobilisation and fragmentation of the resulting ganglia. We found that the effect of fluid-solid interactions on the relationship between viscosity and shear rate is negligible in the conducted microfluidic experiments, in agreement with the experiments by Chauveteau [52]. It was also shown that adding polymer, thus increasing  $Ca$  and  $M$ , is more effective at a lower flow rate.

In our experiments, polymer waterflooding proved to be more efficient to displace oil than waterflooding, confirming previous results [2], regardless of the value of  $C_p$ . Moreover,  $S_{ro}$  decreased with increasing  $C_p$  at all tested  $Ca$  values and the CDCs were found to be non-monotonic at every  $C_p$ , extending the results recently published for packs of glass beads and micromodels [9,55] to the case of polymer waterflooding. This suggests that it may be possible to attain similar oil recoveries both in polymer and regular waterfloods under injection flow rates which differ by several orders of magnitude. The highest  $M$  is obtained at low values of  $Ca$  when polymer molecules are not aligned in the direction of flow, resulting in a “double stabilizing effect” of the displacing interface which impedes viscous fingering. We found that the dependency of  $S_{ro}$  and the ganglia sizes on the flow rate is less pronounced at high values of  $C_p$ . In particular,  $S_{ro}$  was found to be independent of  $Ca$  above a critical value of  $M$ . Using a percolation theory approach, we obtained that the average power-law exponent in our experiments was in agreement with the numerical predictions previously presented for 2D networks [59]. Moreover, the values of the power-law exponents obtained at low flow rates were found to be close for all the values of  $C_p$  considered in our work.

This micromodel study enabled us to maximize our control over the boundary conditions and focus on the effects of  $C_p$  on  $Ca$ ,  $M$  and the residual oil saturation. This work indicates a starting point towards the development of quantitative tools for the analysis of oil recovery efficiency using shear-thinning fluid. The presented results should now be extended to more complex 3D geometries

in future work. Also, the obtained relationships can be implemented in reservoir simulation software for EOR in order to provide a more realistic alternative to the Newtonian assumption, which is expected to result in a better estimation of recovery efficiency at the pilot plant and reservoir scales. In particular, these results may provide useful guidance on the selection of the injection flow rate when using shear-thinning fluids in the mentioned applications.

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#### Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.jcis.2016.03.027>.

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