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L-Shell Photoionization of Magnesium-Like Ions with New Results for Cl^{5+}

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Abstract: Measurements of the absolute photoionization cross sections for the magnesium-like Cl^{5+} ion are reported, over the 190–370 eV photon energy range corresponding to the L-shell (2s and 2p subshells) excitation regime. The experiments were performed with the Multi-Analysis Ion Apparatus (MAIA) on the PLÉIADES beamline at the SOLEIL synchrotron radiation storage ring facility. Single and double ionization ion yields produced by photoionization of the 2p subshell of the Cl^{5+} ion from the $2p^63s^2\ ^1S_0$ ground state and the $2p^63s3p\ ^3P_{0,1,2}$ metastable levels were observed, as well as 2s excitations. Theoretical calculations of the photoionization cross sections using the Multi-Configuration Dirac-Fock and R-matrix approaches were carried out and the results are compared with the experimental data. The Cl^{5+} results are examined within the overall evolution of L-shell excitation for the early members of the Mg-like isoelectronic sequence (Mg, Al^+ , Si^{2+} , S^{4+} , Cl^{5+}). Characteristic photon energies for P^{3+} are estimated by interpolation.

Keywords: Photoionization; Atomic data; Inner-shell excitation; Chlorine ion

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1. Introduction

Photon driven excitation and ionization along the magnesium isoelectronic sequence have long been of interest for experimental and theoretical investigations [e.g. 1–18]. This is not surprising, given the nature of magnesium-like systems with their simple closed-subshell ground state configuration $2p^63s^2$. The 1S_0 ground state tends to make it a relatively stable ion configuration in many plasma environments and, on that basis, from a theoretical point of view, photoionization calculations should focus mainly on the effects of excited state configurations. However, this ideal picture largely fails in practice, as electron correlations, e.g. two-electron excitations, turn out to be extremely important in this system, leading to a significant departure from the simple one-electron excitation picture. Many early investigations concentrating on the first ionization threshold energy region highlighted the complexity of such electron interactions, along with consequent demands on appropriate theories, see e.g. [17] and references therein. As short wavelength photon interactions lead to inner-shell excitations, which couple with multiple-excitations of the valence electrons, photoionization calculations become

even more challenging, due to the increased number of unfilled (sub)shells. Reliable photoionization laboratory investigations of magnesium-like ions in the inner-shell excitation photon energy regime are therefore of continuing interest as they provide stringent benchmarking opportunities for different theoretical approaches.

Experimental and theoretical investigations of the photoionization of free atomic ions are becoming ever more important, stimulated as they are by the abundant data obtained from x-ray satellite observatories such as Chandra and XMM-Newton. Future space missions such as XRISM and Athena promise even greater sensitivity and higher spectral resolution. Optimising the value of astrophysical spectral observations, and the concomitant provision of greater physical insights, require improved theoretical modelling and simulation of astrophysical plasma environments. The latter rely on fundamental atomic data of the type provided by ongoing systematic and complementary experimental and theoretical investigations of the interaction of ionizing photons with free atomic ions. This is evidenced by the recent growth in laboratory astrophysics initiatives and associated data banks [19–24].

In the absence of experimental results, much of the atomic photoionization data exploited in modelling ionized environments has to rely on atomic physics calculations. Investigations of isoelectronic magnesium-like ions (twelve bound electrons) provide one important avenue for calibration of different theoretical approaches. Along the isoelectronic sequence from neutral magnesium through Al^+ , Si^{2+} , P^{3+} , S^{4+} and Cl^{5+} ions, the increasing core charge leads to significant changes in the relative effects of the nuclear charge versus electron-electron interactions on the photoionization properties. The sequence provides an ideal case study to examine the ability of theoretical models to predict and interpret these changes, which involve level crossing and plunging configurations [17].

Plasma-based light source experiments were successful in recording resonances and ionization thresholds for early members of the magnesium sequence for both ground and excited states, see, for example [1,5–7,25]. The biggest step, however, in the systematic investigation of the inner-shell photoionization of positive ions in general, has resulted from dedicated merged photon-ion beam facilities at synchrotron radiation storage rings, notably Daresbury (UK), SuperACO and later SOLEIL (France), ASTRID (Denmark), ALS (USA) and PETRA III (Germany), see e.g. [26–30] and references therein. The great advantage of such merged beam experiments is that they isolate specific ion stages and allow quantitative results to be obtained at high spectral resolution, often resulting in absolute cross sections for different ionization channels and thereby providing the highest quality fundamental data for atomic and plasma modelling and for benchmarking of the most advanced atomic theories.

Absolute cross sections for L -shell ($2s$ and $2p$) photoionization along the magnesium series have been previously obtained through synchrotron radiation based merged-beam experiments for Al^+ [9,31], Si^{2+} [10], S^{4+} [18] and Fe^{14+} [32], the latter being produced in an electron beam ion trap. These experiments have been complemented by various theoretical investigations which interpret the evolution of the observed resonances in the early part of the sequence and show that considerable changes in the relative intensities and positions of resonances take place as the core charge increases along the sequence. The L -shell single and double photoionization cross sections of magnesium itself have been studied extensively using synchrotron radiation in high resolution experiments, but only on a relative scale, see [16] and references therein.

The next member of the sequence is Cl^{5+} . Chlorine is an extremely reactive element, appearing in many gaseous, liquid and solid molecular forms of considerable scientific and industrial significance. Like all halogens it is strongly oxidizing, being one electron short of the neighbouring inert gas configuration. Chlorine ions play key roles in many terrestrial and astrophysical environments where understanding their interaction with radiation is important [33–38].

We report here the first study of L-shell photoionization of magnesium-like Cl^{5+} for photon energies between 190 and 370 eV, straddling the 2s and 2p inner-shell excitation regimes. It is interesting to compare the successes of the Multi-Configuration Dirac Fock (MCDF) and the R-matrix theoretical treatments for Cl^{5+} , to the success of the previous analogous treatments for S^{4+} [18]. Our results provide experimental absolute photoionization cross sections for Cl^{5+} , a comparison with the theoretical predictions of both MCDF and R-matrix approaches and an insight on the evolution along the isoelectronic sequence from Al^+ to Cl^{5+} . To our knowledge, no such photoionization data for P^{3+} is available in the open literature. From the observed trends along the sequence, we estimated the values of some relevant characteristic energies for P^{3+} .

2. Experimental Details

The experimental results for Cl^{5+} reported here were obtained at the dedicated merged photon-ion apparatus MAIA (Multi-Analysis Ion Apparatus) on the ultra-high resolution soft x-ray (10 eV to 1 keV photons) PLÉIADES beamline at SOLEIL. Well characterized synchrotron photon and ion beams overlap, and the resulting photoionization ions are selectively measured, providing cross section information for the different ionization channels. An advantage of working with ions over neutral species is that the number density in the overlap region can be determined, enabling absolute cross sections to be measured. A comprehensive description of MAIA, and how absolute photoionization cross section results may be determined, is provided in [26]. Here we provide a shorter description to include the specific experimental parameters used for the Cl^{5+} investigations.

HCl gas was introduced into an Electron Cyclotron Resonance (ECR) ion source in order to generate chlorine ions. Cl^{5+} ions were extracted and accelerated by an applied potential difference of -4kV and guided, by a 90° bending magnet, into the overlap region to meet the counter-propagating synchrotron radiation beam. An input power of 32 W at 12.36 GHz was used to optimize the production of Cl^{5+} ions. The magnetic filter enabled the selection of the most abundant $^{35}\text{Cl}^{5+}$ isotope. The ion current, measured in a Faraday cup placed after the magnet exit, was of the order of 10 μA . This beam was then focused and shaped to match the size of the counter propagating photon beam. The remaining current of ions interacting with the photons was typically of the order of 300 nA. The length of the interaction region was determined by a 57 cm long tube placed in the path of the two beams and polarized at a voltage of -2kV. Three transverse profilers, located respectively at the center and both ends of this pipe, allowed measurement of the overlap of the photon beam and the ion beam; a Form Factor [26] of 32000 m^{-1} was reached. The primary ion beam current was measured after the interaction region by means of a Faraday cup, while the photoionized ions, either singly ionized Cl^{6+} or doubly ionized Cl^{7+} , were separated from the primary Cl^{5+} beam by a second dipole magnet, selected in speed by an electrostatic analyzer, and measured with a microchannel-plate detector coupled to a counter. A photon chopper was used to subtract the contribution of ions produced by collisions in the residual gas (background pressure of 1.5×10^{-9} mbar) to the Cl^{6+} or Cl^{7+} signal. The photon beam flux was monitored by a calibrated photodiode and a typical current of $\sim 100\ \mu\text{A}$ at 195 eV photon energy and 150 meV bandwidth was measured. Knowing the photodiode current, the Cl^{5+} ion current, the form Factor characterizing the overlap of the two beam, the length of the interaction region, the ion speed, and the efficiencies of the photodiode and channel-plate detectors, and recording the Cl^{6+} and the Cl^{7+} signals as functions of the photon energy, allowed the determination of the single and double absolute photoionization cross sections of the Cl^{5+} ions. During the Cl^{5+} experiments, SOLEIL was operated with a current of 450 mA. Circular left polarization, the one delivering the highest flux in the photon range of interest, was used. The photon energy, corrected for the Doppler shift due to the ion velocity, was calibrated by the use of a gas cell containing argon, where the $2p_{3/2} \rightarrow 4s$ transition in argon at 244.39 eV [39] was measured. The energy uncertainties are of the order of 20 meV but vary depend-

ing on the resonance (see Tables). The total uncertainty of the measured cross sections is estimated to be not greater than 15% and is mostly due to the combined effects of the inaccuracy of the determination of the beam overlaps (the Form Factor), the detector efficiency and the photon flux.

The heating microwaves interact directly with electrons in the ion source through the ECR mechanism and a complicated range of processes involving energetic electrons are responsible for the production of the ions. The detailed electron energy distribution is not known and the ECR ion source plasma is not in equilibrium [40]. A well-recognised result is that in the merged beam technique the ions in the interaction region can often exist in excited states as well as the ground state [26-30]. The population of excited levels depends on their lifetimes and whether they survive the journey from the source into the interaction region. In general, this can be the case for metastable levels, some of which can have relatively long lifetimes. We will see below how the issue of excited states for the specific case of magnesium-like ions can be satisfactorily resolved.

3. Theoretical details

For the recent analogous investigations of photoionization of S^{4+} we used two quite disparate theoretical approaches, MCDF and R-matrix theory [18]. We use the same methods to predict and interpret the new Cl^{5+} results presented here. While long established and used for the calculation of many photoionization cross sections for a wide variety of ion species, both methods are being continuously reviewed and improved. In the MCDF approach the twelve electron magnesium-like ion is tackled directly and the quality of the results depends critically on including the most relevant electron configurations, this being the subject to calculational limitations. The R-matrix approach treats the magnesium-like challenge as a problem of an incident electron scattering off the eleven electron sodium-like ion. The quality of the final overall results of course therefore depends on the accuracy of the intermediate target description. In many cases some of the thresholds of the target system are already known and this information can be used to help in the R-matrix approach. This was indeed the case for S^{4+} [18] but not for Cl^{5+} . It is, therefore, interesting to see how the R-matrix code works for the latter when compared to the former. Because of the similarity of the computations for the Cl^{5+} system to those previously carried out for the S^{4+} ion, we here provide only brief descriptions for the R-matrix and MCDF calculations. Both length and velocity gauge calculations were carried out, using both approaches, and always show very satisfactory agreement. On that basis, for the sake of brevity, only the length gauge results are presented in this paper.

In order to focus on the problem at hand, viz. the L-shell photoionization of Cl^{5+} and its behaviour along the beginning of the magnesium sequence, we do not provide here lengthy mathematical descriptions to support the fundamental aspects of the theoretical descriptions. Only the most important details, i.e. those specific to the case of Cl^{5+} are provided. We invite the reader interested in the more fundamental and mathematical aspects of the MCDF and R-matrix theories to check the following recent references that will provide didactic descriptors, as well extensive lists of anterior references: [41,42] for MCDF and [43-45] for R-Matrix.

3.1. R-Matrix calculations

The calculational convenience of transitioning from Mg-like S^{4+} to Cl^{5+} is that the electronic orbital and configuration descriptions are the same once proper Z-scaling is accounted for. Previous R-matrix calculations for S^{4+} have been described in detail [18,45,46], and the change for the new calculations on Cl^{5+} simply amounts to adding one more proton to the nucleus, keeping the same number of electrons. Indeed, from simple Z-scaling of the radial coordinate $\rho = Zr$, the radial orbital $P(\rho) \rightarrow Z^{1/2}P(r)$, and the cross section $\sigma(Z) \sim \sigma(1)/Z^2$, the plots of the corresponding radial orbitals $P(r)$ (shown

in Figure 1) and resultant photoabsorption cross sections are both remarkably similar. The Z-scaling also leads naturally to a reduction in the electron correlation effect, manifested via the electron-electron repulsion $1/|\vec{r}_1 - \vec{r}_2|$ that scales as $1/Z$ and becomes less significant at higher Z , therefore Cl^{5+} is expected to show a more hydrogenic structure than S^{4+} . This behaviour is seen from Figure 1 where both sets of orbitals exhibit very similar patterns with a slightly greater localisation of the orbitals near the nuclear core for Cl^{5+} .

For the present Cl^{5+} work, the main series considered within the R-matrix formulation are the $2s^2 2p^6 3l$ channels of Cl^{6+} and the $2s^2 2p^5 3s 3l$ and $2s^2 2p^5 3s^2$ inner-shell channels. Note that again, as for S^{4+} , the $2s 2p^6 3s 3p$ channels are omitted to keep the computation tractable; this means that certain weak resonances will be absent that are seen in the MCDF results. Nevertheless, the main $2p \rightarrow nd$ Rydberg resonance series are well featured in the computed end results, and the weaker, interspersed $2p \rightarrow (n+1)s$ series and $2s \rightarrow np$ series at higher photon energy are also included.

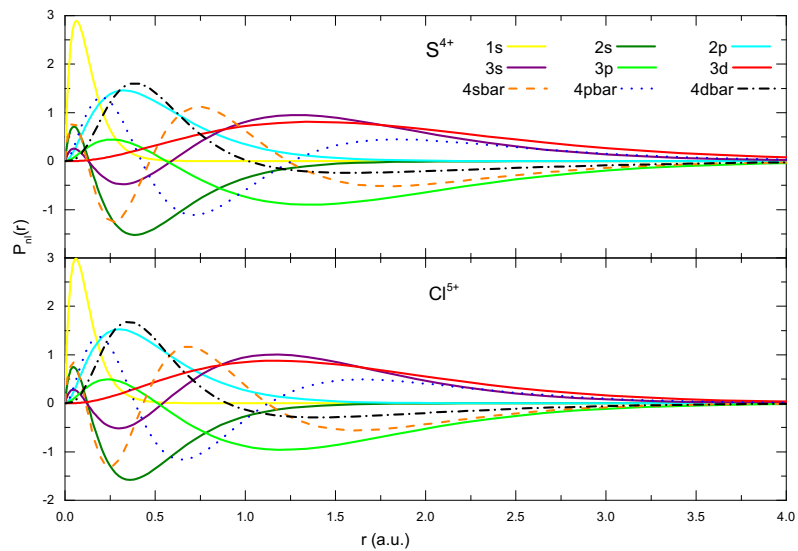


Figure 1. Plots of radial orbitals $P_{nl}(r)$ as a function of the radial coordinate r (in atomic units) used in the present R-matrix calculations. The same orbitals are plotted using the same colour code for both S^{4+} and Cl^{5+} .

As can never be overstated, the primary source of uncertainty in any R-matrix calculation, which is based on a variational principle, is due to a lack of convergence in the initial and/or final state energies, leading to a corresponding non-convergence of the photon transition energies. In order to simplify the comparison, we present *ab initio* results for Cl^{5+} , rather than use certain empirical energy information [48], knowing in advance that certain energy shifts are required to align with experimental results. Additionally, the R-matrix results are preconvolved with a resonance width of $\Gamma_{\text{spectator}} = 2.5 \times 10^{-3} \text{Ryd}$ for the spectator Auger decay process in order to ensure full resolution of the various infinite Rydberg series of otherwise narrowing resonances ($\Gamma_{\text{participator}} \sim 1/n^3$). $\Gamma_{\text{participator}}$ refers to the width of the participator Auger decay in which the initially photon-excited electron engages in the Auger process whereas it does not in the spectator Auger decay.

As a final note, the R-matrix method does include the Fano interference [49] between direct photoionization and indirect photoexcitation-autoionization, and thus asymmetric profiles can be revealed in general. This is in contrast to perturbative methods, such as the MCDF method, where the resonance is treated as a single final state, giving a Breit-Wigner (symmetric Lorentzian) resonance profile added incoherently to the (uncoupled) smooth background photoionization cross section.

Hence, the asymmetric profile of the experimental results of, most prominently, the $2s \rightarrow$ 243
np Rydberg series can only be reproduced by the R-matrix calculations here. 244

3.2. MCDF calculations 245

An updated version of the MCDF code developed by Bruneau [50] has been used to 247
compute the relevant photoexcitation and photoionization cross sections. Calculations 248
have been performed using a full intermediate coupling scheme in a jj basis set. 249
Calculations were restricted to electric dipole transitions using both the Coulomb and 250
the Babushkin gauges which correspond to the velocity and the length form of the 251
electric dipole operator in the non-relativistic limit, respectively [51]. Preliminary 252
calculations were performed to compute a set of one-electron wave functions resulting 253
from the energy minimization of the Slater transition state [52] using the following 254
configurations set: [Ne]3snl, [Ne]3s, and [F]3s², and [He]2s2p⁶3s², where $n = 3, \dots, 7$ and $l =$ 255
 s, p, d and where [He], [F], and [Ne] mean $1s^2$, $1s^2 2s^2 2p^5$, and $1s^2 2s^2 2p^6$, respectively. This 256
one-electron wave function set (OWFS) was used to calculate the $2s$ and $2p$ 257
photoexcitation cross sections from the 1S_0 level of the [Ne]3s² ground configuration and 258
from the $^3P_{0,1,2}$ metastable levels of the [Ne]3s3p configuration. Concerning the 259
photoexcitation cross sections from the ground level, the following photo-excited 260
configurations were retained: [F]3s²3d, [F]3s3p², [F]3s²n'l', and [He]2s2p⁶3s²nd, where n' 261
 $= 4, \dots, 7$ and l' = s, d. For the photoexcitation cross sections from the [Ne]3s3p $^3P_{0,1,2}$ 262
metastable levels, the photo-excited configurations retained were : [F]3s²3p, [F]3s3p3d, 263
[F]3s3pn'l', [He]2s2p⁶3s3p², and [He]2s2p⁶3s3pn'p. The initial OWFS has been also used 264
to compute autoionization rates for [F]3s²3d and [F]3s²3p/3s3p3d levels photoexcited 265
from the [Ne]3s² 1S_0 ground level and the [Ne]3s3p $^3P_{0,1,2}$ metastable levels, respectively. 266
The largest calculated autoionization rates were found for the [F]3s²3d 1P_1 and 3P_1 excited 267
levels, with corresponding Auger widths equal to 86 and 92 meV, respectively. The 268
Auger widths for the [F]3s²3p excited levels are all lower than 3.6 meV. The direct 2p 269
and 3s photoionization cross sections have been calculated also using the initial OWFS 270
for the [Ne]3s² 1S_0 and [Ne]3s3p $^3P_{0,1,2}$ initial levels. The 3p photoionization cross sections 271
were also computed for the [Ne]3s3p $^3P_{0,1,2}$ levels. 272

4. Results 273

4.1 L-shell photoionization of Cl⁵⁺ 274

We now present the results for single and double ionization of Cl⁵⁺ ions over the photon 275
energy range corresponding to L-shell excitations (both 2s and 2p). Figure 2 shows a 276
schematic energy level diagram indicating some of the main ionization pathways due to 277
photon absorption in the L-shell excitation regime. In particular it shows excitation from 278
the ground 2p⁶3s² 1S , and the metastable 2p⁶3s3p 3P levels which lie just over 12 eV 279
above the ground state (the vertical upward lines indicate photoabsorption). The final 280
inner-shell excited states shown lying above ~ 211 eV then give rise to Auger decay 281
resonances in the photoionization cross section, which can interact with the underlying 282
direct photoionization process and the downward dotted arrows illustrate the ensuing 283
production of either Cl⁶⁺ or Cl⁷⁺ ions due such non-radiative decay process(es) of the 284
original 2p vacancy. 285
286

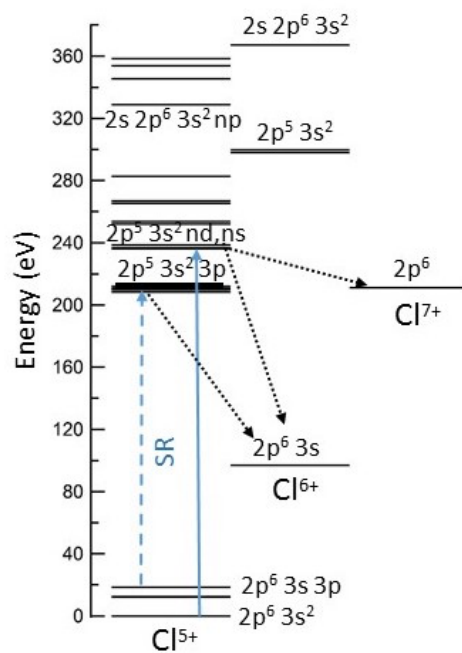


Figure 2. Schematic energy level diagram for Cl^{5+} showing excitation energies and ionization thresholds. The vertical solid and dashed lines indicate absorption pathways for synchrotron radiation (SR) photons, starting respectively from the ground level $3s^2 \ ^1S$ and the metastable $3s3p \ ^3P$ levels. The dotted lines show how the inner shell excitations lead to single ionization (Cl^{6+}) or double ionization (Cl^{7+}) channels.

Figure 3 shows the measured photoionization cross section over the photon energy region from 190 to 370 eV. The 285 - 320 eV photon region was not scanned as resonances were not expected in this interval. All cross sections between 190 and 285 eV were measured in the very dominant single ionization (SI) channel and all the cross sections above 326 eV were measured in the double ionization (DI) channel (which becomes the dominant channel above the $2p^{-1}$ ionization limit). We also show the results of the *ab initio* MCDF and R-matrix calculations where the theoretically predicted resonances are folded with the experimentally determined bandpasses for the different spectral regions. Because of the weakness of the resonances near 200 eV and those above 320 eV, their cross sections (both experimental and theoretical) are multiplied by a factor of ten which accounts for the apparent vertical displacements of the cross sections on the right hand side of figure 3.

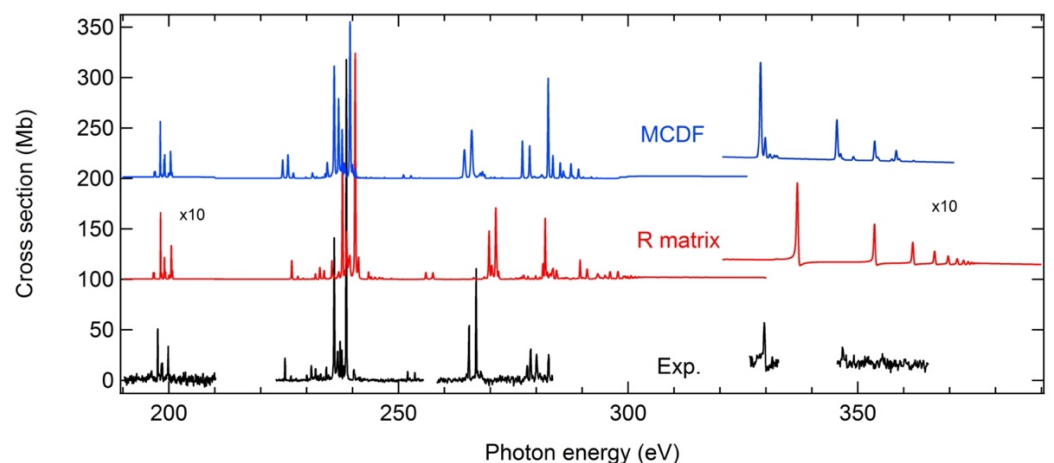


Figure 3. Photoionization cross section data measured (black trace) and calculated using the R-matrix and MCDF theories (red and blue traces, respectively) for Cl^{5+} for photon energies lying be-

tween 190 and 370 eV. The experimental data (labelled Exp.) is the single ionization below the photon energy of 300 eV and the double ionization above the photon energy of 300 eV. The region around 200 eV corresponds with 2p-excitations from the metastable $2p^63s3p\ ^3P$ levels. The resonances lying to higher photon energies arise predominantly from 2p (and 2s) excitations from the ground state $2p^63s^2\ ^1S_0$ level. The cross section values in both the 200 eV and above 320 eV regions are $\times 10$, in order to enhance visibility.

We first discuss how we estimate the contribution of metastable levels to the overall photoionization cross section. We then analyse the experimental cross section in comparison with the MCDF and R-matrix predictions, in separate contiguous energy regions corresponding to changing photon interaction processes and taking into account the contribution due to the metastable levels.

4.1.1. Metastable resonance region

The importance of the contribution of metastable levels to photoabsorption of plasmas containing magnesium-like ions was recognised in some early dual laser-produced plasma experiments [6], which showed that for Mg, Al⁺ and Si²⁺ the resonances arising from the $2p^63s3p\ ^3P$ levels appear in a separate photon energy region to the resonances arising from the ground state [5,7]. This feature allows an estimation of the metastable states population fractions by comparing the theoretically predicted cross sections from these states with the measured ones at those photon energies. Similar advantageous behaviour was observed for S⁴⁺ [18] and is again the case for the current Cl⁵⁺ results.

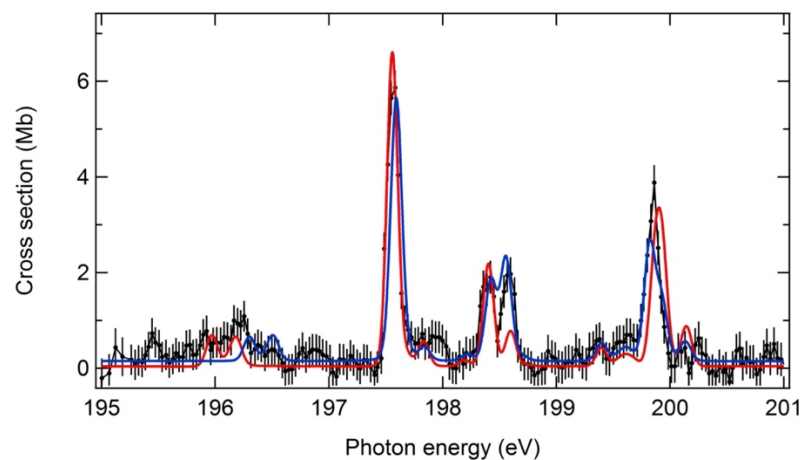


Figure 4. Experimental (single ionization) and scaled theoretical photoionization cross sections of Cl⁵⁺ in the 195 - 201 eV photon region. The observed resonance structure corresponds to 2p excitations from the metastable $2p^63s3p\ ^3P$ to $2p^53s^23p\ ^3S, ^3P, ^3D$ levels. The relative ground and $2p^63s3p\ ^3P$ metastable level populations are derived from fitting the theoretical MCDF (blue) and R-matrix (red) cross sections -shown here after convolution with a Gaussian profile of 110 meV FWHM and shifted by -0.54 eV meV and -0.64 meV, respectively, to the experimental data (black line with superimposed statistical error bars).

In Figure 3, the photoionization resonances arising from excitation from the 3P metastable levels ($2p^63s3p\ ^3P \rightarrow 2p^53s^23p\ ^3S, ^3P, ^3D$) can be seen in the 195-201 eV photon energy region, well separated from the ground state resonances lying above 220 eV photon energy. We can estimate the relative populations of the metastable levels by comparing the experimental data to the MCDF and R-matrix predicted cross sections. Figure 4 shows in detail the measured cross section due to the metastable levels and the comparative cross sections from both MCDF (blue line) and R-matrix (red line) calculations. The detailed comparison of the relative strengths of the individual resonances is determined by the relative populations of the individual $^3P_{0,1,2}$ J-levels and

the summation of the cross section over all the resonances depends on the relative metastable to ground state ratio. The best fit of the theoretical to experimental data implies relative populations of 77% 1S_0 + 4% 3P_0 + 1% 3P_1 + 18% 3P_2 . As was the case for S^{4+} , the very low contribution of the $2p^63s3p\ ^3P_1$ state is readily explained by its E1 radiative decay lifetime of $\sim 2.6\ \mu s$ [53] which contributes to significantly repopulating the ground state by the time the fast ($3.23 \times 10^5\ ms^{-1}$) Cl^{5+} sample ions reach the interaction zone. These relative population factors are used in all future figures where we compare the experimental data with the theoretical predictions.

It should be noted that in comparing the experimental data of Figure 4 to theory, the *ab initio* MCDF predictions were shifted by -0.54 eV and the *ab initio* R-matrix results were shifted by -0.64 eV. The integrated cross sections over the metastable resonances, taking into account the relative populations, were: Experimental ($2.9 \pm 0.4\ Mb.eV$), MCDF (2.36 Mb.eV), R-matrix (2.91 Mb.eV). In Table 1, we show experimental and theoretical (both R-matrix and MCDF) resonance energies, together with resonance line strengths (cross section integrated over a single resonance profile) and assignments, for the structures in the 195 eV to 200 eV photon energy region arising from inner-shell excitations of the valence-excited metastable 3P levels. The assignments are based on best intensity and energy position matchings of the observed resonances and the MCDF predictions.

Table 1. Experimental energies, theoretical energies, line strengths and assignments in *LSJ* notation (based on MCDF results) for Cl^{5+} resonances in the 195 eV - 200 eV photon energy range, arising from $2p \rightarrow 3s$ inner-shell excitations from the valence-excited metastable $2p^63s3p\ ^3P_{0,1,2}$ states.

Experimental *	Energy (eV) / Strength (Mb eV)			Assignment
	R Matrix	MCDF		
195.66(4) / 0.09(2)	196.61 / 0.083	196.84 / 0.064		$^3P_2\text{-}^3S_1$
195.95(3) / 0.15(3)	196.83 / 0.074	197.05 / 0.064		$^3P_0\text{-}^3S_1$
197.29(2) / 0.85(13)	198.20 / 0.864	198.13 / 0.700		$^3P_2\text{-}^3D_3$
197.54(4) / 0.09(2)	198.47 / 0.118	198.38 / 0.036		$^3P_1\text{-}^3D_2$
198.12(3) / 0.27(4)	199.04 / 0.268	198.97 / 0.211		$^3P_0\text{-}^3D_1$
198.31(4) / 0.28(5)	199.24 / 0.076	199.10 / 0.273		$^3P_2\text{-}^3P_2$
199.09(4) / 0.07(3)	200.04 / 0.054	199.94 / 0.048		$^3P_2\text{-}^3D_1$
199.33(4) / 0.09(2)	200.18 / 0.013	200.08 / 0.012		$^3P_1\text{-}^3D_1$
199.49(4) / 0.11(2)	200.25 / 0.028	200.15 / 0.024		$^3P_0\text{-}^3D_1$
199.59(2) / 0.47(8)	200.51 / 0.478	200.36 / 0.306		$^3P_2\text{-}^3D_2$
	200.57 / 0.252	200.47 / 0.156		$^3P_2\text{-}^3P_1$
199.97(5) / 0.05(2)	200.79 / 0.067	200.68 / 0.50		$^3P_0\text{-}^3P_1$

* The number in brackets is the experimental uncertainty on the last digit, i.e. 195.66(4) eV is the same as (195.66 ± 0.04) eV. The same convention is used for all the data presented in this column.

4.1.2. $2p \rightarrow 3d$ excitation region

The dominant resonance structures observed between 235 and 240 eV in Figure 3 are due to the expected $2p$ - $3d$ excitations, accompanied by considerably weaker $2p$ - ns resonances, and are shown in detail in Figure 5. The relative strengths of the individual resonances within this group vary considerably as one progresses from neutral magnesium towards Cl^{5+} , and the detailed spectroscopic assignments of the corresponding resonances for the early members of the sequence gave rise to considerable early discussions [1,2,5,16], with the labelling to some extent depending on the particular theoretical approach. This is not surprising as, previously noted in section 2.1, considerable challenge arises in the theoretical calculations due to the complexity associated with multiply excited outer electron configurations combining with the

innershell excited 2p (or 2s) hole. Further complexity arises from the nominally closed shell ground state of $3s^2 \ ^1S_0$ mixing with configurations such as $3p^2$ [5,9,10]. The theoretical calculations indicate that some of the weaker resonances within Figure 5 are attributable to such electron correlation effects between energetically close-lying multiply excited states.

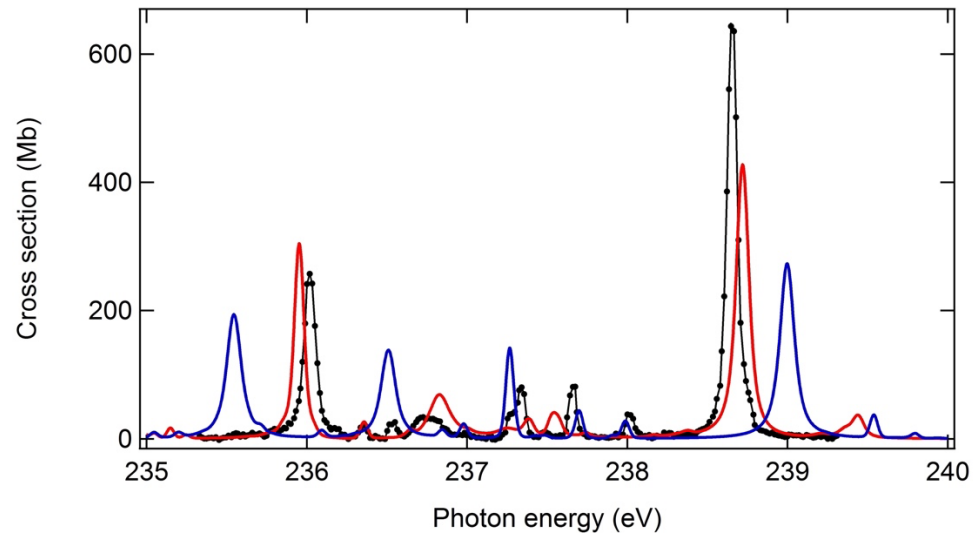


Figure 5. Photoionization cross sections for Cl^{5+} in the photon energy region corresponding to $2p \rightarrow 3d$ excitations: experimental data (single ionization, black trace) and MCDF (blue) and R-matrix (red) theoretical predictions, respectively. The theoretical predictions are folded with the experimental bandpass (Gaussian profile of 50 meV FWHM) and weighted according to semi-empirically determined population percentages (see text). The MCDF and R-matrix theoretical predictions are shifted by -0.46 eV and -1.86 eV, respectively.

It is seen from Figure 5 that the R-matrix results mimic the experimental data in this region somewhat better than the corresponding MCDF predictions, but by a small amount. Both theoretical approaches require systematic energy shifts in order to bring the strongest resonances into approximate agreement with experiment (MCDF and R-matrix shifts of -0.46 eV and -1.86 eV respectively). When compared to the experimental data, the R-matrix relative strengths of the main resonances are somewhat underestimated, while the energy separation of the strongest resonances is slightly overestimated (by typically an amount of less than 0.5 eV) in the MCDF calculations. For the latter approach, the use of an even more extended set of ground state and photoexcited configurations would likely improve the value of this energy separation, via both improved OWFS and description of ground and excited states correlations. This relatively minor improvement would require significant additional computational efforts which were not available to the authors. The cross sections integrated over the photon energies of the spectral region of Figure 5 are: Experiment ($129 \pm 19 \text{ Mb.eV}$), MCDF (111.2 Mb.eV) and R-matrix (118.9 Mb.eV), respectively.

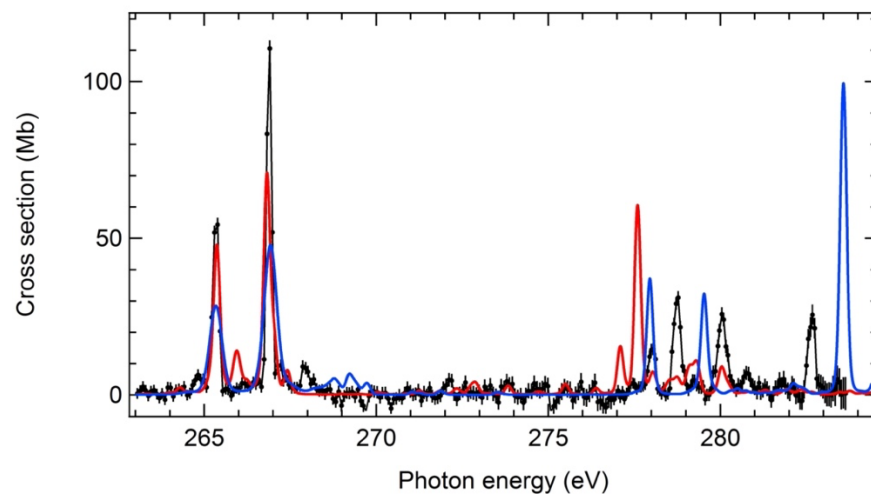


Figure 6. Photoionization cross sections for Cl^{5+} in the photon energy region corresponding to $2p \rightarrow nd$ excitations: experimental data (single ionization, black trace) and MCDF (blue) and R-matrix (red) theoretical predictions, respectively. The theoretical predictions are folded with the experimental bandpass (Gaussian profile of 190 meV FWHM) and weighted according to semi-empirically determined population percentages (see text). The MCDF and R-matrix theoretical predictions are shifted by +0.97 eV and -4.36 eV, respectively.

4.1.3. Region of $2p \rightarrow nd$ excitations

Figure 6 shows the corresponding comparisons for the experimental and *ab initio* theoretical predictions for the resonances in the $2p \rightarrow nd$ ($n > 3$) photon energy region. The systematic energy shifts required to bring the theoretical predictions into approximate agreement with the experimental data are +0.97 eV for the MCDF and a larger shift of -4.36 eV for the R-matrix calculations. The integrated cross sections over the spectral region covered by Figure 6 are in good agreement and are respectively: Experiment (87 ± 13 Mb.eV), MCDF (71.8 Mb.eV) and R-matrix (85.4 Mb.eV). Both the R-matrix and MCDF results suggest that the strong resonance feature observed at 282.66 eV, likely corresponds to the first member ($n = 3$) of the $2s \rightarrow np$ 1P_1 series. Numerical fitting of the Rydberg series for the $2p \rightarrow nd$ series using the basic $E_n = I_p - \frac{13.6 \times 6^2}{(n-\delta)^2}$ hydrogenic quantum defect formula (in eV) leads to values of 299.6(2) eV and 0.22(1) for the $(2s^2 2p^5 3s^2)$ 2P ionisation limit I_p and quantum defect δ , respectively. In the experimental conditions, it was not possible to reliably access the energy values of the two fine-structure limits $^2P_{1/2,3/2}$. The comment made in 3.1.2 about the use of more extended OFWS and configuration sets is also applicable here.

4.1.4. Region of $2s \rightarrow np$ excitations

Above the $2p^5 3s^2$ 2P limit, we observed a regular series of relatively weak resonances analogous in shape to those previously observed for S^{4+} [54]. As experimental absolute cross sections were not available here, the data was instead normalised to the theoretical cross sections, as shown in Figure 7. The strongest resonance lies at ~ 330 eV and can be identified as the $2s \rightarrow 4p$ member of the series. The most striking feature of the resonances in this region are the strongly asymmetric Fano profiles due to the strong autoionisation interaction with the underlying continua. As noted in section 2.1, the R-matrix calculation includes the Fano interference between the resonance and the underlying continua and mimics rather well the observed asymmetric profiles. Hydrogenic extrapolation (see previous paragraph) of the experimental $2s \rightarrow np$ series leads to best fit values of 373.2(6) eV and 0.70(1) for the $2s$ $^2S_{1/2}$ ionization threshold energy and quantum defect of the $2snp$ 1P_1 levels, respectively.

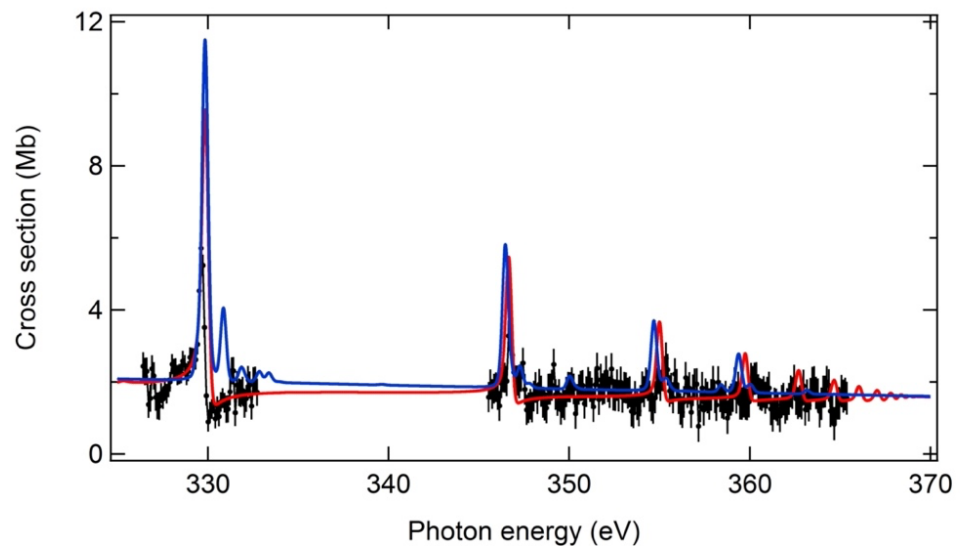


Figure 7. Photoionization cross sections for Cl^{5+} in the photon energy region corresponding to excitations from the $2s$ inner-shell: MCDF (blue) and R-matrix (red) theoretical predictions, experimental data (double ionization, black trace) normalized to the theoretical curves. The theoretical predictions are folded with the experimental bandpass (Gaussian profile of 340 meV FWHM) and weighted according to semi-empirically determined population percentages (see text). The MCDF and R-matrix theoretical predictions are shifted by +1.0 eV and -7.0 eV, respectively.

In Table 2, we gather together the experimental measurements and the corresponding theoretical predictions for all resonances observed between 225 and 370 eV, most of which have been shown in detail in Figures 5, 6 and 7. Table 2 shows that the vast majority of the observed resonances are reasonably accounted for by both theories, in terms of resonance energy, strength and width. In addition, the supernumerary low-intensity peaks seen in Figure 5 are readily interpreted as transitions from the $2p^6 3s 3p^3 P_{0,2}$ metastable states to $^3S, ^3D$ states of the multiply-excited $2p^5 3s 3p 3d$ configuration which is consistent with our interpretation of the 195 eV - 201 eV low-energy photon region (see section 3.1.1.).

Table 2. Experimental and theoretical (MCDF and R-matrix) energies, as-measured line strengths and, where available, Auger widths for the Cl^{5+} resonances due to $2p \rightarrow nd$ and $2s \rightarrow np$ inner-shell excitations from the $2p^6 3s^2 \ ^1S_0$ ground state. Where identifiable from the output of the MCDF theory, the dominant electron configuration and leading LSJ character of the final state of the resonance is given in the outermost right column.

Energy (eV)/Strength (Mb eV)/Auger width (meV) * Experimental **	Energy (eV)/Strength (Mb eV)/Auger width (meV) * R-matrix	Energy (eV)/Strength (Mb eV)/Auger width (meV) * MCDF	Assignment (MCDF)
225.28(3) / 4.0(7) / x	226.77 / 3.94 / x	224.78 / 5.06 / x	$2p^5 3s 3p^2 \ ^3D_1$
226.56(7) / 0.7(4) / x	228.08 / 0.63 / x	225.93 / 6.57 / x	$2p^5 3s 3p^2 \ ^3P_1$
230.03(7) / 0.9(4) / x	231.91 / 1.07 / x		
231.01(3) / 2.9(6) / x	232.88 / 2.75 / x	231.25 / 1.32 / x	$2p^5 3s 3p^2 \ ^3P_1$
231.93(4) / 2.2(5) / x	233.80 / 2.12 / x		
232.49(7) / 0.8(4) / x			
233.05(5) / 1.2(4) / x	235.18 / 0.19 / x		
233.64(10) / 0.5(4) / x			
234.26(4) / 2.4(5) / x		234.48 / 2.83 / x	$2p^5 3s 3p 3d \ ^3D_3$

234.73(6) / 1.0(4) / x			
235.98(2) / 26(4) / 51(4)	237.81 / 29 / 37	236.01 / 39.8 / 45	$2p^5 3s^2 3d \ ^3D_1$
236.35(3) / 1.1(4) / x			
236.54(3) / 1.5(4) / x			
236.71(3) / 9(2) / 158(65)	238.69 / 20.3 / 134	236.97 / 28 / 92	$2p^5 3s^2 3d \ ^3P_1$
237.27(3) / 2.2(3) / x			
237.34(3) / 4.7(8) / x		237.73 / 5.5 / x	$2p^5 3s 3p 3d \ ^3D_2^{***}$
237.49(4) / 0.5(4) / x			
237.66(3) / 4.8(8) / x		238.16 / 2.7 / x	$2p^5 3s 3p 3d \ ^3D_3^{***}$
238.01(3) / 2.3(5) / x		238.45 / 1.72 / x	$2p^5 3s 3p 3d \ ^3D_1^{***}$
238.61(2) / 78(12) / 46(2)	240.58 / 58.1 / 69	239.46 / 42.6 / 86	$2p^5 3s^2 3d \ ^3P_1$
240.26(4) / 2.0(5) / x		240 / 2.24 / x	$2p^5 3s 3p 3d \ ^3S_1^{***}$
240.47(7) / 9(4) / x			
251.98(2) / 1.5(2) / x	255.97 / 1.9 / 87	251.10 / 1.0 / x	$2p^5 3s^2 3d \ ^1P_1$
253.55(2) / 1.4(2) / x	257.51 / 1.8 / 87	252.71 / 0.8 / x	$2p^5 3s^2 4s \ ^3P_1$
265.33(3) / 13(2) / x	269.73 / 12.2 / 59	264.36 / 14.0 / x	$2p^5 3s^2 4d \ ^3D_1$
266.88(3) / 21(3) / x	271.18 / 17.9 / 53	265.96 / 21.8 / x	$2p^5 3s^2 4d \ ^3P_1$
278.01(3) / 4.1(7) / x			
278.75 / 8.5(1.3) / x		276.98 / 9.09 / x	$2p^5 3s^2 5d \ ^3P_1$
280.05(3) / 8.4(1.3) / x		278.56 / 7.57 / x	$2p^5 3s^2 5d \ ^3P_1$
282.66(3) / 6.5(1.0) / x		282.60 / 21.9 / x	$2s 2p^6 3s^2 3p \ ^1P_1$
329.6(1) / x / x	336.88 / x / x	328.85 / 4.27 / x	$2s 2p^6 3s^2 4p \ ^1P_1$
346.7(1) / x / x	353.38 / x / x	345.47 / 1.77 / x	$2s 2p^6 3s^2 5p \ ^1P_1$
355.3(1) / x / x	362.03 / x / x	353.69 / 0.88 / x	$2s 2p^6 3s^2 6p \ ^1P_1$
360.4(1) / x / x	366.67 / x / x	358.38 / 0.49 / x	$2s 2p^6 3s^2 7p \ ^1P_1$

* The symbol x indicates partial absence of data for that entry. No entry at all means that there are no data available.

** The number in brackets is the experimental uncertainty on the last digit of the data, i.e. 235.98(2)/26(4)/51(4) is the same as $(235.98 \pm 0.02) \text{ eV} / (26 \pm 4) \text{ MbeV} / (51 \pm 4) \text{ meV}$. The same notation convention is used for all the data presented in this column.

*** These resonances are due to $2p \rightarrow 3d$ excitations from the initial $2p^6 3s 3p \ ^3P_{0,2}$ metastable states.

4.2 Evolution along the Mg-like sequence

Studies of isoelectronic sequences of atomic energy levels [55] and absorption oscillator strengths (f -values) [56], line strengths or cross sections are of fundamental interest. New atomic data can be inferred from isoelectronic sequences via the interpolation/extrapolation to neighbouring atoms and ions of sets of f -values/energies exhibiting smooth and systematic variations. Further, it is the trend along an isoelectronic sequence that is also of great general interest, as a smooth trend can be modeled using Z -dependent perturbation theory. Irregular, non-monotonic, trends are also known to occur and are commonly related to the crossing of levels of correlation-mixed states from interacting electronic configurations or spin-orbit mixed states [57]. The magnesium spectrum is a case in point in this case for correlation mixing, due to the strongly perturbing effects of the $3p^2$ configuration on the $3s3d$ configuration and over the entire $3d$ ns series indeed. As pointed out in the introduction section, these effects are found to persist in the presence of a $2p$ vacancy. Therefore, it is interesting to view the Cl^{5+} results within the overall context of the magnesium isoelectronic sequence.

Figure 8 provides a full view of both the single and double experimental photoionization cross sections, measured in synchrotron radiation based merged-beam experiments, including Al^+ [9] (ASTRID), Si^{2+} [10] (SuperACO), S^{4+} [18] (SOLEIL) and Cl^{5+}

(SOLEIL, this work). Although it is not possible to make detailed and/or quantitative intercomparisons between the four traces of Figure 8 due to their very different photon energy ranges with associated different spectral dispersions (determined by the beamline instrumentation) as well as the choice of experimental monochromator bandpass(es), the following qualitative remarks can be made. As expected, the resonance structures shift markedly to higher energies as the nuclear charge increases. The corresponding trends will be explored in greater detail for selected transitions below. Progressing along the series, the progressive discretization of the SI resonance structure (i.e. mostly the $2p^5 3s^2 nd$ resonances) into a seemingly hydrogenic Rydberg series for Cl^{5+} , as well as the concomitant redistribution of the line strengths into the first $2p^5 3s^2 3d$ series member, are apparent.

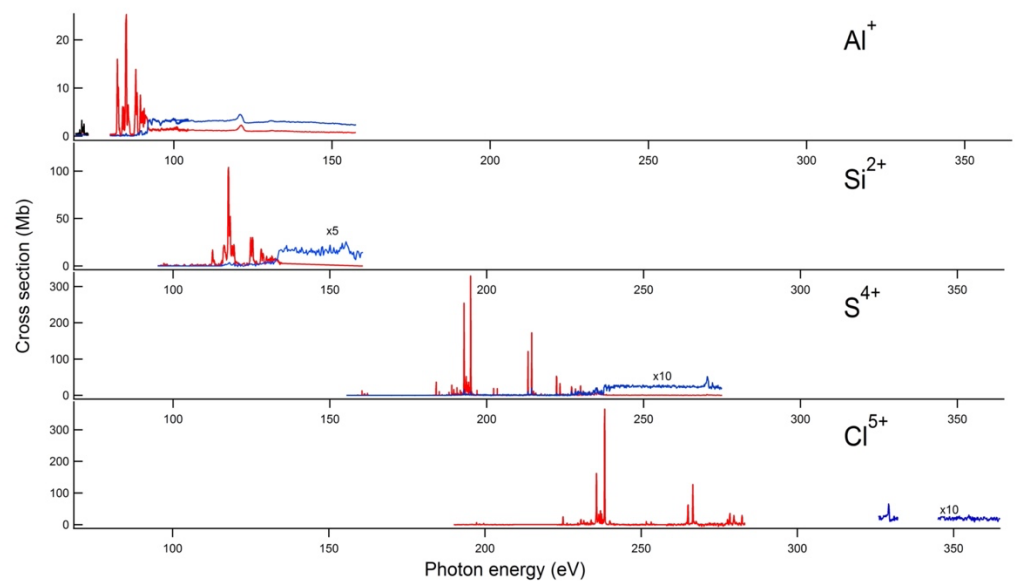


Figure 8. Single (red) and double (blue) photoionization cross sections for the magnesium-like ions Al^+ [9], Si^{2+} [10], S^{4+} [18] and Cl^{5+} [this work] in the photon energy region corresponding to L -shell excitations.

In order to better visualise and characterize the main features of the isoelectronic evolution, we show in Figure 9 the total cross sections for the ions Al^+ to Cl^{5+} but displayed on modified photon energy scales so that the resulting spectra line up for better inter-comparison. To accomplish this, the energy scales are multiplied by appropriate numerical factors and suitably shifted so that the main $2p \rightarrow 3d$ and $2p \rightarrow 4d$ resonance structures line up (i.e. the same $2p \rightarrow 3d$, $2p \rightarrow 4d$ energy difference is maintained for the four ions) below each other. It is clear from Figure 9 that for S^{4+} and Cl^{5+} the overall resonance structures are very similar and confirm that by S^{4+} the increased core charge has become the dominating factor and simplifies the spectra as they become more hydrogenic in character. For the early members of the sequence the $2p \rightarrow 3d$ structures show considerable changes as we move from Al^+ to S^{4+} : the supernumerary resonances to the lower energy side of the $2p \rightarrow 3d$ group notably are strong for Al^+ , weaker for Si^{2+} and very much weaker for S^{4+} and Cl^{5+} , showing the rapidly diminishing effects of the main $2p^5 3s(3p^2)$ series perturber (see above).

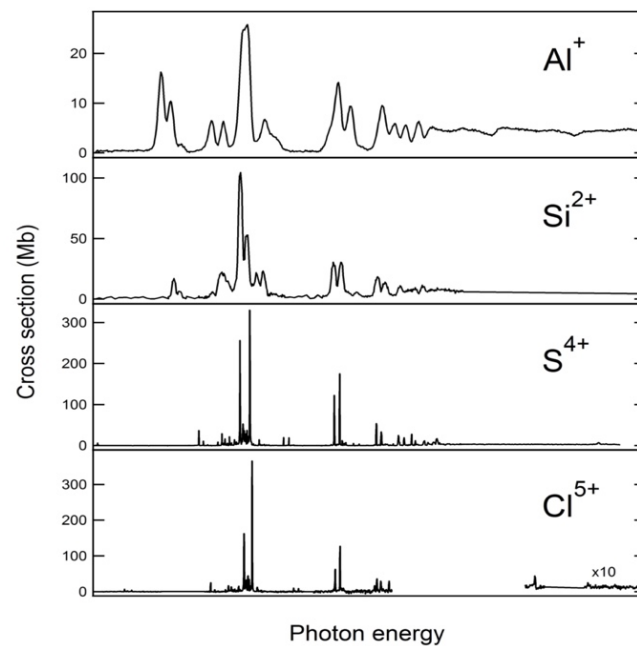


Figure 9. Photoionization cross sections for the magnesium-like ions Al⁺ [9], Si²⁺ [10], S⁴⁺ [18] (sum of the single and double ionization channels) and Cl⁵⁺ (this work: single ionization below, or double ionization above, the photon energy of 300 eV) in the photon energy region corresponding to L-shell excitations, with modified photon energy scales (see text).

In Table 3, we have compiled the main energy level and strength data (resonance energies and inner ionization thresholds) for all the early members of the sequence including magnesium. Where necessary explanations regarding the origin of some data entries are provided in the footnotes of Table 3. We plot this data in two different ways in order to establish isoelectronic trends and interpolate to the missing P³⁺ ion.

Table 3. Top line: Experimental energy (eV), middle line: Non radiative (NR) width (meV) and bottom line: Strength (Mb eV) for the strongest $2p \rightarrow 3d$ ¹P₁, ³D₁, ³P₁ resonances; energy of the 2p limit (eV) and experimental energy of the $2s \rightarrow 3p$ ¹P₁ resonance along the magnesium-like sequence. Experimental data and their reference are provided for all members of the sequence up to Cl⁵⁺, apart from P³⁺ for which interpolated values are deduced. The symbol x indicates that the data is not available. The number in brackets is the experimental uncertainty on the last digit of the data, i.e. 55.492(1) is the same as (55.492 ± 0.001) etc.; the same convention is used for all the data presented in this Table where error values are available.

Atom/ion	$2p \rightarrow 3d$ ¹ P ₁	$2p \rightarrow 3d$ ³ D ₁	$2p \rightarrow 3d$ ³ P ₁	2p limit	$2s \rightarrow 3p$ ¹ P ₁
Mg I	55.492(1)	55.677(1)	55.838(1)	57.658(2) ^e	x
	4.6(9)	5.0(1)	8.2(4)		
	x	x	x		
Al II	84.99(2)	85.36(2)	85.57(2)	91.75(15) ^c	121.5(5)
	x	x	x		
	5.6 ^b	0.54 ^b	1.5 ^b		
Si III	117.6(1)	118.1(1)	118.8(1)	133.5(1) ^c	155.7(4)
	x	x	x		
	37(7) ^b	17(3) ^b	5(1) ^b		
P IV (present work) ^a	154.4	153.9	154.7	180.5	193.6
	x	x	x		
	x	x	x		

	194.88	192.74	193.42	237.35 ^c	235.4
S V	51	47	149		
	46(7) ^b	32(5) ^b	13(2) ^b		
Cl VI (present work)	238.61(2)	235.98(2)	236.71(3)	299.6 ^d	282.66
	46(2)	51(4)	158(65)		
	68(10) ^b	26(4) ^b	9(2) ^b		

^a For P IV the entries are obtained by interpolation of the isoelectronic plots of Figure 10 and italicised for clarity. ^b Not corrected for possible contributions of metastable states. ^c Values estimated from the experimental photon energy of the onset of double ionization. ^d From hydrogenic fit (see text). ^e Statistically averaged over the ²P_{1/2} and ²P_{3/2} components.

Firstly, as shown in Figure 10, the cross section data (represented to scale for all the ions where electronic data is available) are displayed as a function of photon energy, and parametrically, as a function of the net core charge ζ seen by a Rydberg electron (ζ = 1 for Mg, ζ = 2 for Al⁺, etc...). The spectra are shifted vertically from one to the next by an arbitrary amount of 100 Mb for clarity. The three curves in Figure 10 show the movement of the strongest 2p → 3d (the energy differences between the three possible final states of Table 3 are too small to be seen in Figure 9) and 2s → 3p resonances, and the 2p ionization threshold as the net core charge increases from one to six. Noting the very smooth evolution of the curves along the sequence, the data are very accurately represented by 3rd-order polynomial fits (red-, blue- and green-colored broken lines, respectively), it seems justified to derive results for the missing member P³⁺ by interpolation, we show the corresponding data in Table 3.

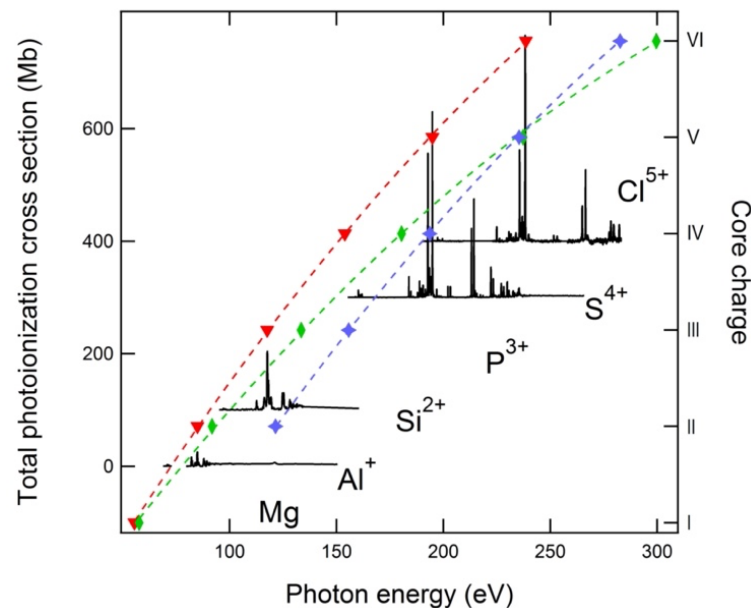
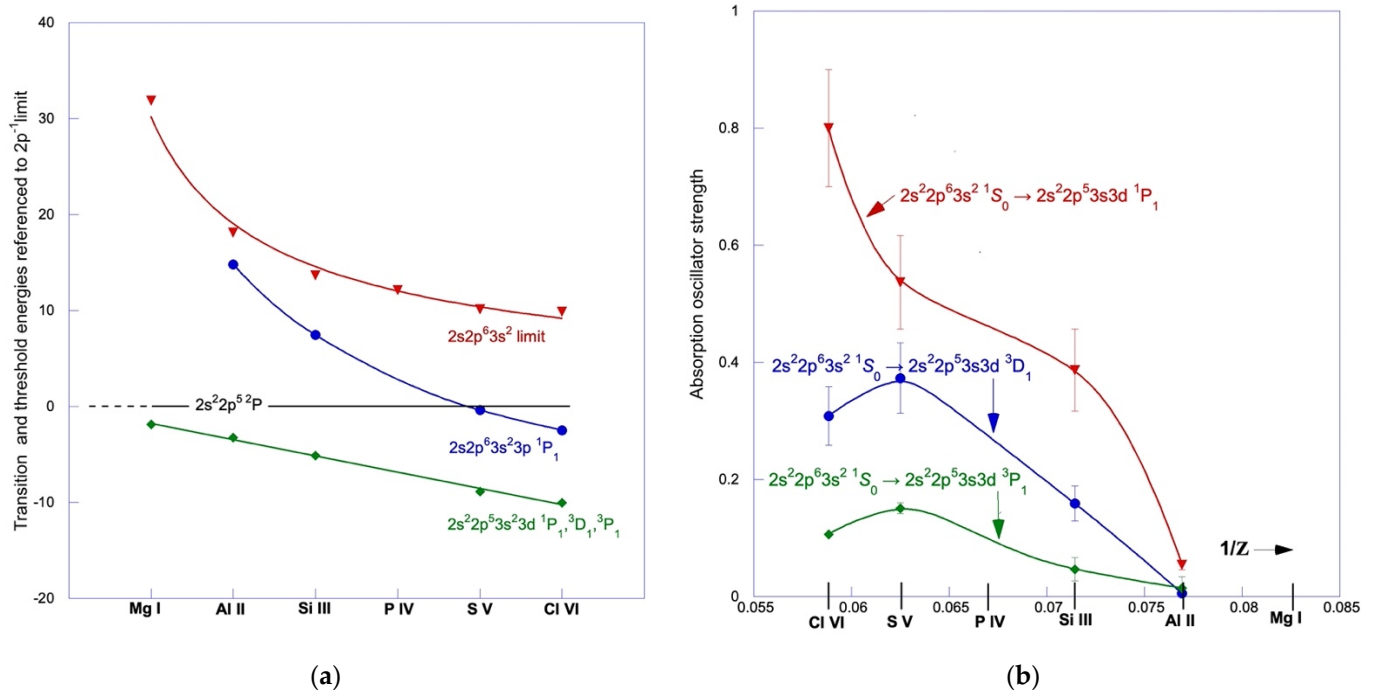


Figure 10. Photoionization cross sections for the magnesium-like sequence Al⁺ [9], Si²⁺ [10], S⁴⁺ [18] (sum of the single and double ionization channels) and Cl⁵⁺ (this work: single ionization below, or double ionization above, the photon energy of 300 eV) in the photon energy region corresponding to L-shell excitations. No experimental data as yet exists for P³⁺. The scale ticks on the right hand side indicates the net core charge of the ion. The energies of the strongest 2p → 3d resonance (red triangles), the 2s → 3p resonance (blue stars) and the 2p⁻¹ threshold (green diamonds) are shown for each ion. The data are very accurately represented by 3rd-order polynomial fits (red-, blue- and green-colored broken lines, respectively) yielding the corresponding photon energies for P³⁺ by interpolation.

We note that for the first four members, the 2s → 3p resonance is found at energies above the 2p threshold. For a value of the net core charge close to five (vicinity of S⁴⁺), this situation is reversed. This is discussed in greater detail below.

Secondly, we examine the isoelectronic trends of characteristic (resonance and threshold) energies and absorption oscillator strength as shown in Figures 11(a) and 11(b), respectively. In Figure 11(a), the $E_{2p \rightarrow 3d}$ and $E_{2s \rightarrow 3p}$ transition energies divided by the net core charge are plotted, referred to the energy value of the first inner limit $2p^5 3s^2 \ ^2P$ (E_{2p}) divided by the net core charge (ζ), i.e. $(E_{2p \rightarrow 3d} - E_{2p})/\zeta$ and $(E_{2s \rightarrow 3p} - E_{2p})/\zeta$, respectively. The energy differences between the three possible final states $^1P_1, ^3D_1, ^3P_1$ are too small to be seen in Figure 11(a). Further relevant data in the form of the theoretical $2s^{-1}$ threshold energies taken from [58], referred to the $2p^{-1}$ threshold in the same manner, are also included in Figure 11(a).



(a) (b) **Figure 11.** Isoelectronic plots for selected L -shell transitions and thresholds along the magnesium electronic sequence: (a) Transition and threshold energies (in eV) relative to the $2p$ limit, divided by the net core charge (spectral roman number) for the first six members of the sequence (the experimental data for P IV is unknown); (b) Absorption oscillator strength plotted as a function of $1/Z$ for the $2p \rightarrow 3d \ ^1P_1, ^3D_1, ^3P_1$ transitions. Further details for both plots are given in the text. The solid lines joining the points in both plots are cubic-spline numerical fits to guide the eye more easily through the data.

From Figure 11(a), we observe a regular (linear) series behaviour for the $2p^5 3s^2 3d$ average term energy, while for both the $2s^2 2p^6 3s^2 3p \ ^1P_1$ and the $2s^{-1}$ threshold energies the series behaviours are clearly non-linear, although smooth. Notably, the energy position of the first member of the asymmetric profile $2s \rightarrow 3p \ ^1P_1$ excitation moves closer to the $2p^{-1}$ threshold as the core charge increases, and drops just below and well below the $2p^{-1}$ threshold for S^{4+} [18] and Cl^{5+} , respectively. This crossing of the $2p^{-1}$ threshold by the $2s^2 2p^6 3s^2 3p \ ^1P_1$ state is accompanied by a noticeable change from Fano to Lorentzian profile and a prominence of the resonance in the single ionization channel only. As one moves further up the sequence this downward movement towards the $2p^{-1}$ threshold (and finally below) is expected to be replicated for the higher members of the series ($n > 3$). We note the similarity of this behaviour with the previously observed behaviour for the $2s \rightarrow np$ transitions in the neon-like sequence [59]. This suggests a lesser role played by the aforementioned $(3s^2 + 3p^2 + 3d^2)$ correlations on the $2s \rightarrow 3p$ transition compared with the $2p \rightarrow 3d$ for the early members of the Mg-like sequence. If we interpolate the data for P^{3+} from Figure 11(a), we obtain the values 154 eV ($2p$ - $3d$) and 195 eV ($2s$ - $3p$), which compare favourably with the corresponding predictions from Figure 10, as shown in Table 3. The value of the $2p^{-1}$ threshold for P^{3+} , which is needed to

obtain the data just quoted, was estimated from [60] to be (183 ± 1) eV and is in reasonable agreement with the interpolated value shown in Table 3.

In Figure 11(b), we plot the oscillator strengths $f_{i \rightarrow j}$ for the $2p \rightarrow 3d$ $^1P_1, ^3D_1, ^3P_1$ transitions obtained from the integrated cross sections (in Mb eV) shown in Table 3, using the standard equation $\int_{line} \sigma(E) dE = 109.8 f_{i \rightarrow j} \int_{line} \Phi_{ij}(E) dE$, where Φ_{ij} is the normalized line profile, as a function of $1/Z$ where Z is the atomic number. Correction factors of 0.95, 0.975, 0.78 and 0.77 were applied to the Al^+ , Si^{2+} , S^{4+} and Cl^{5+} strength values in Table 3, respectively, to take into account the different initial ground state populations. The curves for the $2p \rightarrow 3d$ $^3D_1, ^3P_1$ transitions are seen to present a maximum (near S^{4+}) which is characteristic of series where configuration interaction effects are known to be important [55]. This is fully compatible with our previous discussions regarding the effects of the $(3s^2 3d + 3s 3p^2)$ mixing along the magnesium sequence. As the nuclear charge increases, the oscillator strength transfers into the fully LS allowed $2p$ $^1S_0 \rightarrow 3d$ 1P_1 transition in tandem with the weakening of the configuration interaction effects discussed above.

5. Conclusions

The development of the storage-ring-based merged beam technique has allowed the systematic study of the inner-shell photoionization for extended isoelectronic sequences. For magnesium-like ions, the current results extend the sequence up to Cl^{5+} and the similarity of the S^{4+} and Cl^{5+} ion yields implies that the photoionization behaviour has settled down when compared to the earlier members of the sequence. The new experimental results for Cl^{5+} are compared with *ab initio* MCDF and R-matrix calculations. Differences between the experimental data and the theoretical predictions underscore the importance of the ongoing benchmarking of theory. While the relative energies and strengths of resonances are reasonably predicted by theory, it is clear that significant systematic energy shifts are required to bring the theoretically predicted resonance structures into reasonable coincidence with experiment. Interpolation of the results along the sequence provides estimates for the energies of the $2p$ - $3d$ and $2s$ - $3p$ resonances and the $2p^{-1}$ and $2s^{-1}$ thresholds for the P^{3+} ion, which has not yet been experimentally studied.

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