

# Non-local matching of superpixel-based deep features for color transfer and colorization

Roxane Leduc, Hernan Carrillo, Nicolas Papadakis

### ▶ To cite this version:

Roxane Leduc, Hernan Carrillo, Nicolas Papadakis. Non-local matching of superpixel-based deep features for color transfer and colorization. Image Processing On Line, In press, 14, pp.232-249.  $https://doi.org/10.5201/ipol.2024.522\ .\ hal-04394848v2$ 

# HAL Id: hal-04394848 https://cnrs.hal.science/hal-04394848v2

Submitted on 21 Aug 2024

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Non-local matching of superpixel-based deep features for color transfer and colorization

Roxane Leduc<sup>1</sup>, Hernan Carrillo<sup>2</sup>, and Nicolas Papadakis<sup>3</sup>

<sup>1</sup>INSA Rouen, France
 <sup>2</sup>Univ. Bordeaux, CNRS, Bordeaux INP, LaBRI, UMR 5800, F-33400 Talence, France
 <sup>1</sup>Univ. Bordeaux, CNRS, INRIA, Bordeaux INP, IMB, UMR 5251, F-33400 Talence, France

August 21, 2024

#### Abstract

In this article, we give a thorough description of the algorithm proposed in [H. Carrillo, M. Clément and A. Bugeau, Non-local matching of superpixel-based deep features for color transfer, 2021] for color transfer by relying on a robust non-local correspondence between low-level features at high resolution. An adaptation of this method to colorization process is also described. We highlight the overall relevant results obtained with this technique for both applications and also show its limitations.

### 1 Introduction

This article deals with both color transfer, the process of changing the color distribution of a target image based on a reference image, and colorization, the process of digitally applying color to grayscale images. One practical application of these techniques is, for example, to provide filmmakers with a quasi-automatic tool that makes their tasks less time-consuming and tedious than today's professional software. While both color transfer and colorization can sometimes suffer from poor spatial and color consistency, the method described in the studied paper [3] addresses these issues by relying on robust non-local matching between low-level features at high resolution. The non-local concept has already been used extensively in computer vision, notably by [2] to improve the performance of digital image denoising methods.

The general idea behind the method proposed by [3] is the following. A superpixel segmentation of the target and reference images is first realized using the SLIC algorithm [1]. Next deep feature maps, which are abstract and semantic representations of an image obtained using a pre-trained deep neural network, are extracted at a superpixel level. Subsequently, a non-local correspondence between superpixels of both images is established using an attention mechanism on the deep features. Global relationships between superpixel are taken into account thanks to this non-local correspondence step, that does not include any additional training. Once the non-local correspondence is established, the pixel-level colors are transferred using a weighted average that takes into account the previously computed attention map between superpixels. All in all, the unsupervised method of [3] is able to transfer the color of the reference image to the target image, while respecting the structure of the target and maintaining a limited computation time for efficient image or video processing.

In this paper, we propose an online implementation of this color transfer method and an extension to the colorization problem. While converting a color image to a grayscale image is

a standard task, the reverse operation is a complex problem since no information about the colors to be added is known *a priori*. This task is classically performed by users, based on their expertise or artistic experience to add hues to monochromatic images. We show that it is possible to automate this colorization process thanks to recent advances in machine learning and neural networks.

The organization of the paper is as follows. Section 2 gives a detailed explanation of the non-local matching technique proposed in [3]. We then study the application of the method to color transfer in section 3. The proposed extension to colorization is finally explored in section 4.



Figure 1: Visualisation of a superpixel segmentation S obtained with the SLIC algorithm [1].

## 2 Non-local matching method

In this section, we present the method proposed by [3] for non-local matching of super-pixel-based deep features between two RGB images  $I_T$  and  $I_R$ . In what follows, we will keep the notations of the reference article:  $I_T$  will be the target image and  $I_R$  the reference one. We first describe in section 2.1 the extraction of super-pixels features, called super-features. The matching process between super-features is then detailed in section 2.2.

### 2.1 Super-Features Encoding (SFE)

The encoding of the super-features F of an image I takes place in three stages: 1) super-pixel decomposition, 2) extraction of deep features using convolutional neural networks, 3) channel averaging process to obtain super-features (see Algorithm 1).

#### 2.1.1 Super-pixel segmentation

Firstly, two super-pixel maps are generated using a super-pixel decomposition algorithm on the target and reference images. A super-pixel is a group of connected pixels that share common characteristics such as similarity of color or intensity and spatial proximity. Super-pixels are commonly used to speed up the execution of image processing algorithms and, in some cases, to improve results.

We use the SLIC algorithm [1] which is an adaptation of the k-means clustering algorithm for image segmentation purpose. SLIC segments an image into superpixels using both color and spatial position information. It associates neighboring pixels based on their similarity and updates the superpixel centers until convergence is reached. Rather than simply decimating the image to reduce the amount of information, segmenting into superpixels provides a set of regions of interest to process, without reducing the amount of raw information in the image. Figure 1 illustrates this process. This steps produces two super-pixels maps  $S_T$  and  $S_R$  that respectively contain  $N_T$  and  $N_R$  super-pixels. We also denote as  $P_i^T$  (resp.  $P_i^R$ ) the number of pixels contained in the *i*-th super-pixel  $S_T(i)$  (resp.  $S_R(i)$ ).

#### Algorithm 1: Super-Features Encoding (SFE)

```
Input: f: Features maps H \times W \times C

S: Superpixel map H \times W

N: Number of segments in the Superpixel map

Result: F: Super-Features

for i from 0 to N-1 do

F_T(i) \leftarrow average\_pooling(f(S(i)));
F(i) \leftarrow Stack(F_T(i)); // piling up superpixel i in matrix F of size <math>N \times C
```

#### Algorithm 2: Super-Features Matching (SFM)

```
Input: F_T: Target image Super-features maps H_T \times W_T \times C

F_R: Reference image Super-features maps H_R \times W_R \times C

N_T: Number of segments in the Superpixel map from target

N_R: Number of segments in the Superpixel map from reference

Result: M_{TR}: Correlation matrix N_T \times N_R

for i from 0 to N_T - 1 do

\begin{bmatrix}
\text{for } j \text{ from } 0 \text{ to } N_R - 1 \text{ do} \\
M_{TR}(i,j) \leftarrow \frac{(F_T(i) - \mu_T)^T (F_R(j) - \mu_R)}{\|F_T(i) - \mu_T\|_2 \|F_R(j) - \mu_R\|_2};
\end{bmatrix}
```

#### 2.1.2 Deep features

Deep learning features are obtained from a pre-trained convolutional network applied on the reference and target images  $I_R$  and  $I_T$ . We use here the first three layers — Conv1.2, Conv2.2 and Conv3.4 — of a modified VGG-19 architecture [6] as a feature extractor. These first three layers provide a long range of low-level features that suit diverse types of images.

In each case, after the convolution step and the application of a ReLU function, activations are then batch-normalized before moving on to the next layer. This stabilizes activation values, reduces covariation effects between different activations and improves learning convergence. As mentioned above, the VGG architecture we used is a modified one. Indeed, we decided to replace the max-pooling layers from the baseline VGG-19 architecture by an average pooling (see Section 2.1.3).

This step thus produces l = 3 (one for each layer) feature maps  $f_{Tl}$  and  $f_{Rl}$ , composed of C = 64, 128 then 256 channels. The spatial dimension of the feature maps  $f_{Tl}$  (resp.  $f_{Rl}$ ) correspond to the one of the target image  $I_T$  (resp. reference image  $I_R$ ).

**Remark.** This approach takes into account features derived from VGG-19, a pre-trained deep convolutional networks particularly effective for processing high-dimensional data such as images or videos. The method can nevertheless handle any other handcrafted or learned features.

#### 2.1.3 Average pooling

Finally, we apply average pooling to the deep features using super-pixel maps  $S_T$  and  $S_R$ . The features  $f_T$  and  $f_R$  of the pixels inside each superpixel are averaged per channel and then stacked in the form of matrices known as *super-features*. We therefore obtain three super-feature maps  $F_{T_l} \in \mathbb{R}^{N_T \times C}$ , for the target image, with l index ranging from 1 to 3 corresponding to the information from the first three layers of VGG-19 convolutional neural network and  $N_T$  the number of super-pixels of the target image. In the same way, for the reference image, we obtain three super-feature maps  $F_{R_l} \in \mathbb{R}^{N_R \times C}$ ,  $l = 1 \cdots 3$ . The overall super-features encoding is illustrated in Figure 2.

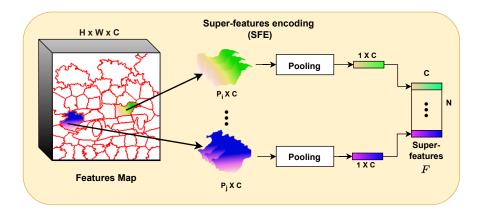


Figure 2: Super-features encoding of [3]. Let H and W be the image size in number of pixels, C the number of channels of the different VGG-19 layers used,  $N_R$  (resp.  $N_T$ ) the total number of reference (resp. target) super-pixels, and  $P_i$  the number of pixels in the i-th superpixel  $S_R(i)$  (resp.  $S_T(i)$ ). The process takes as input a feature map of size  $H \times W \times C$ , in which each super-pixel is extracted and encoded in vectors of size  $P_i \times C$ . Afterward, the vectors are pooled channel-wise and, finally, stacked in the respective super-features matrices  $F_{R_l}$  (resp.  $F_{T_l}$ ) of size  $N_R \times C$  (resp.  $N_T \times C$ ).

## 2.2 Super-Features Matching (SFM)

As stated above, super-features provide a compact encoding for calculating the correlation between deep features. In order to achieve a robust correspondence between the super-features of the target named  $F_{T_l}$  and the super-features of the reference named  $F_{R_l}$ , the authors were inspired by the attention mechanism described in [8].

Attention mechanisms [7] were popularized with the rise of transformers, a type of neural network architecture that has revolutionized the field of natural language processing and other sequence processing tasks. The attention mechanism allows the model to focus on specific parts of the input when generating output. Rather than processing the whole sequence at once, transformers use attention to give variable importance to each element of the sequence depending on its context.

The idea of the Super-Features Matching (SFM) process is to exploit the non-local similarities between the super-features of the images by calculating the attention map at layer l as follows:

$$A_l(i,.) = \operatorname{softmax}\left(\frac{M_{T_l R_l}(i,.)}{\tau}\right), \qquad i = 1 \cdots N_T,$$
 (1)

where, for each superpixel i of the target and j of the reference, we define:

$$M_{T_l R_l}(i,j) = \frac{(F_{T_l}(i) - \mu_{T_l})^T (F_{R_l}(j) - \mu_{R_l})}{\|F_{T_l}(i) - \mu_{T_l}\|_2 \|F_{R_l}(j) - \mu_{R_l}\|_2}.$$
 (2)

In this equation,  $M_{T_lR_l}$  corresponds to the correlation matrix between the super-features of the target  $F_{T_l}(i)$  and the reference  $F_{R_l}(j)$ , computed using the mean values  $\mu \in \mathbb{R}^C$  over the  $N_T$  (resp  $N_R$ ) super-feature values. The choice of the normalization through correlation is motivated by the use of a global temperature parameter  $\tau > 0$  to process all components  $M_{T_lR_l}$  in the same way. The softmax operation in expression (2) is realized with respect to the second dimension of the matrix, so that  $\sum_j A_l(i,j) = 1$  for all super-pixels  $i = 1 \cdots N_T$  of the target image; while  $A_l(i,j) \geq 0$  for all  $i = 1 \cdots N_T$  and  $j = 1 \cdots N_R$ .

The final attention map A is the weighted sum of the attention maps for each layer, divided

by the sum of the weights:

$$A(i,j) = \frac{\sum_{l=1}^{3} w_l A_l(i,j)}{\sum_{l=1}^{3} w_l},$$
(3)

where all weights  $w_l$  are set to 1 in our experiments. The value of the attention map A(i, j) can be understood as a measure of the influence of the super-pixel  $S_R(j)$  of the reference image  $I_R$  for the processing of the super-pixel  $S_T(i)$  of the target image  $I_T$ . For further details, please refer to Algorithmn 2.

#### 2.3 Complexity analysis

Let  $n = H \times W$  be the number of pixels in an image. Then, the number of features in a deep learning feature map is  $D = n \times C$  which translates into a computational complexity of  $\mathcal{O}(D^2) = \mathcal{O}(n^2C^2)$  for computing the correlation matrix. In contrast, with our novel superfeatures encoding, if we set the number of superpixels in the order of  $\sqrt{n}$ , then instead we rewrite with  $D_s = \sqrt{n} \times C$ , resulting in  $\mathcal{O}(D_s^2) = \mathcal{O}(n \times C^2)$  for the correlation operation. As  $C \ll n$  can be ignored, we go from a quadratic to a linear complexity operation  $\mathcal{O}(n)$ .

## 3 Color transfer

In this section, we focus on transferring the color of a reference image  $I_R$  to a target image  $I_T$ . To that end, we follow the color fusion framework initially proposed in [5] which uses the attention maps to obtain the new color for each pixel of the target image.

#### 3.1 Method

Color transfer aims at changing the colors of pixels in the target image  $I_T$  using the color palette of the reference image  $I_R$ . To that end, the method [3] extends the color fusion framework initially proposed in [5]. The process leverages on the attention map A provided by SFE-encoding and SFM-matching, which encodes semantic correspondences between both images. For all pixels inside a super-pixel  $S_T(i)$ ,  $i = 1 \cdots N_T$ , the attention map A(i,j) is used as a weight to balance the importance of the color to transfer from the reference super-pixel  $S_R(j)$ . For more details please refer to the Algorithm 3.

Denoting as  $\overline{I}_R(j)$  the mean color value of pixels belonging to the super-pixel j of the reference image  $I_R$ , the output of the color transfer process on the target image  $I_T$  at pixel p is obtained as

$$\widehat{I}_{T}(p) = \frac{\sum_{j=1}^{N_R} W(p,j) \overline{I}_{R}(j)}{\sum_{j=1}^{N_R} W(p,j)},$$
(4)

where  $W(p,j) = \sum_{i=1}^{N_T} d(p,i) A(i,j)$  and d(p,i) depends on the distance between the pixel p and the center  $\bar{p}_i = (\sum_{p \in S_T(i)} p)/P_i$  of the i-th super-pixel of the target image. This weight is calculated using a Mahalanobis-type formula:

$$d(p,i) = e^{-\frac{(V_T(p) - \overline{V}_T(i))^T \Sigma_i^{-1} (V_T(p) - \overline{V}_T(i))}{\sigma_g}}$$
 (5)

with  $V_T(p) = [p, I_T(p)]$  being the vector describing the position and the color of pixel p, and  $\overline{V}_T(i) = [\overline{p}_i, \overline{I}_T(i)]$  being the average vector describing the position and color centroids of superpixel  $S_T(i)$ . The spatial and colorimetric covariances of pixels belonging to the superpixel  $S_T(i)$  are computed as:

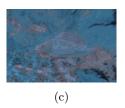
$$\Sigma_i = \begin{pmatrix} \delta_s^2 [Cov(p)]_{p \in S_T(i)} & 0\\ 0 & \delta_c^2 [Cov(I_T(p)]_{p \in S_T(i)} \end{pmatrix}, \tag{6}$$

where the parameters  $\delta_s^2$  and  $\delta_c^2$  respectively weight the influence of spatial and color information. The standard deviation  $\sigma_g$  is used to modulate the sensitivity of the d(p,i) distance to the differences between the vectors  $V_T(p)$  and  $\overline{V}_T(i)$ .

In order to optimize computational performance, an initial resizing (down-sizing) was applied to the  $I_R$  and  $I_T$  input images. To guarantee optimum visual quality at the end of the algorithm, we introduce a conversion to the CIELAB color space. We start by converting  $\hat{I}_T$  from RGB to CIELAB color space. We thus obtain the 3 channels Lab representation  $(\hat{L}, \hat{a}, \hat{b})$  for the colorized image  $\hat{I}_T$ . We then isolate its chrominance channels  $\hat{a}$  and  $\hat{b}$  and use them for the resizing operation (up-sizing). Next, we concatenate the luminance channel of the original  $I_T$  image (also converted into CIELAB space to retrieve the luminance channel) with the resized chrominance channels  $\hat{a}$  and  $\hat{b}$  of  $\hat{I}_T$ . This process replaces the luminance channel of the resulting image  $\hat{I}_T$  with the original gray level of  $I_T$ . This is an essential step to maintain the structural information present in  $I_T$ . Finally, we convert back the resulting image from CIELAB color space to the RGB color space, giving us the final synthesized image. As illustrated in Figure 3, this post-processing makes the colorized images more realistic.







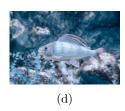


Figure 3: (a) Target; (b) Reference; (c) Resizing without any prior CIELAB conversion; (d) Resizing combined with CIELAB conversion.

. In this setting, we achieve a good trade-off between preserving important image information and achieving a compact representation of the image and have a fast enough process.

#### 3.2 Experimental study

Using the online demonstration, the color transfer method [3] can be applied on any pairs of target and reference images. In this section we carry out a series of experiments to describe the influence of the different parameters.

We first run the companion demonstration code on four pairs of real images<sup>1</sup> to illustrate the pros and cons of this technique applied to color transfer. For this demonstration and based on empirical testing (see Figure 4) we have set the number of superpixels equal to  $3 \times \lfloor \sqrt{H \times W} \rfloor$ . Choosing  $\lfloor \sqrt{H \times W} \rfloor$  superpixels provides a number of segments proportional to the square root of the total image size. This approach balances detail fidelity (preventing over-segmentation that produces too many superpixels) and computational efficiency (avoiding under-segmentation that loses important details). Figure 4 demonstrates the impact of this hyperparameter on color transfer. In Figures 4(a) and 4(b) the sun's reflection on the palm tree appears inadequate, whereas this issue is resolved in Figure 4(c). Additionally, the color of the bushes in Figure 4(c) appears more perceptually natural. Multiplying this number by 3 produces the right amount of superpixels that are more accurate at capturing local detail while remaining manageable for subsequent processing algorithms. For more details on the influence of superpixels and illustration of matched superpixels, we refer the reader to [4].

We now analyze the influence of the different  $\tau$ ,  $\delta_s$ , and  $\delta_c$  parameters of the method. As illustrated in Figure 5, the color transfer method can provide plausible results for images containing a single object of interest (flower and bird examples) or more complex scenes (beach example). In the case of the road against a mountain backdrop – see the 4th row of the figure, the correspondence between super-pixels is questionable (as an example, the color of the broken line in the middle of the road has remained unchanged).

<sup>&</sup>lt;sup>1</sup>Real means no computer-generated images.

#### Algorithm 3: Color transfer

```
Input: I_T: Target image H_T \times W_T \times 3
           I_R: Reference image H_R \times W_R \times 3
Result: I_T: Color transferred image H_T \times W_T \times 3
L \leftarrow 3:
S_T \leftarrow Slic(I_T);
S_R \leftarrow Slic(I_R);
N_T, N_R \leftarrow \text{Number of superpixels from } S_T \text{ and } S_R;
for l from 0 to L-1 do
    f_{Tl} \leftarrow Conv_l(I_T);
    f_{Rl} \leftarrow Conv_l(I_R);
    F_{Tl} \leftarrow \text{SFE}(f_{Tl}, S_T, N_T, N_R);
    F_{Rl} \leftarrow \text{SFE } (f_{Rl}, S_R, N_T, N_R);
    M_{TRl} \leftarrow \text{SFM}(F_{Tl}, F_{Rl}, N_T, N_R);
    for i from 0 to N_T - 1 do
       A_l(i,:) \leftarrow \operatorname{softmax}\left(\frac{M_{TRl}(i,:)}{\tau}\right);
H_T \leftarrow \text{Height of the target image};
W_T \leftarrow \text{Width of the target image};
for h from 0 to H_T - 1 do
    for w from 0 to W_T - 1 do
         p \leftarrow (h, w);
         V_T(p) = [p, I_T(p)];
                                                                                // Position and color of pixel p
         for i from 0 to N_T - 1 do
              \overline{V}_T(i) = [\bar{p}_i, \overline{I}_T(i)];
                                                // Average of the position and color centroids of S_T(i).
              dist(p,i) \leftarrow -(V_T(p) - \overline{V}_T(i))^T \Sigma_i (V_T(p) - \overline{V}_T(i)); // Where \sigma_g is calculated
            d(p,i) \leftarrow e^{-\frac{dist(p,i)}{\sigma_g}}
         \widehat{I}_{T_{ab}}(p) \leftarrow RGB2Lab(\widehat{I}_{T}(p)) // *Passing from RGB to Lab color space to get ab
\widehat{I}_{T_{ab}}(p) \leftarrow Resize(\widehat{I}_{T_{ab}}(p), (H_T, W_T, 2)) // *Interpolation to up-size of the target image I_T
I_{T_{gray}} \leftarrow RGB2Gray(I_T);
\widehat{I}_T(p) \leftarrow Lab2RGB(concat[I_{T_{gray}}, \widehat{I}_{T_{ab}}(p)] \ // \ * \ Concatenation \ of \ original \ luminance \ and
    predicted chrominance.
```

 $\tau$ -parameter sensitivity analysis. We now evaluate the impact of the main temperature parameter  $\tau$  of equation (1), that balances the weights in the attention map A. Figure 6 illustrates the color transfers obtained for the beachfront image and different values of  $\tau$ . As stated in [3], our experiments suggest that a value  $\tau = 1.5e - 2$  gives satisfactory visual results of a large range of images.

As the value of  $\tau$  increases (for example,  $\tau = 1.5e-1$ ), the softmax operation of expression (1) makes the probability distribution A(i, .) more uniform. This implies an important mixing of the

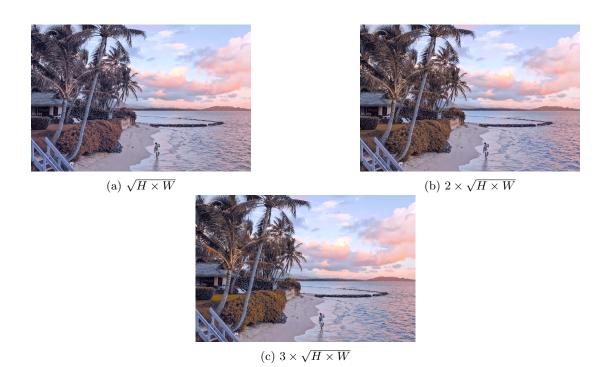


Figure 4: Influence of number of superpixels.

colors of all superpixels  $S_R(j)$ , which lead to drab colors in the synthesized image (Figure 6a). On the other hand, when  $\tau$  decreases, there is a one-to-one matching between a target superfeature and a reference super-feature. For  $\tau = 1.5e - 4$ , this results in non-uniform color transfer at the bottom left part of the image displayed in Figure 6f.

 $\delta_s$  and  $\delta_c$ -parameters sensitivity analysis. We now evaluate the impact of the  $\delta_c$  and  $\delta_s$ -parameters of equation (6), that weight the influence of color and spatial information. Figure 7 illustrates the color transfers obtained for the road image and different values of  $\delta_s$  and  $\delta_c$ . As stated in [3], our experiments suggest that values  $\delta_s = 10$  and  $\delta_c = 0.1$  gives satisfactory visual results of a large range of images. Indeed, with a preponderance of color information  $\delta_c$  and less importance given to spatial information  $\delta_s$ , we observe an inadequate distribution of colors, particularly at the foot of the mountain. In addition, the edges of the road are poorly colored, with dull, lackluster hues that do not faithfully reflect the chromatic palette of the original image.

Limitations. When the shapes and contours of the target image (Figure 8a) differ significantly from those of the reference image (Figure 8b), the transferred colors can appear inappropriate, creating visual artefacts and degrading the perceived quality of the resulting image. In addition, the sharp colors of the reference image may not match the hues of the target image, especially if the latter has more subtle color transitions (see the pixels near the leaves of the tree in Figure 8c). This incompatibility can lead to abrupt and unnatural contrasts in the transformed image, reducing its overall aesthetic.

## 4 Colorization

We now propose an extension of the method [3] to colorization. In this setting, the target image  $I_T$  is a grayscale image, whereas the reference one  $I_R$  is a color image.

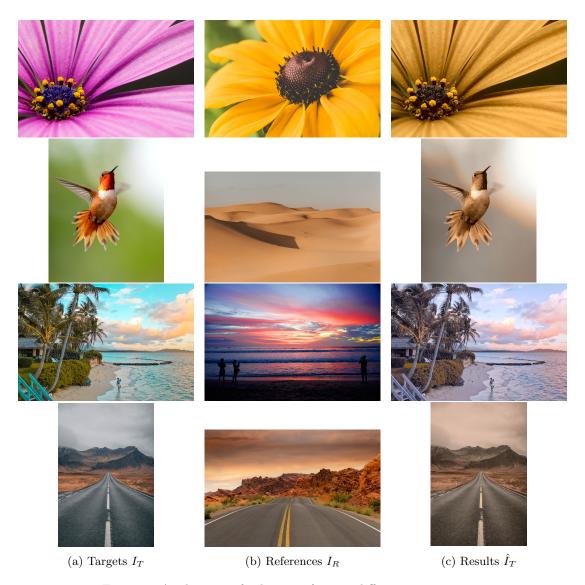


Figure 5: Application of color transfer to 4 different image series.

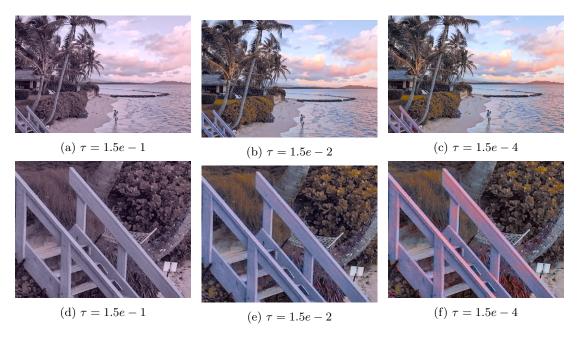


Figure 6: Influence of the temperature value  $\tau$  on the color transfer.

#### 4.1 Method

The colorization technique we propose consists of 4 steps: 1) transformation of the reference color image into a grayscale one  $I_{R_g}$ ; 2) computing SFE-encoding and SFM-correspondences between super-features of grayscale images  $I_T$  and  $I_{R_g}$ ; 3) synthesis of the colorized target image  $\hat{I}_T$ , using attention maps and the original colors of the source image  $I_R$ ; 4) post-processing in CIELAB color space, by mixing the original luminance information in the grayscale image  $I_T$  with the chrominance channels of  $\hat{I}_T$ . For further details, please refer to Algorithm 4.

From colors to grayscale. The transformation of the RGB color image  $I_R = (R, G, B)$  into a grayscale image is done using the standard weighted average from PAL or NTSC models:  $I_{R_q} = 0.299R + 0.587G + 0.114B$ .

Super-features encoding and matching. We apply the SFE-encoding to both the grayscale image  $I_{R_g}$  and the target one  $I_T$ . Next we perform the SFM-matching with a slight modification of the attention map computation described in section 2.2. The merging of the attention maps corresponding to the 3 VGG-19 layers is here realized before the softmax operation:

$$A(i,.) = \operatorname{softmax}\left(\frac{\sum_{l=1}^{3} w_l M_{T_l R_{gl}(i,.)}}{\tau}\right), \qquad i = 1 \cdots N_T.$$
 (7)

In our experiments, this change appeared useful to avoid the transfer of drab colors.

Color fusion framework. The colorized image  $\hat{I}_T$  is obtained by tracing back the original colors of the superpixels in the reference image  $I_R$ , as detailed in equation (4) of section 3.

**Post-processing step.** As explained in section 3, we are going to perform a conversion in CIELAB space in order to improve the visual rendering during resizing, which reduces computation time. We will concatenate the luminance channel of the target grayscale image  $I_T$  with the chrominance channel of the resulting image  $\hat{I}_T$ . Figure 9 illustrates this process that produces



Figure 7: Influence of the  $\delta_s$  and  $\delta_c\text{-parameters}$  on the color transfer.



Figure 8: (a) Target; (b) Reference; (c) Result.

results that are more consistent, more perceptually faithful and less sensitive to variations in brightness.



Figure 9: (a) Target; (b) Reference; (c) Resizing without any prior CIELAB conversion; (d) Resizing combined with CIELAB conversion.

#### 4.2 Experimental study

We present in Figure 10 colorization results obtained with the companion demonstration code applied on four real images. When the source and target images are carefully selected, so that they have a particularly high degree of similarity, the visual results are relevant, with realistic colorization (see for instance the flower and the coastline). The colorization process nevertheless tends to reproduce the most predominant hue in the reference image (dipper and human face examples).

 $\tau$ -parameter sensitivity analysis. We evaluate the influence of the temperature parameter  $\tau$  in equation (7) on the flower example. As illustrated in Figure 11, when  $\tau = 1.5e - 2$ , the color palette of the reference image  $I_R$  is better represented in the colorized image. On the other hand, increasing the value as  $\tau = 1.5e - 1$  results in a decrease in the diversity of colors present in the final image.

 $\delta_s$  and  $\delta_c$ -parameters sensitivity analysis. We now evaluate the impact of the  $\delta_c$  and  $\delta_s$ -parameters of equation (6), that weight the influence of color and spatial information. Figure 12 illustrates the colorization process obtained for the image and different values of  $\delta_s$  and  $\delta_c$ . Again, our experiments suggest that values  $\delta_s = 10$  and  $\delta_c = 0.1$  gives satisfactory visual results of a large range of images. Indeed, when the emphasis is placed primarily on color information while neglecting spatial information, the final rendering proves less satisfactory and lacks coherence. Close examination of the image reveals an inconsistent distribution of colors, marked by noticeable and distinct variations in different places. This non-homogeneity creates contrasting areas where hues appear to diverge significantly, introducing visual irregularities within the image.

Limitations. One of the main problems observed is the tendency to produce an almost monochromatic result, which can appear very artificial. When the reference image (Figure 13b) is dominated by a single hue, this color can be excessively transferred to the target image

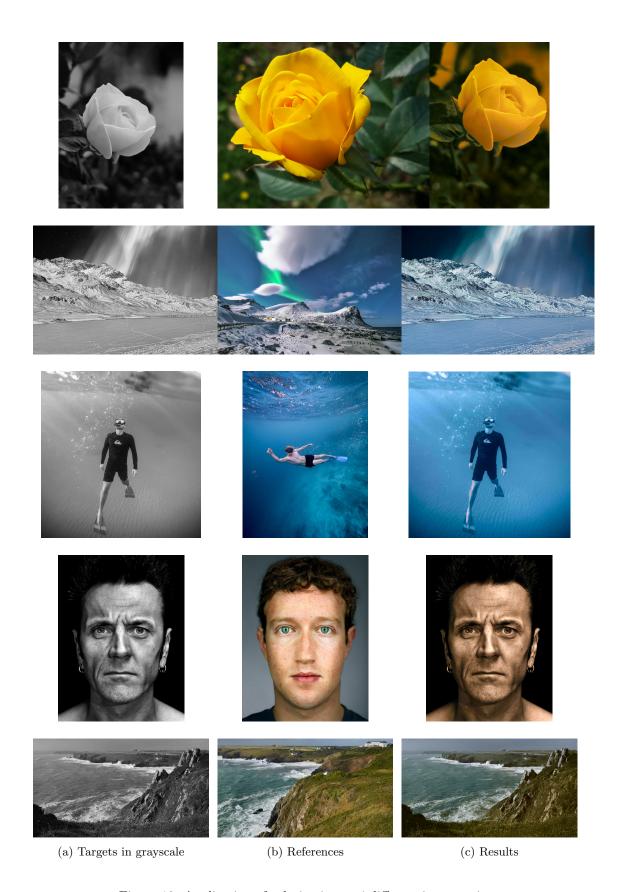


Figure 10: Application of colorization to 4 different image series.



Figure 11: Influence of the temperature value  $\tau$  in the colorization results.

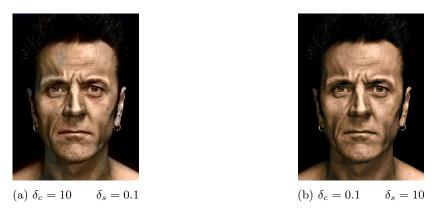


Figure 12: Influence of the  $\delta_s$  and  $\delta_c$ -parameters in the colorization results.

#### Algorithm 4: Colorization

```
Input: I_T: Grayscale target image H_T \times W_T \times 1
            I_R: Reference image H_R \times W_R \times 3
Result: I_T: Colorized target image H_T \times W_T \times 3
I_{R_q} \leftarrow Color\_to\_grayscale(I_R);
S_T \leftarrow Slic(I_T);
S_{R_g} \leftarrow Slic(I_{R_g});
N_T, N_R \leftarrow Number of superpixels from S_T and S_R;
for l from 0 to L-1 do
     f_{Tl} \leftarrow Conv_l(I_T);
     f_{R_gl} \leftarrow Conv_l(I_{R_g});

F_{Tl} \leftarrow \text{SFE}(f_{Tl}, S_T, N_T, N_R);
    F_{R_gl} \leftarrow \text{SFE} (f_{R_gl}, S_{R_g}, N_T, N_R); \\ M_{TR_g} \leftarrow \text{SFM}(F_{Tl}, F_{R_gl}, N_T, N_R);
  A_l \leftarrow w \times M_{TR_q};
for i from 0 to N_T - 1 do
    A(i,:) \leftarrow \operatorname{softmax}\left(\frac{\sum_{l=1}^{L} A_l}{\tau}\right);
H_T \leftarrow \text{Height of the target image};
W_T \leftarrow \text{Width of the target image};
for h from 0 to H_T - 1 do
     for w from 0 to W_T - 1 do
          p \leftarrow (h, w);
          V_T(p) = [p, I_T(p)] ;
                                                                                         // Position and color of pixel p
          for i from 0 to N_T - 1 do
                \overline{V}_T(i) = [\bar{p}_i, \overline{I}_T(i)]; // Average of the position and color centroids of S_T(i).
               dist(p,i) \leftarrow -(V_T(p) - \overline{V}_T(i))^T \Sigma_i (V_T(p) - \overline{V}_T(i)) ;
            for j from 0 to N_R - 1 do
             W(p,j) \leftarrow \sum_{i=1}^{N_T} d(p,i)A(i,j);
             \overline{I}_R(j) \leftarrow The mean color value of pixels in super-pixel j of I_R;
          \widehat{I}_T(p) \leftarrow \frac{\sum_{j=1}^{N_R} W(p,j) \overline{I}_R(j)}{\sum_{j=1}^{N_R} W(p,j)};
\widehat{I}_{T_{ab}}(p) \leftarrow RGB2Lab(\widehat{I}_{T}(p)) // *Passing from RGB to Lab color space to get ab
    chrominance
\widehat{I}_{T_{ab}}(p) \leftarrow Resize(\widehat{I}_{T_{ab}}(p), (H_T, W_T, 2)) // *Interpolation to up-size of the target image I_T
\widehat{I}_T(p) \leftarrow Lab2RGB(concat[I_T,\widehat{I}_{T_{ab}}(p)] \ // \ * \ Concatenation \ of \ original \ luminance \ and
    predicted chrominance.
```

(Figure 13a), regardless of the latter's natural details. As a result (Figure 13c), complex or varied structures in the target image can be simplified or filled by the predominant blue color of the reference, resulting in a significant loss of chromatic diversity and visual detail. In addition, the marked difference in spatial structures between the two images can lead to inconsistent application of color. For example, a bluish hue from the uniform sky in the reference image may be inappropriately applied to detailed, textured areas of the target image, such as players' shirts. This mismatch creates unnatural visual effects.



Figure 13: (a) Target; (b) Reference; (c) Result.

### 5 Conclusion

This paper presents a framework for color transfer and colorization of a target image using the color information contained in a reference image. The process is based on non-local matching of deep features extracted from superpixels through an attention mechanism. Experimental results demonstrate the effectiveness of this technique, that manages to preserve the fine details, textures and structures of the target images, while producing consistent and plausible color synthesis using the information from the reference image.

# Acknowledgment

This study has been carried out with financial support from the French Research Agency through the PostProdLEAP project (ANR-19-CE23-0027-01).

# Image Credits



 $<sup>^2</sup>$ https://www.pexels.com/fr-fr/discover/

<sup>3</sup>https://dspace.mit.edu/bitstream/handle/1721.1/100018/Durand\_Style.pdf



#### References

- [1] R. Achanta, A. Shaji, K. Smith, A. Lucchi, P. Fua, and S. Süsstrunk, *SLIC Superpixels Compared to State-of-the-Art Superpixel Methods*, IEEE Transactions on Pattern Analysis and Machine Intelligence, 34 (2012), pp. 2274–2282.
- [2] A. Buades, B. Coll, and J.-M. Morel, A Non-Local Algorithm for Image Denoising, in 2005 IEEE Computer Society Conference on Computer Vision and Pattern Recognition (CVPR'05), vol. 2, 2005, pp. 60–65.
- [3] H. CARRILLO, M. CLÉMENT, AND A. BUGEAU, Non-local Matching of Superpixel-based Deep Features for Color Transfer, in International Conference on Computer Vision Theory and Application (VISAPP'22), 2022, pp. 38–47.
- [4] H. CARRILLO, M. CLÉMENT, AND A. BUGEAU, Super-attention for exemplar-based image colorization, in Proceedings of the Asian Conference on Computer Vision, 2022, pp. 4548–4564.
- [5] R. GIRAUD, V.-T. TA, AND N. PAPADAKIS, Superpixel-based color transfer, in IEEE International Conference on Image Processing (ICIP'17), 2017, pp. 700–704.
- [6] K. Simonyan and A. Zisserman, Very deep convolutional networks for large-scale image recognition, arXiv preprint arXiv:1409.1556, (2014).
- [7] A. VASWANI, N. SHAZEER, N. PARMAR, J. USZKOREIT, L. JONES, A. N. GOMEZ, L. KAISER, AND I. POLOSUKHIN, Attention is all you need, Advances in neural information processing systems, 30 (2017).
- [8] B. Zhang, M. He, J. Liao, P. V. Sander, L. Yuan, A. Bermak, and D. Chen, Deep exemplar-based video colorization, in IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR'19), 2019, pp. 8052–8061.