



**HAL**  
open science

## Coherent acoustic pulse emission by ensembles of plasmonic nanoparticles

Balint Eles, Aurélien Crut, Natalia Del Fatti, Julien Lumeau, Antonin Moreau, Vincenzo de Michele, Youcef Ouerdane, Nathalie Destouches

► **To cite this version:**

Balint Eles, Aurélien Crut, Natalia Del Fatti, Julien Lumeau, Antonin Moreau, et al.. Coherent acoustic pulse emission by ensembles of plasmonic nanoparticles. *The European Physical Journal. Special Topics*, 2023, 232 (13), pp.2221-2230. 10.1140/epjs/s11734-023-00811-x . hal-04415560

**HAL Id: hal-04415560**

**<https://cnrs.hal.science/hal-04415560v1>**

Submitted on 11 Apr 2024

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# Coherent acoustic pulse emission by ensembles of plasmonic nanoparticles

*Balint Eles<sup>1</sup>, Aurélien Crut<sup>2</sup>, Natalia Del Fatt<sup>2</sup>, Julien Lumeau<sup>3</sup>, Antonin Moreau<sup>3</sup>, Vincenzo De Michele<sup>1</sup>, Youcef Ouerdane<sup>1</sup>, Nathalie Destouches<sup>1,\*</sup>*

*<sup>1</sup>Univ Lyon, UJM-Saint-Etienne, CNRS, Institut d Optique Graduate School, Laboratoire Hubert Curien UMR 5516, F-42023 Saint-Etienne, France*

*<sup>2</sup>FemtoNanoOptics group, Université de Lyon, CNRS, Université Claude Bernard Lyon 1, Institut Lumière Matière, F-69622 Villeurbanne, France*

*<sup>3</sup>Aix Marseille Univ, CNRS, Centrale Marseille, Institut Fresnel, Marseille, France*

## **Corresponding Author**

\* [nathalie.destouches@univ-st-etienne.fr](mailto:nathalie.destouches@univ-st-etienne.fr)

## **ABSTRACT**

The ability of a layer of silver nanoparticles with broad size dispersion to excite a coherent acoustic phonon wave-packet in its supporting glass substrate following femtosecond laser excitation was tested using time-domain Brillouin scattering in transmission configuration. The generation and propagation over several micrometer distances of gigahertz acoustic phonons in the underlying glass was observed for all investigated samples, involving nanoparticle layers with different morphological properties. The phonon wave-packet exhibits frequency-dependent attenuation rates and amplitudes in the 40 GHz – 50 GHz acoustic frequency region. The measured attenuation rates are consistent with previous experimental results on silica, indicating that anharmonic interaction of acoustic waves with the thermal phonon bath has dominating contribution to the phonon damping. The features of the acoustic waves emitted by a discontinuous nanoparticle layer were investigated using a simplified theoretical model, allowing to better understand at which condition they are similar to those of the waves emitted by a continuous thin film.

Keywords: Opto-acoustic transducer, Picosecond acoustics, Nanoparticle ensemble, Brillouin oscillation, Phonon damping

## Introduction

Efficient coupling between light pulses and the acoustic phonons of a material can be realized using different types of opto-acoustic transducers, enabling the generation of coherent wave-packet of phonons with picoseconds pulse duration and nanometric spatial extent in the material. Such acoustic pulses find applications in nanoscale imaging of mechanical properties,<sup>1</sup> or in fundamental studies on frequency-dependent sound attenuation, e.g. in disordered media.<sup>2-4</sup> Thin metallic films are frequent choices for opto-acoustic transducers.<sup>5,6</sup> Due to the strong optical absorption of metals, the temperature of a metallic film is rapidly increased following its pulsed illumination resulting in its thermal expansion, which launches a wave-packet of acoustic phonons propagating away from the film at the local speed of sound. The spectral content of the acoustic wave-packet is strongly dependent on the thickness of the metallic thin film and on the properties of its interface with the investigated material, which determine the frequencies and damping rates of the film vibrations.

Several investigations were also conducted with size-reduced transducers, which is crucial for improving the lateral resolution in imaging applications (lateral resolution being limited by diffraction to a few hundreds of nanometers in the film case). Quantum wells were for instance used as acoustic sources.<sup>7</sup> Additionally, attempts were made for using as transducers single metallic nanoparticles, whose vibrational eigenmodes have been widely investigated.<sup>8-15</sup> Guillet et al. detected ultrasonic waves emitted by a single submicronic gold particle in the surrounding silica matrix using picosecond ultrasonics technique in reflection configuration.<sup>16</sup> Single cylindrical shaped gold nanoparticles on a silicon wafer were demonstrated to exhibit excellent potential for transduction of bulk transverse waves.<sup>17</sup> Yu et al. demonstrated that laser excitation of a single gold micrometer-sized nanoplate efficiently generates longitudinal acoustic waves in glass substrate, which were detected by their associated Brillouin oscillations.<sup>18</sup> Hypersounds emitted by a single copper nanowire in the surrounding silicon membrane were also detected.<sup>19</sup> Another study evidenced that a single gold nanorod can act like an opto-acoustic nanosource of propagating longitudinal acoustic wave in silica substrate.<sup>20</sup>

Beside the acoustic pulse emission into the bulk matrix, hypersonic surface waves can be excited, as well as detected, using single plasmonic nanoantennas.<sup>21</sup>

Ensembles of close metal nanoparticles represent an intermediate case between those discussed above (continuous film and single nanoparticle). In earlier studies, near-coalescence metallic nanoislands were demonstrated as excellent candidates for fabricating nanoscale electronic components,<sup>22–24</sup> surface enhanced Raman scattering<sup>25</sup> and pioneering sensing approaches,<sup>26</sup> to mention a few. Additionally, there have been numerous investigations on excitation of acoustic vibration modes on nanoparticle ensembles. These studies, mostly performed on nanoparticles embedded in a solid matrix or in solution, have in particular addressed in detail the size, shape and environment dependence of vibrational frequencies (quantitative investigations of vibrational quality factors being challenging due to spurious inhomogeneous effects associated to inherent size and shape dispersion).<sup>22–30</sup> However, the detection of coherent acoustic pulse emission by ensembles of nanoparticles in their environment has not been demonstrated yet. In the present article, we report the detection of coherent acoustic pulses emitted by a layer of silver nanoparticles with broad size dispersion and propagating over several microns distances in the underlying glass substrate. Four samples with various interparticle distances and shape properties were investigated, and the attenuation of the Fourier spectral components was monitored in the acoustic frequency range of 40 GHz – 50 GHz during the propagation away from the acoustic sources. The limits for the application of such nanoparticle ensembles for opto-acoustic transducers are demonstrated.

## Experimental methods

Multilayer samples composed of  $\text{TiO}_2\text{:Ag:TiO}_2$  with different nominal Ag thicknesses are prepared using physical vapor deposition at room temperature on N-BK7 glass substrate. The chemical composition of the substrate is provided as 69.13  $\text{SiO}_2$ , 10.75  $\text{B}_2\text{O}_3$ , 10.40  $\text{Na}_2\text{O}$ , 6.29  $\text{K}_2\text{O}$ , 3.07  $\text{BaO}$  and 0.36  $\text{Sb}_2\text{O}_3$  in wt %. Ag layers are obtained from Ag granules, and  $\text{TiO}_2$  layers from pure  $\text{TiO}_2$  material. Three samples with initial Ag thicknesses of 1.5 nm, 5 nm and 10 nm are prepared in this study. Due to the ultrathin layers, non-spherical, near-coalescence Ag nanoislands are obtained. The thicknesses of both  $\text{TiO}_2$  layers are fixed at 30 nm in all samples. The conditions of the sample preparations and the transmittance spectra can be found in Supplementary Information.

The picosecond acoustic experiment is based on a Yb:KGW femtosecond laser (PHAROS from Light Conversion) operating at 60 kHz, with a pulse duration of  $\sim 200$  fs, central wavelength of 1030 nm and output power of 6 W. The pump beam is obtained from an OPA and a subsequent stage of harmonic generator (both from Light Conversion) capable of tuning the pump wavelength from 210 nm to 20  $\mu\text{m}$ . Pump wavelengths are chosen to directly excite the broad localized surface plasmon resonance (LSPR) of the different samples, i.e. 1100 nm, 1000 nm and 700 nm respectively for the three initial samples with decreasing Ag thicknesses, and 540 nm for an additional laser-processed sample described in the next section. The time-resolved experiments are conducted in a commercial pump-probe arrangement (HARPIA from Light Conversion). The pump is chopped at 75 Hz and focused on the sample at nearly normal incident angle. The probe is time-delayed with respect to the pump with a maximum time delay up to  $\sim 7$  ns, and then frequency-doubled to produce 515 nm beam using a beta barium borate crystal. Spectrally broad white-light continuum (350 nm – 650 nm) is generated in a 4 mm thick sapphire crystal, subsequently the beam is focused on the sample by a parabolic mirror at normal incident. The pump and the probe beam spot diameters are around 100  $\mu\text{m}$  and 90  $\mu\text{m}$ , respectively. The transmitted probe light is collected using the imaging spectrograph (Kymera 193i, OXFORD instruments) equipped with a NMOS linear image sensor (HAMAMATSU S8380-256Q). The spectral resolution is  $\sim 1.7$  nm, acquiring 32 pulses/spectrum (0.5 ms of integration time). Every transient spectrum is the average of 10,000 spectra.

The detection principle of the coherent acoustic pulse propagation is provided as follows. Each wavelength in the probe beam is partially transmitted and back-reflected by single phonon frequency component (phase-matched phonon) in the acoustic wave-packet via Brillouin scattering process. The back-reflected portion of the beam escapes the sample after reflection on the transducer layer, and interferes with the transmitted light in the spectrograph. As the strain pulse propagates with the local speed of sound in the substrates, the interference pattern periodically varies leading to oscillating signal with the time delay  $t$ . The temporal period of the oscillating signal is derived as

$$T = \frac{\lambda_0}{2vn}, \quad (1)$$

where  $\lambda_0$  is the vacuum probe wavelength,  $v$  is the local sound velocity,  $n$  is the refractive index of the medium.  $T$  corresponds to the inverse of the frequency of the phase-matched acoustic phonon. When attenuation is present during the propagation of the wave-packet, the

amplitude decrease of the oscillations provides information on the attenuation of the phase-matched Fourier component.

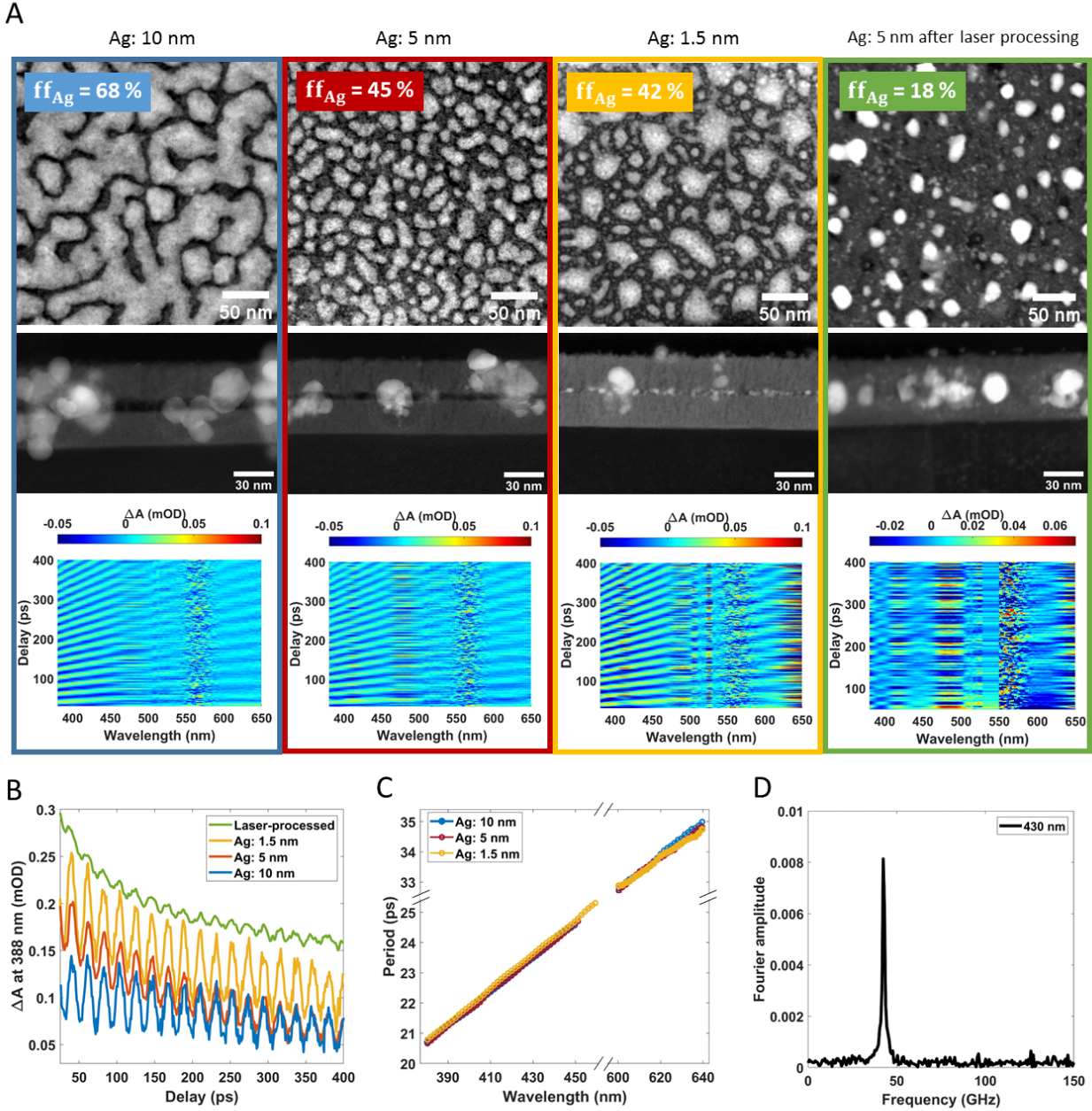
## Results and discussion

In Figure 1 panel A, the first three columns contain plane-view high-angle annular dark-field scanning transmission electron microscope (HAADF-STEM) images of the samples with different initial nominal thicknesses (10 nm, 5 nm, 1.5 nm), the corresponding cross-section images and the 2D maps of transient absorption spectra after thermal background removal. The fourth column contains an additional measurement performed on the *Ag: 5 nm* sample after submission to laser processing by 515 nm wavelength using 31 mJ/cm<sup>2</sup> laser fluence in order to persistently reshape the initial nanoparticle size and shape distribution. The details of the laser reshaping experiment can be found in the Supplementary information. As a result, rather spherical nanoparticles distribution with considerably smaller surface covering is achieved. As revealed by the cross-section HAADF-STEM image of this sample, the multilayer system collapses into a single layer of TiO<sub>2</sub> with nanoparticles embedded due to the high laser-induced temperature rise in the material. In each cross-section image, massive nanoparticle traces can be observed in the TiO<sub>2</sub> layers, which results from the TEM lamella preparation.

The comparison of the STEM images at different nominal thickness reveals two main structural characteristics. Firstly, the correlation between the Ag thickness and the average neighboring distance between the adjacent nanoparticles (nanoislands), i.e. smaller Ag thickness results in higher nanoparticle separation. This results in smaller LSPR coupling, reflected as a blue-shifting resonance in the steady-state spectra (shown in Supplementary Information). Secondly, the morphology and connectivity of the film nanoparticles, i.e., the thickest sample contains highly connected complex structures, which transform into more simple distributions of clearly separated rod-like (*Ag: 5 nm*) and rather spherical particles (*Ag: 1.5 nm* and laser-processed sample). In the latter two cases, nanoparticle diameters vary on a scale from a few nm until few tens of nm (typically 30 nm – 40 nm), and the average interparticle distance is estimated in the range of 10 nm in the laser-processed sample. The *Ag: 10 nm* sample is the one with the morphology closest to the one used in traditional time-resolved Brillouin scattering experiments, where continuous metallic layers with typical thicknesses of few tens of nanometers are used as transducers.

The 2D carpets of the transient absorption spectra reveal the presence of an oscillatory signal for all samples (Figure 3A), which is ascribed to Brillouin oscillations induced by the propagation of an acoustic pulse in the underlying glass substrate. The amplitudes of these oscillations exhibit strong probe wavelength-dependence. Beside the observed large amplitudes, Brillouin oscillations are not detected in the spectral region 540 nm – 590 nm due to low probe intensity, and the amplitude is strongly disturbed by noise in the region 450 nm – 490 nm. It is important to notice that the 2D carpet of the laser-processed sample also contains an oscillatory signal component in the reduced wavelength range of 380 nm – 400 nm. However, its amplitude is considerably smaller compared to the three intact samples. Image B shows the example time trace of 388 nm for the four samples (the green curve was shifted vertically for clarity). The limited efficiency for the coherent pulse excitation is attributed to the low filling factor of the nanoparticles, and will be investigated in the modelling section of the paper. Image C shows that the period of the vibrations linearly increases with probe wavelength from 20.8 ps to 35.3 ps for the three intact samples, in agreement with Eq. (1) and the low dispersion of the glass refractive index on this probe wavelength range. The period at each probe wavelength was determined based on the raw time traces by averaging 10 oscillations. Image D shows the Fourier amplitude spectrum of a representative time trace at 430 nm (*Ag: 10 nm sample*) with a single spectral peak at 42.7 GHz, i.e., the phase-matched acoustic frequency at this particular wavelength.

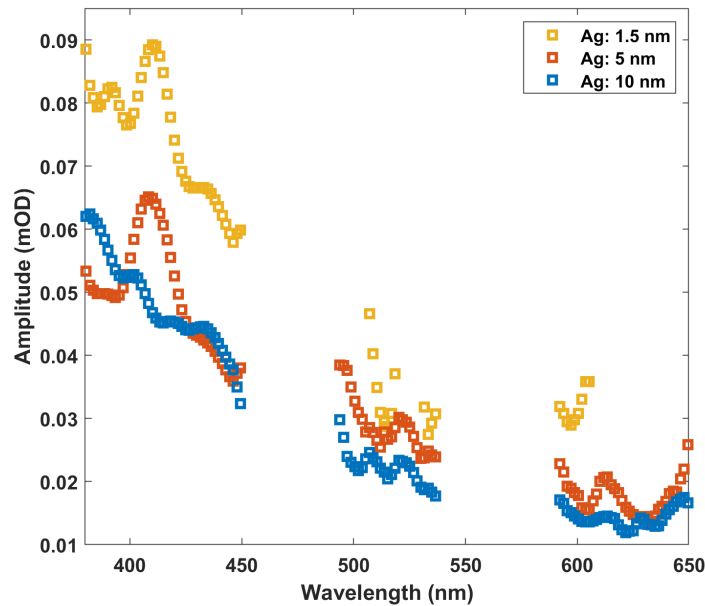
The sound velocity of  $5993 \pm 14$  m/s in N-BK7 was determined based on the expression of the oscillation period using the average of the determined period at each probe wavelength and the refractive index spectrum of N-BK7 provided by Schott. Additionally, one can assume that each frequency component propagates with the same phase velocity. For comparison, the sound velocity in vitreous silica thin films measured by the same experimental technique reported by Ayrinhac et al.,  $5995 \pm 10$  m/s is very close to our value.<sup>36</sup> The similarity of these determined sound velocities is consistent with the fact that silica is the main component of N-BK7 glass.



**Figure 1.** *A: Plan-view and cross-section HAADF-STEM images of the different samples, and the 2D maps of the corresponding transient absorption spectra after thermal background subtraction highlighting the Brillouin signals.  $ff_{Ag}$  stands for Ag filling factor. Note, that even the laser-processed sample, the 2D carpet evidences small amplitude Brillouin signal between 380 and 400 nm. B: Example time traces probed at 388 nm for each sample before background removal (raw experimental data). The trace of the laser-processed sample (green) is shifted vertically for clear observation of the residual Brillouin oscillation. C: Plot of vibration period vs probe wavelength for the different samples. The data from the laser-processed sample is not plotted due to the small vibration amplitude and wavelength range. D: Fourier amplitude spectrum of the representative probe wavelength of 430 nm (from Ag:10 nm sample) indicating the presence of a single frequency component of 42.7 GHz.*



The amplitude of the oscillations exhibits a non-monotonic decrease tendency towards longer probe wavelength, as shown in Figure 2 for the three intact samples. The amplitude values contain the average of the first three cycles in the vibration for each wavelength. The decreasing tendency in the oscillation amplitude is not related to the excitation of the acoustic pulse since the power of the pump laser is identical for all the probe wavelengths, nor with the spectral intensity profile of the probe laser. One should note that the probe photon energy for a shorter wavelength is higher and closer to the energy band gap of the N-BK7 glass substrate. For Schott BK7 borosilicate glass, the energy band gap was calculated from the transmission spectrum of the glass to be 4.28 eV.<sup>37</sup> The 380 nm probe should be more sensitive to the band gap energy modulation induced by the traveling acoustic pulse, but less for higher probe wavelengths with lower energies. In other words, the photoelastic coupling for the N-BK7 glass is stronger for a blue probe wavelength than for a longer wavelength.<sup>38</sup>



**Figure 2.** The probe wavelength dependence of the Brillouin signal's amplitude for the different samples.

Ishioka et al. studied the energy dependence of coherent phonons in GaP and Si in the probe energy range from 480 nm to 630 nm.<sup>39</sup> They measured that the differential reflectivity amplitude of the oscillations increased significantly for GaP approaching 480 nm, but moderately for Si. Baydin et al. measured drastic increase of the amplitude of Brillouin oscillations towards higher probe energy, and it is maximized near the direct optical transitions

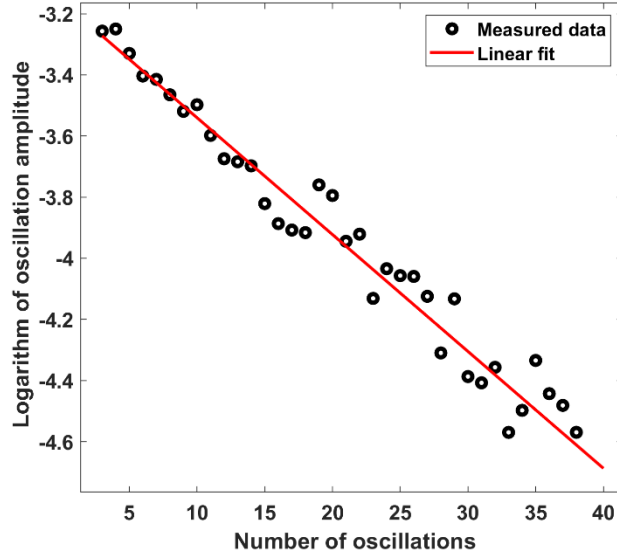
of GaP.<sup>40</sup> Above the direct band gap, a nontrivial wavelength-dependence was measured. Additionally, a theoretical model was developed to quantitatively explain the measured oscillation amplitudes. Assuming weak strain amplitudes, i.e. strains  $< 10^{-4}$ , and that the temporal shape of the pulse can be described by derivative of a Gaussian, a simple expression was derived stating that the differential reflectivity amplitude of the oscillation is proportional to the photon energy derivative of the complex dielectric function  $\epsilon$ :

$$A_{osc} \propto \left| \frac{\partial \epsilon}{\partial E} \right| = \sqrt{\left( \frac{\partial \epsilon_r}{\partial E} \right)^2 + \left( \frac{\partial \epsilon_i}{\partial E} \right)^2}, \quad (2)$$

where  $\epsilon_r$  and  $\epsilon_i$  are the real and imaginary parts, respectively. Thereby, the dielectric function of the medium in which the acoustic pulse propagates determines the probe wavelength-dependence of the Brillouin oscillation's amplitude. Qualitatively, the non-monotonic decreasing tendency of the measured oscillation amplitude in the present case could be also related to the  $|\partial \epsilon / \partial E|$  spectrum of the glass substrate. In glass, one can neglect the second term in Eq. (2) in the visible wavelength range as  $\epsilon_i \ll \epsilon_r$ , therefore the oscillation amplitudes will be determined by the energy derivative of the real dielectric function (the spectra of  $\epsilon_i$  and  $\epsilon_r$ , and the calculated  $|\partial \epsilon / \partial E|$  for N-BK7 can be found in the Supplementary Information).

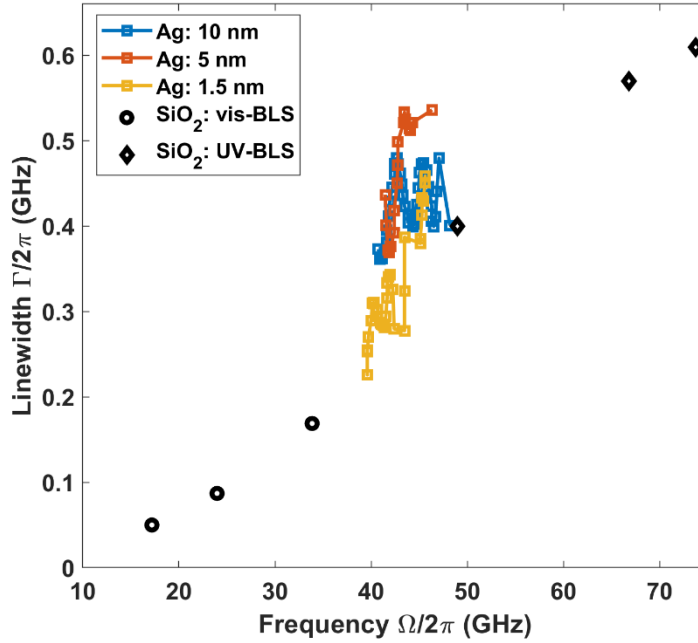
Due to the rapidly decreasing vibration amplitude the wavelength-dependent attenuation is investigated exclusively for the spectral region of 380 nm – 450 nm in the followings. The logarithm of the oscillation amplitude as a function of the oscillation number is reported in Figure 3 using the representative example time trace of 430 nm, where circles show the determined amplitude of the oscillations, and red solid line shows linear fit to the data points. The data fit on a straight line in presence of exponential decay of the phonon frequency components during the propagation in the glass. Deviation from exponential decay would indicate acoustic pulse diffraction, i.e., spreading of the pulse during propagation, or significant density of inhomogeneities inside the glass.<sup>41</sup>

Each oscillation corresponds to an acoustic pulse propagation by a distance of  $\lambda_0/2n$ . Until the the coherent signal is lost ( $\sim 1000$  ps), the strain pulse propagates a distance of about  $\sim 6$   $\mu\text{m}$  away from the nanoparticle layer in the bulk glass. It has to be emphasized that the coherent acoustic pulse excitation originates from the optical response of the individual nanoparticles with diameters varying from a few nanometers until a few tens of nanometer (Figure 1, STEM images of the *Ag: 1.5 nm* and laser-processed samples).



**Figure 3.** The decay of the logarithm of the oscillation amplitude with increasing oscillation number for the representative example time trace of 430 nm (from Ag:10 nm sample). The linear fit to the measured data points is indicated by red line.

From the fit of the experimental data to the straight line, one can conclude that the amplitude decay is exponential with increasing propagation distance  $d$ ,  $A(d) \propto e^{-\alpha d}$ , where  $\alpha$  is the attenuation coefficient determined from the linear fit. The  $\alpha$  attenuation coefficient was calculated for each wavelength in the range 375 nm – 460 nm for the three intact samples, covering the acoustic frequency range 39.6 GHz – 48.1 GHz that is obtained as the inverse of the oscillation periods. The acoustic linewidth parameters that would have been measured in a scattering experiment<sup>42-45</sup> were calculated as  $\Gamma/2\pi = \alpha v/\pi$ , where  $v$  is the previously obtained sound velocity in N-BK7. The obtained linewidth values are reported in Figure 4. For comparison, data in SiO<sub>2</sub> from visible BLS technique at three scattering angles,<sup>46</sup> and from UV-BLS technique measured at two angles<sup>47</sup> or at two wavelengths<sup>48</sup> are also plotted. The general tendency of non-monotonic increasing attenuation rate towards higher acoustic frequencies is reflected in our data.



**Figure 4.** The measured linewidth parameters in the function of the acoustic frequency for the different samples. Data obtained in SiO<sub>2</sub> measured by visible BLS (Ref. 46) and UV-BLS (Refs. 47 and 48) techniques are plotted for comparison.

The acoustic frequency dependence of the sound attenuation in disordered materials originates from an interplay of several physical mechanisms from the ultrasonic to the THz frequency regions at different temperatures. The room temperature sound damping is ruled by internal friction due to anharmonic interactions of the acoustic wave with the thermal phonon bath and thermally activated relaxation (TAR) of structural inhomogeneities in the acoustic frequency region of  $\sim 10$  GHz until  $\sim 100$ s of GHz.<sup>36,49</sup> At 35 GHz and room temperature, the sound damping due to anharmonicity contributes nearly twice compared to thermally activated relaxation.<sup>3</sup> This results in a nontrivial frequency dependent attenuation, however, the tendency could be approached by a quadratic scaling in agreement with the Akhiezer mechanism.<sup>50,51</sup> This was supported by experimental characterizations using ultrasonics and Brillouin light scattering (BLS).<sup>46–48</sup> Theoretical models have been developed and proposed to describe the relaxation processes of sound attenuation in glasses.<sup>4,52–54</sup> Towards higher frequencies, the contribution of TAR exhibits saturation and anharmonicity becomes the dominant source of sound damping approaching the frequency region of  $\sim 200$  GHz. Further increasing acoustic frequencies around  $\sim$ THz exhibits damping proportional to the fourth power of the acoustic frequency as measured in densified silica and lithium diborate glasses by inelastic x-ray scattering.<sup>43,44</sup> The increased rate of damping is expected for elastic scattering in

a statically disordered medium compatible with the Rayleigh law.<sup>50,51,55</sup> In the middle acoustic frequencies in the region of hundreds of GHz until the onset of the Rayleigh regime, a non-trivial frequency dependence was reported by several experimental works.<sup>6,36,49,56</sup>

As shown in the reference,<sup>36</sup> the data points from the BLS experiments in Figure 4 align precisely to the theoretical prediction of the sum of anharmonicity and TAR mechanisms with nearly two times stronger contribution from anharmonicity. Based on the quantitative fit of our data points among the BLS data, we suggest that these two mechanisms rule the sound attenuation in the present N-BK7 multicomponent glass as well in the acoustic frequency region of tens of GHz.

As previously discussed, our work demonstrates that a discontinuous nanoparticle layer can generate optically detectable acoustic waves in its supporting glass substrate. In the following, we describe a simple 2D model built to qualitatively explain this key experimental observation and better understand the relation between the morphological properties of a nanoparticle layer and the features of the acoustic waves that it produces. This model addresses the simplified case of an infinite one-dimensional chain of uncoupled, point-like emitters with non-uniform density, emitting scalar waves in a half-plane, whose attenuation upon propagation is neglected.

The density of emitters is described by a function  $(a)$ , with  $a$  the spatial coordinate along the emitter chain (located at  $z=0$ ). All emitters are assumed to generate coherent acoustic pulses of same angular frequency  $\omega$  and duration  $\tau$ , described by the damped oscillating function of time  $h(t)$  such as (using complex notation) :

$$h(t) = \begin{cases} 0 & \text{if } t < 0 \\ e^{-\frac{t}{\tau}} e^{i\omega t} & \text{if } t \geq 0 \end{cases} \quad (3)$$

The wave created at a  $(x, z)$  point located at a distance  $z$  from the 1D emitter chain results from the interferences between the circular waves generated in the  $z > 0$  half-plane by all the emitters. Its complex amplitude  $A(x, z, t)$  thus writes, introducing  $a' = a - x$ :

$$A(x, z, t) = \int_{-\infty}^{\infty} f(a' + x) \frac{h\left(t - \frac{\sqrt{a'^2 + z^2}}{c_L}\right)}{(a'^2 + z^2)^{\frac{1}{4}}} da' \quad (4)$$

where  $c_L$  denotes the speed of sound in the  $z > 0$  half-plane and  $\sqrt{a'^2 + z^2}$  corresponds to the distance between the emitter located in  $(a, 0)$  and the  $(x, z)$  point where the amplitude is

calculated. Since  $h(t) = 0$  for  $t < 0$  (Eq. (3)),  $A(x, z, t) = 0$  when  $t < \frac{z}{c_L}$ , the time needed for acoustic waves to cover the distance  $z$ . At slightly larger times  $t = \frac{z}{c_L} + t'$  such that  $t' \ll \frac{z}{c_L}$ , the emitters with non-zero contribution to the integral of Eq. (4) are located in a spatial region such that

$$|a'| \leq \sqrt{(c_L t)^2 - z^2} = a'_{max}(z, t) \quad (5)$$

with  $a'_{max}(z, t) \ll z$ . The  $(a'^2 + z^2)^{\frac{1}{4}}$  denominator appearing in Eq. (4) can then be approximated as  $\sqrt{z}$ , while the oscillating function of  $a'$   $h\left(t - \frac{\sqrt{a'^2 + z^2}}{c_L}\right)$  can be approximated as  $h\left(t - \frac{z}{c_L} - \frac{a'^2}{2c_L z}\right)$ . Eq (4) then becomes

$$A(x, z, t) \approx \frac{e^{\left(-\frac{1}{\tau} + i\omega\right)t'}}{\sqrt{z}} \int_{-a'_{max}(z, t)}^{a'_{max}(z, t)} f(a' + x) e^{\left(\frac{1}{\tau} - i\omega\right)\frac{a'^2}{2c_L z}} da' \quad (6)$$

The  $f(a)$  density can be generally written as  $f(a) = \bar{f} + f_{fluct}(a)$ , with  $\bar{f}$  its average value. Separating the contributions of  $\bar{f}$  and  $f_{fluct}(a)$  in the integral of Eq. (6), and expressing the former one  $A_{film}$  (corresponding to a constant emitter density, as e.g. in the thin film case) as a function of the sole  $t' = t - \frac{z}{c_L}$  variable using the *Erf* error function, Eq. (6) can be rewritten as

$$A(x, z, t) \approx A_{film}(t') + \frac{e^{\left(-\frac{1}{\tau} + i\omega\right)t'}}{\sqrt{z}} \int_{-a'_{max}(z, t)}^{a'_{max}(z, t)} f_{fluct}(a' + x) e^{\left(\frac{1}{\tau} - i\omega\right)\frac{a'^2}{2c_L z}} da' \quad (7)$$

with

$$A_{film}(t') = \bar{f} \sqrt{\frac{2\pi c_L}{\frac{1}{\tau} - i\omega}} \text{Erf} \left( i \sqrt{\left(\frac{1}{\tau} - i\omega\right)t'} \right) e^{\left(-\frac{1}{\tau} + i\omega\right)t'} \quad (8)$$

The integral appearing in Eq. (7) represents the perturbation of the spatio-temporal profile of the emitted wave induced by an inhomogeneous emitter density (non-zero  $f_{fluct}$ ), as compared to the case of a homogeneous one of same average density  $\bar{f}$ . Its integrand is a product of a function of zero average value ( $f_{fluct}(a)$ ) and of an oscillatory function of  $a$  ( $e^{\left(\frac{1}{\tau} - i\omega\right)\frac{a^2}{2c_L z}}$ ). Its value is thus expected to strongly depend on the characteristic distance  $d_f$  over which the  $f$  function fluctuates, and to become much smaller than  $A_{film}$  when  $d_f$  is much smaller than the characteristic fluctuation distance of  $e^{\frac{-i\omega a^2}{2c_L z}}$  (as can be seen by decomposing then the integral of Eq. (7) as a sum of integrals on intervals small enough for the oscillating function to remain approximately constant, but large enough for the average value of  $f_{fluct}$  on the interval to approach its 0 overall average value). This exponential has a local wavelength  $\lambda' = 2\pi \frac{c_L z}{\omega a^2}$ . Since  $|a'| \leq a'_{max} \cong \sqrt{2zc_L t'}$ ,  $\lambda'$  obeys  $\lambda' \geq \lambda \sqrt{\frac{2z}{c_L t'}}$ , where  $\lambda$  is the acoustic wavelength. The  $d_f \ll \lambda'$  condition is thus always fulfilled at the front of the emitted pulse, as  $\lambda' \rightarrow \infty$  when  $t' \rightarrow 0$ . A general criterion for the whole emitted acoustic pulse to resemble that emitted by a homogeneous transducer can be obtained by replacing  $t'$  by the duration of the emitted pulse  $\tau$ , leading to

$$d_f \ll \lambda \sqrt{\frac{2z}{c_L \tau}} \quad (9)$$

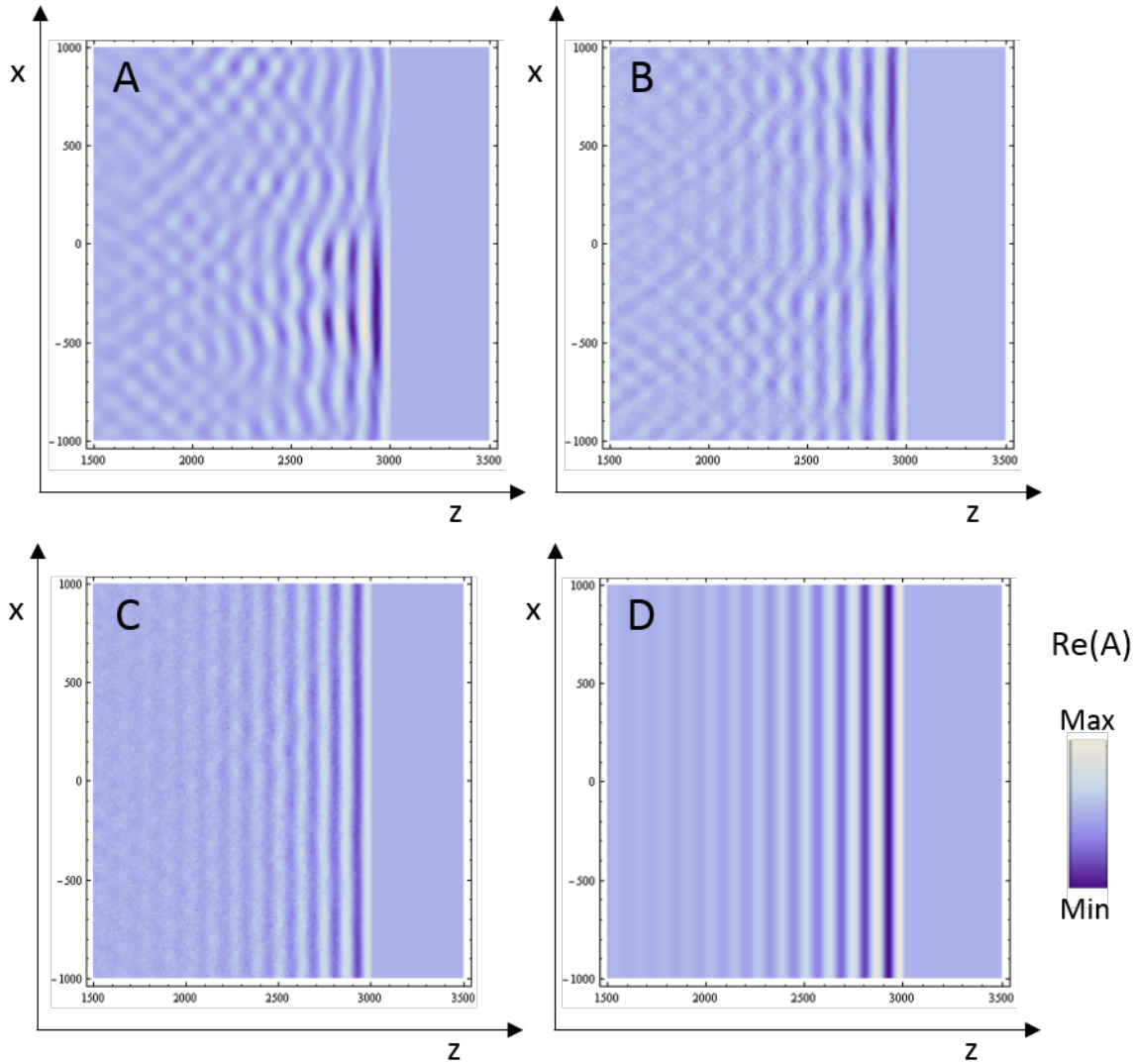
In our experiments,  $c_L$  is about 6000 m/s, and the  $f=40-50$  GHz detected acoustic frequencies correspond to  $\lambda = \frac{c_L}{f}$  acoustic wavelengths in the 120-150 nm range. As the acoustic quality factors of substrate-supported nano-objects  $Q = \pi f \tau$  is typically of the order of 10,  $\tau$  is estimated to be of the order of 100 ps for an acoustic source emitting at 50 GHz. Thus, after propagation on distance of a few  $\mu\text{m}$ , the  $\sqrt{\frac{2z}{c_L \tau}}$  factor has a value of a few units ( $\approx 5$  for  $z=6 \mu\text{m}$ ).

Numerical simulations of the waves produced by emitters with inhomogeneous density, based on Eq. (4) are presented in Figure 5. An emitter chain extending over 10  $\mu\text{m}$  was considered in these simulations (a finite emitter chain being required for numerically estimating the integral of Eq. (4) with random  $f$  values). Several random functions with the same average values but differing by the  $d_f$  characteristic distance over which they fluctuate were used for  $f$ . This was practically done by considering functions with independent and equiprobable random values of 0 and D over successive  $d_f$  intervals ( $d_f$  values of 1, 10 and 100 nm being considered in Figure 5). The results of these simulations confirm and illustrate the conclusions

of the analytical analyses presented above. Indeed, they show that the emitted waves resemble more and more those emitted by a homogeneous transducer (shown in Figure 5D) as  $d_f$  is decreased, and that this similarity is strong when the criterion of Eq. (9) is fulfilled, which is the case when  $d_f=1$  nm or 10 nm (Figure 5B-C).

For the actual samples used in this study,  $d_f$  can be roughly estimated as the average interparticle distance in the sample, whose value is of the order of less than 10 nm for all samples. The criterion of Eq. (9) is thus satisfied, as  $d_f$  is more than 10 times smaller than  $\lambda \sqrt{\frac{2z}{c_L \tau}}$  for acoustic propagation over distances of a few microns, which is consistent with the successful experimental detection of Brillouin oscillations for all samples. Eq. (8), which shows that the amplitude of the emitted wave scales as the average emitter density, also partly explains the strongly reduced amplitude of these Brillouin oscillations for the laser-processed sample, whose filling factor is much lower than that of the other samples. Such explanation is however only partial, as the amplitude of the measured optical signals is also expected to depend on the frequency content of the emitted acoustic wave-packets, which may be very different for the laser-processed sample as compared to other ones.





**Figure 5.** Numerical simulations of the waves generated by an inhomogeneous chain of emitters. Calculations were based on the model described in the main text (Eq. (4)), considering a  $10\ \mu\text{m}$  long chain of emitters. Emitter densities with randomly chosen, equiprobable 0 or  $D$  values every  $d_f=100\ \text{nm}$  (A),  $10\ \text{nm}$  (B) and  $1\ \text{nm}$  (C) intervals (and thus with same average value  $D/2$ ) were considered in these calculations. The case of an emitter chain with homogeneous  $D/2$  density is also shown for comparison (D). A  $c_L=6000\ \text{m/s}$  sound velocity was used, and calculations were done for  $t=0.5\ \text{ns}$  time.

## Conclusion

Ultrafast laser excitation of a layer of randomly located plasmonic nanoparticles with broad size dispersion (diameter varying from few to few tens of nm) was shown to enable the generation of a coherent acoustic pulse in its supporting N-BK7 glass substrate for all the samples tested. However, the coherent pulse generation efficiency was seen to dramatically reduce following laser reshaping of the nanoparticle layer, the pulse propagation then becoming detectable exclusively in a narrow probe spectral range where the photoelastic coupling between the photons and the acoustic phonons is the highest. The reduced pulse emission efficiency was attributed to the considerably lower nanoparticle filling factor after laser processing. The previous experimental observations were found to be qualitatively consistent with a simplified model of wave emission by an ensemble of emitters with non-uniform spatial density, showing in particular at which condition the effect of a non-uniform emitter density becomes negligible. The pulse propagation in N-BK7 was detected as GHz oscillations in transmission time-resolved measurements. The frequency of these Brillouin oscillations depends on the material properties, such as the local refractive index and the speed of sound, at a given probe wavelength, thereby this method could be suitable in microscopic applications for depth-profiling of different materials. Additionally, tuning the nanoparticles' shape properties and size distribution affects the spectral content of the acoustic pulse. The attenuation rates of the 40-50 GHz Fourier frequency components of the coherent acoustic pulses were determined, revealing their acoustic propagation over several micrometers in N-BK7, with attenuation rates very close to that previously measured on chemically pure silica and thus also dominated by anharmonic interactions with the thermal phonon bath. The similarity is attributed to the high proportion of silica in N-BK7 composition.

## Acknowledgement

The authors thank David Troadec from IEMN (France) for the preparation of the FIB lamella.

## Supplementary Information

The details about the laser-induced nanoparticle reshaping experiment, the sample preparation and characterization methods, the dielectric function of N-BK7 glass and its photon energy derivative, and the transmittance spectra of the samples are provided.

## REFERENCES

- (1) Gusev, V. E.; Ruello, P. Advances in Applications of Time-Domain Brillouin Scattering for Nanoscale Imaging. *Appl. Phys. Rev.* **2018**, *5*(3), 031101.
- (2) Morath, C. J.; Maris, H. J. Phonon Attenuation in Amorphous Solids Studied by Picosecond Ultrasonics. **1996**, *54*(1), 203–213.
- (3) Vacher, R.; Courtens, E.; Foret, M. Anharmonic versus Relaxational Sound Damping in Glasses. II. Vitreous Silica. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2005**, *72*(21), 1–11.
- (4) Fabian, J.; Allen, P. B. Theory of Sound Attenuation in Glasses: The Role of Thermal Vibrations. *Phys. Rev. Lett.* **1999**, *82*(7), 1478–1481.
- (5) Zhu, T. C.; Maris, H. J.; Tauc, J. Attenuation of Longitudinal-Acoustic Phonons in Amorphous SiO<sub>2</sub> at Frequencies up to 440 GHz. *Phys. Rev. B* **1991**, *44*(9), 4281–4289.
- (6) Klieber, C.; Peronne, E.; Katayama, K.; Choi, J.; Yamaguchi, M.; Pezeril, T.; Nelson, K. A. Narrow-Band Acoustic Attenuation Measurements in Vitreous Silica at Frequencies between 20 and 400 GHz. *Appl. Phys. Lett.* **2011**, *98*(21), 211908.
- (7) Lin, K. H.; Lai, C. M.; Pan, C. C.; Chyi, J. I.; Shi, J. W.; Sun, S. Z.; Chang, C. F.; Sun, C. K. Spatial Manipulation of Nanoacoustic Waves with Nanoscale Spot Sizes. *Nat. Nanotechnol.* **2007**, *2*(11), 704–708.
- (8) Ostovar, B.; Su, M. N.; Renard, D.; Clark, B. D.; Dongare, P. D.; Dutta, C.; Gross, N.; Sader, J. E.; Landes, C. F.; Chang, W. S.; Halas, N. J.; Link, S. Acoustic Vibrations of Al Nanocrystals: Size, Shape, and Crystallinity Revealed by Single-Particle Transient Extinction Spectroscopy. *J. Phys. Chem. A* **2020**, *124*(19), 3924–3934.
- (9) Marty, R.; Arbouet, A.; Girard, C.; Mlayah, A.; Paillard, V.; Lin, V. K.; Teo, S. L.;

- Tripathy, S. Damping of the Acoustic Vibrations of Individual Gold Nanoparticles. *Nano Lett.* **2011**, *11* (8), 3301–3306.
- (10) Staleva, H.; Hartland, G. V. Transient Absorption Studies of Single Silver Nanocubes. *J. Phys. Chem. C* **2008**, *112* (20), 7535–7539.
- (11) Burgin, J.; Langot, P.; Del Fatti, N.; Vallée, F.; Huang, W.; El-Sayed, M. A. Time-Resolved Investigation of the Acoustic Vibration of a Single Gold Nanoprism Pair. *J. Phys. Chem. C* **2008**, *112* (30), 11231–11235.
- (12) Ruijgrok, P. V.; Zijlstra, P.; Tchebotareva, A. L.; Orrit, M. Damping of Acoustic Vibrations of Single Gold Nanoparticles Optically Trapped in Water. *Nano Lett.* **2012**, *12* (2), 1063–1069.
- (13) Crut, A.; Maioli, P.; Del Fatti, N.; Vallée, F. Optical Absorption and Scattering Spectroscopies of Single Nano-Objects. *Chem Soc Rev* **2014**, *43*, 3921–3956.
- (14) Zijlstra, P.; Tchebotareva, A. L.; Chon, J. W. M.; Gu, M.; Orrit, M. Acoustic Oscillations and Elastic Moduli of Single Gold Nanorods. **2008**, *8* (10), 3493–3497.
- (15) Crut, A.; Maioli, P.; Del Fatti, N.; Vallée, F. Acoustic Vibrations of Metal Nano-Objects: Time-Domain Investigations. *Phys. Rep.* **2015**, *549*, 1–43.
- (16) Guillet, Y.; Rossignol, C.; Audoin, B.; Calbris, G.; Ravaine, S. Optoacoustic Response of a Single Submicronic Gold Particle Revealed by the Picosecond Ultrasonics Technique. *Appl. Phys. Lett.* **2009**, *95* (6), 061909.
- (17) Amziane, A.; Belliard, L.; Decremps, F.; Perrin, B. Ultrafast Acoustic Resonance Spectroscopy of Gold Nanostructures: Towards a Generation of Tunable Transverse Waves. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2011**, *83* (1), 1–7.
- (18) Yu, K.; Devkota, T.; Beane, G.; Wang, G. P.; Hartland, G. V. Brillouin Oscillations from Single Au Nanoplate Opto-Acoustic Transducers. *ACS Nano* **2017**, *11* (8), 8064–8071.
- (19) Jean, C.; Belliard, L.; Cornelius, T. W.; Thomas, O.; Pennec, Y.; Cassinelli, M.; Toimil-Molares, M. E.; Perrin, B. Spatiotemporal Imaging of the Acoustic Field Emitted by a Single Copper Nanowire. *Nano Lett.* **2016**, *16* (10), 6592–6598.
- (20) Xu, F.; Guillet, Y.; Ravaine, S.; Audoin, B. All-Optical in-Depth Detection of the

- Acoustic Wave Emitted by a Single Gold Nanorod. *Phys. Rev. B* **2018**, *97*(16), 1–7.
- (21) Berte, R.; Della Picca, F.; Poblet, M.; Li, Y.; Cortés, E.; Craster, R. V.; Maier, S. A.; Bragas, A. V. Acoustic Far-Field Hypersonic Surface Wave Detection with Single Plasmonic Nanoantennas. *Phys. Rev. Lett.* **2018**, *121* (25), 1–6.
- (22) Yajadda, M. M. A.; Levchenko, I.; Ostrikov, K. Gold Nanoresistors with Near-Constant Resistivity in the Cryogenic-to-Room Temperature Range Gold Nanoresistors with near-Constant Resistivity in the Cryogenic-to-Room Temperature Range. *J. Appl. Phys.* **2011**, *110*(2), 023303.
- (23) Mirigliano, M.; Milani, P. Advances in Physics: X Electrical Conduction in Nanogranular Cluster- Assembled Metallic Films. *Adv. Phys. X* **2021**, *6*(1), 1908847.
- (24) Lee, S.; Shin, M.; Hwang, S.; Jang, J. Unconventional but Tunable Phase Transition above the Percolation Threshold by Two-Layer Conduction in Electroless-Deposited Au Nanofeatures on Silicon Substrate. *Nanotechnology* **2015**, *26* (50), 505202.
- (25) Šubr, M.; Petr, M.; Kylián, O.; Kratochvíl, J.; Procházka, J. Large-Scale Ag Nanoislands Stabilized by a Magnetron-Sputtered Polytetrafluoroethylene Film as Substrates for Highly Sensitive and Reproducible Surface-Enhanced Raman Scattering (SERS). *J. Mater. Chem. C* **2015**, *3*(43), 11478–11485.
- (26) Chung, T.; Lee, Y.; Ahn, M.-S.; Lee, W.; Bae, S.-I.; Soon, C.; Hwang, H.; Jeong, K.-H. Nanoislands as Plasmonic Materials. *Nanoscale* **2019**, *11* (18), 8651–8664.
- (27) Grant, C. D.; Schwartzberg, A. M.; Norman, T. J.; Zhang, J. Z. Ultrafast Electronic Relaxation and Coherent Vibrational Oscillation of Strongly Coupled Gold Nanoparticle Aggregates. *J. Am. Chem. Soc.* **2003**, *125* (2), 549–553.
- (28) Qian, W.; Lin, L.; Deng, Y. J.; Xia, Z. J.; Zou, Y. H.; Wong, G. K. L. Femtosecond Studies of Coherent Acoustic Phonons in Gold Nanoparticles Embedded in TiO<sub>2</sub> Thin Films. *J. Appl. Phys.* **2000**, *87*(1), 612–614.
- (29) Nelet, A.; Crut, A.; Arbouet, A.; Del Fatti, N.; Vallée, F.; Portalès, H.; Saviot, L.; Duval, E. Acoustic Vibrations of Metal Nanoparticles: High Order Radial Mode Detection. *Appl. Surf. Sci.* **2004**, *226*(1-3 SPEC. ISS.), 209–215.
- (30) Burgin, J.; Langot, P.; Arbouet, A.; Margueritat, J.; Gonzalo, J.; Afonso, C. N.; Vallée, F.;

- Mlayah, A.; Rossell, M. D.; Van Tendeloo, G. Acoustic Vibration Modes and Electron-Lattice Coupling in Self-Assembled Silver Nanocolumns. *Nano Lett.* **2008**, *8* (5), 1296–1302.
- (31) Jais, P. M.; Murray, D. B.; Merlin, R.; Bragas, A. V. Metal Nanoparticle Ensembles: Tunable Laser Pulses Distinguish Monomer from Dimer Vibrations. *Nano Lett.* **2011**, *11* (9), 3685–3689.
- (32) Petrova, H.; Lin, C. H.; De Liejer, S.; Hu, M.; McLellan, J. M.; Siekkinen, A. R.; Wiley, B. J.; Marquez, M.; Xia, Y.; Sader, J. E.; Hartland, G. V. Time-Resolved Spectroscopy of Silver Nanocubes: Observation and Assignment of Coherently Excited Vibrational Modes. *J. Chem. Phys.* **2007**, *126* (9), 1–9.
- (33) Huang, W.; Qian, W.; El-Sayed, M. A. The Optically Detected Coherent Lattice Oscillations in Silver and Gold Monolayer Periodic Nanoprism Arrays: The Effect of Interparticle Coupling. *J. Phys. Chem. B* **2005**, *109* (40), 18881–18888.
- (34) Wang, L.; Nishijima, Y.; Ueno, K.; Misawa, H.; Tamai, N. Effect of Dipole Coupling on Near-IR LSPR and Coherent Phonon Vibration of Periodic Gold Pair Nanocuboids. *J. Phys. Chem. C* **2012**, *116* (33), 17838–17846.
- (35) Huang, W.; Qian, W.; El-Sayed, M. A. Coherent Vibrational Oscillation in Gold Prismatic Monolayer Periodic Nanoparticle Arrays. *Nano Lett.* **2004**, *4* (9), 1741–1747.
- (36) Ayriñac, S.; Foret, M.; Devos, A.; Rufflé, B.; Courtens, E.; Vacher, R. Subterahertz Hypersound Attenuation in Silica Glass Studied via Picosecond Acoustics. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2011**, *83* (1), 1–13.
- (37) Mott, N. F.; Davis, E. F. *Electronic Processes in Non-Crystalline Materials*; Clarendon Press, 1979.
- (38) Wang, J.; Guo, C. Long-Lived Coherent Traveling Acoustic Pulses Induced by Femtosecond Laser Pulses. *Solid State Commun.* **2007**, *144* (5–6), 198–201.
- (39) Ishioka, K.; Rustagi, A.; Höfer, U.; Petek, H.; Stanton, C. J. Intrinsic Coherent Acoustic Phonons in the Indirect Band Gap Semiconductors Si and GaP. *Phys. Rev. B* **2017**, *95* (3), 1–9.
- (40) Baydin, A.; Gatamov, R.; Krzyzanowska, H.; Stanton, C. J.; Tolk, N. Energy-Dependent

Amplitude of Brillouin Oscillations in GaP. *Phys. Rev. B* **2019**, *99*(16), 165202.

- (41) Lin, H. N.; Stoner, R. J.; Maris, H. J.; Tauc, J. Phonon Attenuation and Velocity Measurements in Transparent Materials by Picosecond Acoustic Interferometry. *J. Appl. Phys.* **1991**, *69*(7), 3816–3822.
- (42) Baldi, G.; Benassi, P.; Bove, L. E.; Caponi, S.; Fabiani, E.; Fioretto, D. Dynamic-to-Static Crossover in the Acoustic Attenuation of  $\nu$ -GeO<sub>2</sub>. *EPL (Europhysics Lett.)* **2007**, *78*(3), 36001.
- (43) Rufflé, B.; Foret, M.; Courtens, E.; Vacher, R.; Monaco, G. Observation of the Onset of Strong Scattering on High Frequency Acoustic Phonons in Densified Silica Glass. *Phys. Rev. Lett.* **2003**, *90*(9), 4.
- (44) Rufflé, B.; Guimbretiére, G.; Courtens, E.; Vacher, R.; Monaco, G. Glass-Specific Behavior in the Damping of Acousticlike Vibrations. *Phys. Rev. Lett.* **2006**, *96*(4), 1–4.
- (45) Masciovecchio, C.; Baldi, G.; Caponi, S.; Comez, L.; Fonzo, S. Di; Fioretto, D.; Fontana, A.; Gessini, A.; Santucci, S. C.; Sette, F.; Viliiani, G.; Vilmercati, P.; Ruocco, G. Evidence for a Crossover in the Frequency Dependence of the Acoustic Attenuation in Vitreous Silica. *Phys. Rev. Lett.* **2006**, *035501*, 035501.
- (46) Vacher, R.; Ayrinhac, S.; Foret, M.; Rufflé, B.; Courtens, E. Finite Size Effects in Brillouin Scattering from Silica Glass. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2006**, *74*(1), 1–4.
- (47) Benassi, P.; Caponi, S.; Eramo, R.; Fontana, A.; Giugni, A.; Nardone, M.; Sampoli, M.; Viliiani, G. Sound Attenuation in a Unexplored Frequency Region: Brillouin Ultraviolet Light Scattering Measurements in  $\nu$ -SiO<sub>2</sub>. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2005**, *71*(17), 5–8.
- (48) Masciovecchio, C.; Gessini, A.; Di Fonzo, S.; Comez, L.; Santucci, S. C.; Fioretto, D. Inelastic Ultraviolet Scattering from High Frequency Acoustic Modes in Glasses. *Phys. Rev. Lett.* **2004**, *92*(24), 18–21.
- (49) Devos, A.; Foret, M.; Ayrinhac, S.; Emery, P.; Rufflé, B. Hypersound Damping in Vitreous Silica Measured by Picosecond Acoustics. *Phys. Rev. B - Condens. Matter Mater. Phys.* **2008**, *77*(10), 1–4.

- (50) Ferrante, C.; Pontecorvo, E.; Cerullo, G.; Chiasera, A.; Ruocco, G.; Schirmacher, W.; Scopigno, T. Acoustic Dynamics of Network-Forming Glasses at Mesoscopic Wavelengths. *Nat. Commun.* **2013**, *4*, 1793–1796.
- (51) Pontecorvo, E.; Ortolani, M.; Polli, D.; Ferretti, M.; Ruocco, G.; Cerullo, G.; Scopigno, T. Visualizing Coherent Phonon Propagation in the 100 GHz Range: A Broadband Picosecond Acoustics Approach. *Appl. Phys. Lett.* **2011**, *98*(1).
- (52) Jäckle, J.; Piché, L.; Arnold, W.; Hunklinger, S. Elastic Effects of Structural Relaxation in Glasses at Low Temperatures. *J. Non. Cryst. Solids* **1976**, *20*(3), 365–391.
- (53) Gilkoy, K. S.; Phillips, W. A. An Asymmetric Double-Well Potential Model for Structural Relaxation Processes in Amorphous Materials. *Philos. Mag. B Phys. Condens. Matter; Stat. Mech. Electron. Opt. Magn. Prop.* **1981**, *43*(5), 735–746.
- (54) Buchenau, U.; Galperin, Y. M.; Gurevich, V. L.; Parshin, D. A.; Ramos, M. A.; Schober, H. R. Interaction of Soft Modes and Sound Waves in Glasses. *Phys. Rev. B* **1992**, *46*(5), 2798–2808.
- (55) Baldi, G.; Giordano, V. M.; Monaco, G.; Ruta, B. Sound Attenuation at Terahertz Frequencies and the Boson Peak of Vitreous Silica. *Phys. Rev. Lett.* **2010**, *104*(19), 1–4.
- (56) Wen, Y. C.; Guol, S. H.; Chen, H. P.; Sheu, J. K.; Sun, C. K. Femtosecond Ultrasonic Spectroscopy Using a Piezoelectric Nanolayer: Hypersound Attenuation in Vitreous Silica Films. *Appl. Phys. Lett.* **2011**, *99*(5), 1–4.