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Role of cilia activity and surrounding viscous fluid in properties of metachronal wavesSupravat Dey **Department of Physics and Department Computer Science and Engineering, SRM University-AP, Amaravati, Andhra Pradesh 522240, India*Gladys Massiera[†] and Estelle Pitard [‡]*Laboratoire Charles Coulomb (L2C), Université de Montpellier, CNRS, 34095 Montpellier, France*

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Large groups of active cilia collectively beat in a fluid medium as metachronal waves, essential for some microorganisms motility and for flow generation in mucociliary clearance. Several models can predict the emergence of metachronal waves, but what controls the properties of metachronal waves is still unclear. Here, we numerically investigate the respective impacts of active beating and viscous dissipation on the properties of metachronal waves in a collection of oscillators, using a simple model for cilia in the presence of noise on regular lattices in one and two dimensions. We characterize the wave using spatial correlation and the frequency of collective beating. Our results clearly show that the viscosity of the fluid medium does not affect the wavelength; the activity of the cilia does. These numerical results are supported by a dimensional analysis, which shows that the result of wavelength invariance is robust against the model taken for sustained beating and the structure of hydrodynamic coupling. Interestingly, the enhancement of cilia activity increases the wavelength and decreases the beating frequency, keeping the wave velocity almost unchanged. These results might have significance in understanding paramecium locomotion and mucociliary clearance diseases.

DOI: [10.1103/PhysRevE.110.014409](https://doi.org/10.1103/PhysRevE.110.014409)**I. INTRODUCTION**

The emergence of phase-traveling waves in dense arrays of active beating cilia, known as metachronal waves, is a complex multiscale physics problem [1–7] and is nonequilibrium because of the internal activity-driven movements of cilia. The active beating of each cilium arises from the sliding of microtubules by thousands of molecular motors and the subsequent interaction with the surrounding fluid medium. The coupling of a large number of these oscillators lead to synchronized dynamics over larger lengthscales. Illustrations are abundant in nature with ciliary living systems differing by cilia assembly geometry, cilia activity, or the properties of the surrounding fluid. In respiratory tissues, the continuous cleaning of our lungs is provided by cilia beating waves that generate mucus flow [8,9]. For certain microorganisms such as paramecium, synchronized beating of cilia help in their efficient locomotion [10]. The complexity of a cilia active beating pattern and their interaction with each other through a complex environment makes it difficult to predict the emergent wave properties, despite recent theoretical and experimental advancements.

Models of cilia arrays [11–15] aim to identify the conditions required for such a coordinated state and to comprehend the physical parameters that govern the properties of the metachronal wave and the subsequent mucus transport. Several models have been proposed [11–13,16,17], wherein the coupling was primarily described as a viscous hydrodynamic

coupling. In these models, different types of active forces, from simple to complex, successfully generated continuous beating of a cilium. Numerical simulations enabled the investigation of the intricate structure of cilia by considering their beating as a filament bending wave [12,18,19]. Another approach was to model cilia by actuated micron-sized beads called rotors [20–23] or rowers [11,24,25]. For a large group of cilia arranged in an array, it was shown that hydrodynamic coupling can lead to metachronal waves for various models of cilia [12,14,15]. Recently, the influence, on these collective behaviors, of several physical parameters such as noise [25,26], and disorder in the arrangement and orientation of cilia was investigated both numerically [25,27,28] and experimentally [28,29], showing that spatial heterogeneity favors transport. Other important physical quantities that may play a role on the coordination are the activity related to the sustained beating and the dissipation in the viscous fluid that will have opposite impacts on the metachronal waves emerging from cilia beating. Experimentally, a decrease in beating frequency with viscosity was found [30,31], whereas the beating amplitude and the metachronal wavelength were found constant up to ≈ 50 times the viscosity of water [32,33]. Theoretically, the mutual influence of activity and dissipation were almost not explored [34]. Here, our fundamental inquiry pertains to the interplay between cilia beating characteristics and the fluid medium and its impact on the overall properties of metachronal waves.

II. ROWER MODEL

We study the metachronal waves in the rower model of cilia in viscous fluid for one- and two-dimensional regular lattices in the presence of thermal noise. In the rower

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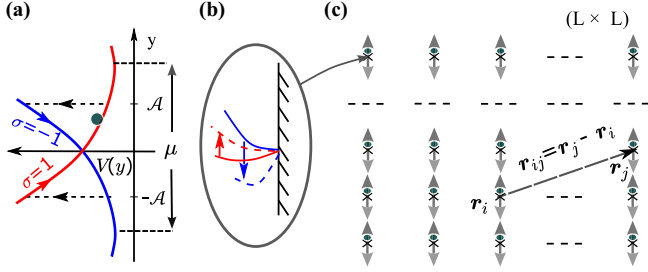


FIG. 1. Rower model of cilia [11]. (a) The motion of a micron-sized bead in a viscous medium under two harmonic potential branches, corresponding to $\sigma \pm 1$, represents the stroke and antistroke beating of a cilium. (b) The bead switches branches when it reaches terminal position $y = \pm \mathcal{A}$. (c) Rowers are arranged in two dimensions on a $L \times L$ square lattice, with their beating direction along the y axis, as indicated by the double arrow. Hydrodynamic interaction between rowers i and j is modeled by the Oseen coupling, which is dependent on the \mathbf{r}_{ij} vector.

model [11,24,25], the complex active beating of a cilium is simplified into the back and forth motion along an axis of a micron-sized bead immersed in a viscous fluid, thus ensuring a low Reynolds number regime. Such an oscillating motion is driven by two harmonic potential branches, corresponding to the stroke and antistroke of the cilia beating, with a geometric switching mechanism. The bead moves downhill of a potential until it reaches one of the two terminal positions for which switching to the second branch occurs [Figs. 1(a) and 1(b)]. This switching is like pumping energy to lift the bead on the upper side of the other potential at the terminal. At a given time, the bead can be found in one of these two states, the stroke and antistroke of the cilia beating, represented by a discrete $\sigma = \pm 1$. The driving force for a bead displacement y for a given σ can be written as

$$f(y, \sigma) = -\frac{dV(y, \sigma)}{dy} = -k(y - \sigma\mu/2), \quad (1)$$

where k is the force constant associated with the harmonic potentials, μ is the distance between minima of two potentials, and \mathcal{A} is the beating amplitude. The supply of energies during each downhill motion in a harmonic potential $k\mathcal{A}^2/2$, and during each switch the pumping energy $k\mu\mathcal{A}$, keep the bead oscillating in the dissipating media. We refer to this pumping energy during each switch as “activity” for the rower model of cilia. Therefore, for a given μ , the “activity” of the bead depends on values of k and \mathcal{A} . Because of its simplicity and ability to capture the two-stroke beating of cilia, the rower model has become a method of choice for theoretical and experimental studies of synchronization in ciliary systems [15,29].

We consider a system of N rowers beating in the y direction in a viscous medium. Rowers are placed regularly in one or two dimensions (square) lattices [see Fig. 1(c)] at fixed positions \mathbf{r}_i (for $i = \{1, 2, 3, \dots, N\}$). The displacement y_i of a rower i is hydrodynamically coupled with the others and is given by

$$\frac{dy_i}{dt} = \frac{f_i}{\gamma} + \sum_{j \neq i} O(i, j) f_j + \xi_i, \quad (2)$$

where $\gamma = 6\pi\eta a$ is the viscous drag coefficient for a bead with radius a and $O(i, j)$ the coupling strength between rowers i and j . In the far-field hydrodynamic coupling approximation, for which both the distance from the surface and the distance between two adjacent rowers (lattice spacing ℓ) are large compared to a , $O(i, j)$ is set by the Oseen tensor $O(i, j) = \frac{1}{8\pi\eta r_{ij}}(1 + (\frac{y_{ij}}{r_{ij}})^2)$, with $i \neq j$, and $\mathbf{r}_{ij} = \mathbf{r}_j - \mathbf{r}_i$ the separation vector between rowers i and j . The last term is due to the thermal noise, obeying the following delta correlation: $\langle \xi(t) \rangle = 0$, $\langle \xi(t_1)\xi(t_2) \rangle = 2D\delta(t_1 - t_2)$. For simplicity, we assume no correlation between the noise acting on each of the rowers as in [25]. The noise strength or diffusivity is equal to $D = k_B T/\gamma$, with k_B and T being the Boltzmann constant and the temperature. The displacement of a single isolated bead shows sustained oscillations with the frequency $\nu_0 = 1/(2\tau_d \log[(\mu + 2\mathcal{A})/(\mu - 2\mathcal{A})])$, where $\tau_d = \gamma/k$ is the relaxation time for the bead to reach equilibrium in a harmonic potential [24]. Two such coupled rowers beat collectively with antiphase synchronization [11]. For many rowers, the interplay between the activity of the rowers and the coupling through the medium generates metachronal waves [11].

III. NUMERICAL RESULTS

The Euler method with an integration step equal to $5 \times 10^{-3}s$ is used to evolve the coupled dynamical equation [Eq. (2)], starting from random initial values for $\{\sigma_i, y_i\}$. The open boundary condition is implemented. Parameters are chosen within the experimentally relevant range [24,35] $a = 1.5 \mu\text{m}$, $\ell = 8 \mu\text{m}$, $k = 2.6 \text{ pN } \mu\text{m}^{-1}$, $\mu = 2 \mu\text{m}$, $\mathcal{A} = 0.56\text{--}0.8 \mu\text{m}$, $\eta = 2\text{--}20 \text{ mPa s}$, and $T = 300 \text{ K}$. The results presented here are for large system sizes $N = L = 200$ (for one dimension) and $N = L^2 = 1600$ (for two dimensions). Comparing the results with smaller systems (not shown here), we confirm that the presented results have no system size dependence.

A. Characterization of metachronal waves

Figure 2 shows the metachronal waves on the one-dimensional lattice. The beads’ displacement against the rowers’ position for a given time displays two spatial waves that are visualized by connecting displacements y_i by lines for all rowers at the even and odd lattice sites separately [Fig. 2(a)] in agreement with [11,36]. This is a unique feature of the rower model and arises due to a degree of antiphase synchronization between two adjacent rowers. The wave propagation is illustrated in Fig. 2(c) by the kymograph obtained for $\sigma_i(t)$. To characterize it, we compute the spatial correlation function between two rowers as a function of their separation vector \mathbf{r} :

$$C(\mathbf{r}) = \frac{\sum_{ij} \langle \sigma_i(\mathbf{r}_i, t) \sigma_j(\mathbf{r}_j, t) \rangle \delta(\mathbf{r} - \mathbf{r}_{ij})}{\sum_{ij} \delta(\mathbf{r} - \mathbf{r}_{ij})}. \quad (3)$$

As the rowers are placed on a regular lattice with lattice spacing ℓ , the coordinates of \mathbf{r} are discrete and can be written as $(m\ell, n\ell)$ with $m, n \in \{0, 1, 2, \dots, L\}$. The measurement is done after a large equilibration time t_0 , where the system is assumed to reach a steady state. Brackets $\langle \cdot \rangle$ represent average over time and ensembles. An ensemble is the collection of

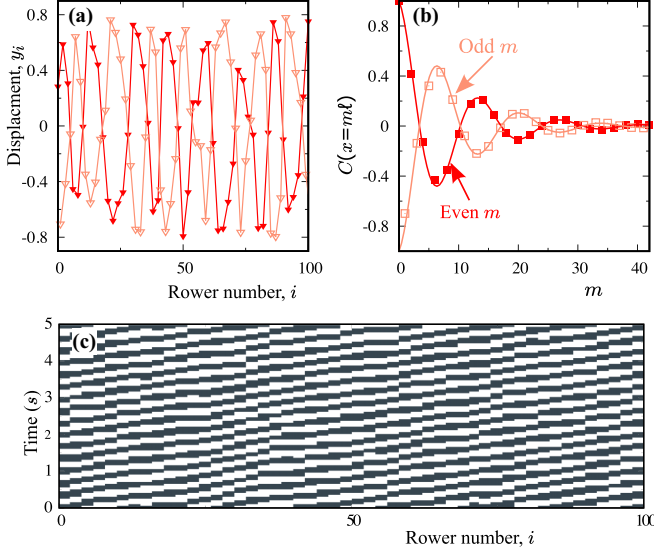


FIG. 2. Metachronal waves in one dimension. (a) Snapshot of displacements of the first 100 rowers. The displacement of even (odd) sites is plotted in light (dark) color. (b) Correlation function $C(x = m\ell)$ between two rowers is plotted against separation distance x . (c) Kymograph of the beating state σ , with white color (black) representing $\sigma=1$ ($\sigma = -1$). Parameters: $\mathcal{A} = 0.8$, $\eta = 6$ mPa s, and $N = 200$.

5000 sets of $\{\sigma_i(t)\}$ recorded every 2 seconds after $t_0 = 2500$ seconds. Depending on the system size, we consider several ensembles with random initial conditions. For one dimension ($N = 200$) the number of ensembles is 100 and for two dimensions ($N = 1600$) it lies between 5 to 10.

B. Wave properties in one dimension

Figure 2(b) shows the variation of $C(x) = C(x, y = 0)$ in one dimension. For odd and even m values, two oscillating curves decay to zero as the distance between rowers $x = m\ell$ increases. While the oscillations indicate the wave nature of the collective beating, the loss of correlations at larger x suggest a damping in the coordination on a characteristic lengthscale l_d . $C(x)$ can be fitted with the simple function $\pm e^{-x/l_d} \cos(2\pi x/\lambda)$, the + (−) sign being for even (odd) m . This fit estimates the wavelength λ and decay length l_d . For Fig. 2, $\lambda \simeq 13.7\ell$ and $l_d \simeq 9.0\ell$. In a recent paper [37], the wavelength and decay length were measured experimentally for metachronal waves on the human bronchial epithelium, and these two lengthscale values are comparable. Our results are consistent with the experiment. The ensemble and spatial average of the beating frequency was computed as $\nu \simeq 3.4$ Hz and combined with λ to infer the metachronal wave velocity $V = \nu\lambda \simeq 370$ $\mu\text{m}/\text{s}$. This value corresponds to the value that can be estimated by measuring the slopes in the kymograph Fig. 2(c).

We then investigate the effect of viscosity of the fluid medium and activity of the cilia on the metachronal waves' quantities: λ , l_d , ν , and $V = \nu\lambda$, by computing $C(x)$ for various η and \mathcal{A} . The plot of $C(x)$ for different \mathcal{A} values shows that both λ and l_d increase with \mathcal{A} [Figs. 3(a) and 3(c)], whereas ν decreases with \mathcal{A} , keeping V almost constant

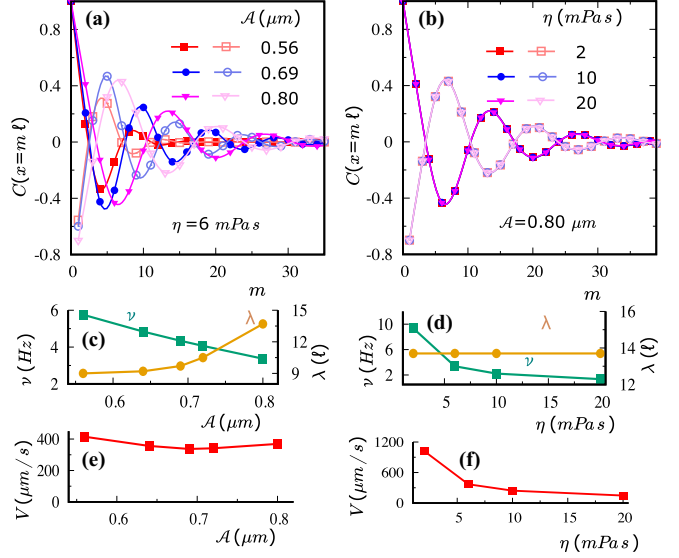


FIG. 3. Effect of viscosity and beating amplitude on metachronal waves in one dimension ($N = 200$). Correlation function $C(x = m\ell)$ as a function of the distance between rowers, (a) for three different \mathcal{A} values (for $\eta = 6$ mPa s) and (b) for three different η values (for $\mathcal{A} = 0.8$ μm). The wavelengths λ are plotted against (c) \mathcal{A} and (d) η , together with the corresponding beating frequency ν . Propagation velocity V is plotted against (e) \mathcal{A} and (f) η . In (b), the different symbols are not distinctively visible as the three curves completely overlap.

[Figs. 3(c) and 3(e)]. As ν_0 , the frequency of a rower decreases with \mathcal{A} , the decrease of ν is expected. Along the same lines, increasing \mathcal{A} , which is a characteristic length of the problem, may naturally increase the lengthscale of the emerging collective dynamics. Thus the respective variation of ν and λ can be generally expected. What is remarkable though is that they compensate to result in an almost constant wave velocity. Interestingly, $C(x)$ does not depend on the values of η [see Fig. 3(b)], meaning λ and l_d are independent of η and implying that the spatial behavior of emergent waves does not depend on the fluid viscosity and are only determined by cilia activity parameters, in agreement with experimental observations [30,33]. Finally, the frequency ν decreases as a function of η and so does V , as measured experimentally in [30,33].

C. Wave properties in two dimensions

On a square lattice, we find that the metachronal wave propagates along the beating direction y whereas no wave is obtained in the perpendicular direction (Fig. 5), suggesting longitudinal waves. In Figs. 4(a) and 4(b), we plot the correlation function along the y direction $C(0, y = n\ell)$ against n for various values of \mathcal{A} and η . Similar to the one-dimensional case, two spatial waves can be seen for even and odd values of n for a given parameter set. For a fixed η , λ increases and ν decreases with \mathcal{A} , keeping the wave velocity V almost constant [Figs. 4(c) and 4(e)]. On the contrary, λ remains constant and ν decreases with η , leading to a decrease in V with η [Figs. 4(d) and 4(f)]. We further note that, although the qualitative behavior of metachronal waves in one and

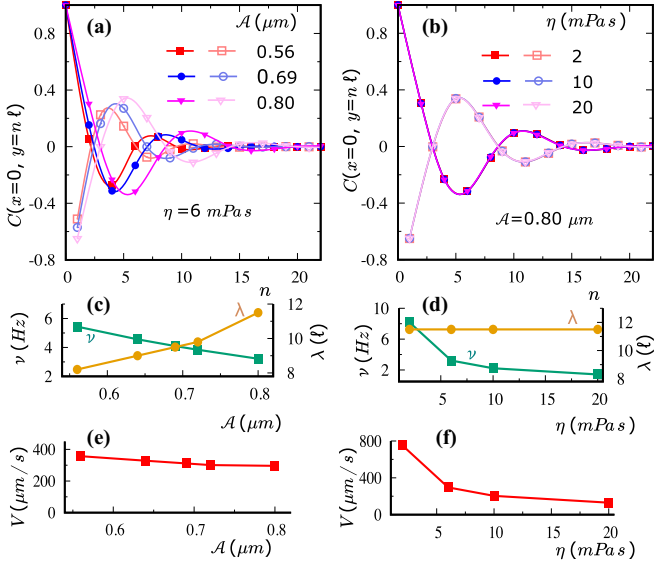


FIG. 4. Effect of viscosity and beating amplitude on metachronal waves in two dimensions ($N = L^2 = 1600$). Correlation function along beating direction $C(x = 0, y = n\ell)$ as a function of the distance between rowers, (a) for three different values of \mathcal{A} (for $\eta = 6$ mPa s) and (b) for three different η values (for $\mathcal{A} = 0.8$ μm). The wavelengths λ are plotted against (c) \mathcal{A} and (d) η , together with the corresponding beating frequency ν . Propagation velocity V is plotted as a function of (e) \mathcal{A} and (f) η . In (b), the different symbols are not distinctively visible as the three curves completely overlap.

two dimensions are similar, the values of λ and V are relatively larger in one dimension. This result raises interesting questions on the implications of the geometry of realistic ciliated tissues, which are mostly organized in two-dimensional groups of cilia bundles.

In the direction perpendicular to beating, no oscillation is obtained (Fig. 5). $C(x, 0)$ either monotonically decays to zero as for large \mathcal{A} or shows a negative correlation for small $y = m\ell$ with odd m that eventually approaches zero for large m . For a given \mathcal{A} , $C(x, 0)$ does not depend on η [Fig. 5(b)], although odd and even m can follow different curves, reminiscent of $C(0, y)$. We compare the decay lengths of correlations along the x and y directions $l_{d,x}$ and $l_{d,y}$. The decay length for the damped oscillations along y , $l_{d,y}$, can be estimated from the fitting method discussed above. The decay length $l_{d,x}$ is

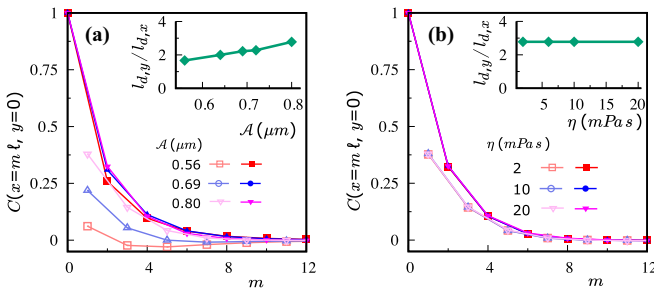


FIG. 5. Effect of viscosity and beating amplitude on correlations along the direction perpendicular to the beating direction $C(x = m\ell, y = 0)$. $C(x = m\ell, y = 0)$ is plotted for (a) three different \mathcal{A} for a fixed $\eta = 6$ mPa s, and (b) for three values of η for a given $\mathcal{A} = 0.69$ μm .

estimated from the exponential fit of the $C(x = m\ell, 0)$ for even m values. The ratio $l_{d,y}/l_{d,x}$ is plotted in the insets, one notes that $l_{d,y}/l_{d,x} \gtrsim 2$. For a fixed \mathcal{A} , it remains unchanged with η . However, for a given η , the ratio increases with cilia activity \mathcal{A} , which means an increased coordination along the beating direction compared the perpendicular one. This anisotropic response may be related to the anisotropy of the interaction strength. Indeed, considering the same r_{ij} value, $O(i, j)$ is two times larger along the y axis than along the x axis.

IV. WHY SPATIAL WAVE PROPERTIES ARE INDEPENDENT OF VISCOUS MEDIA

The fact that we obtain metachronal waves with spatial properties unaffected by viscosity has not been emphasized by previous studies, to our knowledge. Nevertheless, this remarkable numerical observation is robust on an order of magnitude of η and obtained with both one- and two-dimensional simulations. To rationalize this result, one needs to look into the details of characteristic length and timescales of the system set by the activity and the surrounding viscous medium. The relaxation time $\tau_d = 6\pi\eta a/k$ for the bead motion in the viscous medium under a harmonic driving potential, which also determines the natural frequency ν_0 , is a crucial timescale in our problem. In the rower model, there are two lengthscales, \mathcal{A} and μ (Fig. 1). Since we only vary \mathcal{A} , we chose it as the typical lengthscale. We note that our conclusion below, however, does not depend on the choice of the lengthscale. Multiplying both sides of Eq. (2) by τ_d/\mathcal{A} leads to an adimensional equation for the collective beating dynamics

$$\frac{dy'_i}{dt'} = f'_i + \sum_{i \neq j} \frac{3a}{4r_{ij}} (1 + (y_{ij}/r_{ij})^2) f'_j + \zeta_i(t'), \quad (4)$$

where t' and y' are dimensionless time $t' = t/\tau_d$ and displacement $y' = y/\mathcal{A}$. $f'_j = -(y'_j - \mu\sigma_j/2\mathcal{A})$ is the dimensionless force acting on rower j , and $\langle \zeta(t'_1)\zeta(t'_2) \rangle = 2k_B T / (k\mathcal{A}^2) \delta(t'_1 - t'_2)$ is the adimensional noise correlation. As activity parameters \mathcal{A} , k , and μ are constant, Eq. (4) is η independent. The latter means that the spatial properties are independent of η . However, as τ_d is affected by η , it impacts the dynamical properties of the system. If any parameter \mathcal{A} , k , and μ are influenced by the medium, then our observation will break down.

Above, we study the rower model, a minimal model for the active beating of cilia. The hydrodynamic interaction between cilia is implemented via Oseen coupling, assuming the beating amplitude is very small compared to intercellular distance and ignoring the surface effect and correlation in noise between two cilia. We also assume that cilia are arranged in particular ways in space and beat in a specific direction. Here, we argue that the invariance of spatial properties of metachronal waves in various viscous media is more general and not dependent on the model chosen for cilia beating, nor on the cilia mutual interaction in the viscous fluid, nor on the cilia spatial arrangement. Indeed, for a more realistic cilia model, one may choose a complex force profile for active beating having more parameters \mathbf{f}_i [15,19]. For the hydrodynamic coupling, the presence of the surface can be captured by the Blake

tensor in the far field limit [38]. At low Reynolds number, the hydrodynamic coupling tensor has the following properties: it has a multiplicative scalar factor that is inversely proportional to the drag coefficient γ and the tensorial part depends on the position of the active forces.

For a generic hydrodynamic coupling $G(\mathbf{r}_i, \mathbf{r}_j)$ and correlated noise between cilia, the equation of motion is given by

$$\frac{d\mathbf{r}_i}{dt} = \sum_{j=1}^N G(\mathbf{r}_i, \mathbf{r}_j)(\mathbf{f}_j + \mathbf{f}_j^r(t)), \quad (5)$$

where the random force (noise) \mathbf{f}_i^r obeys $\langle \mathbf{f}_i^r(t_1)\mathbf{f}_j^r(t_2) \rangle = 2k_B T G^{-1}(\mathbf{r}_i, \mathbf{r}_j)\delta(t_1 - t_2)$ [25,39,40]. As we discussed above, the coupling tensor can be written as $G(\mathbf{r}_i, \mathbf{r}_j) = \tilde{G}(\mathbf{r}_i, \mathbf{r}_j)/\gamma$, with \tilde{G} being dimensionless and independent of viscosity. We note that this result may not hold true for the viscoelastic or other complex fluids, which are beyond the scope of this paper. However, the above analysis is expected to hold true for complex models of cilia. As the motion of a cilium is localized around a fixed position, for realistic cilia, there may at least exist an effective force constant k^{eff} and a beating amplitude \mathcal{A}^{eff} . Therefore, the relevant lengthscale and timescale could be written as \mathcal{A}^{eff} and $\tau_d = \gamma/k^{\text{eff}}$, respectively. The important assumption here is that these activity parameters k^{eff} and \mathcal{A}^{eff} are independent of fluid viscosity. Now the dimensionless dynamical equation for cilia i is given by

$$\frac{d\mathbf{r}'_i}{dt'} = \sum_{j=1}^N \tilde{G}(\mathbf{r}_i, \mathbf{r}_j)(\mathbf{f}'_j + \mathbf{f}'_j{}^r(t')), \quad (6)$$

where $\mathbf{f}'_j = \mathbf{f}_j/(k^{\text{eff}}\mathcal{A}^{\text{eff}})$ is the dimensionless active force on cilia j . For the dimensionless random forces, it can be shown that they obey the following relation: $\langle \mathbf{f}'_i{}^r(t'_1)\mathbf{f}'_j{}^r(t'_2) \rangle = 2k_B T/(k^{\text{eff}}(\mathcal{A}^{\text{eff}})^2)\tilde{G}^{-1}(\mathbf{r}_i, \mathbf{r}_j)\delta(t'_1 - t'_2)$. Therefore, for a general model for cilia with hydrodynamic coupling such as the Oseen or Blake tensor, the equation can be written in dimensionless form as in Eq. (6). Thus, in the steady state, the spatial properties of the emergent waves will be independent of viscosity, meaning that dissipation only affects temporal parameters.

V. DISCUSSION AND CONCLUSION

Although the dimensional analysis cannot predict the occurrence or nature of emergent behavior, it is remarkable in predicting that the wavelength or other spatial properties will be viscosity independent in general. This property of hydrodynamically coupled oscillators could be used as a simple framework to understand the origin of metachronal waves in biological systems. The breakdown of such invariance can indicate the complexity of living systems. We discuss three following scenarios where our prediction regarding the independence of spatial wave properties with viscosity may fail.

(1) For real cilia, the viscosity of the medium may influence the activity parameters and then our observation can break down. As we discussed above, in this scenario the right-hand side of Eq. (4), will be dependent of viscosity. Therefore, we may not expect invariance of spatial properties of emergent waves. Experimental results [31,41] seem to

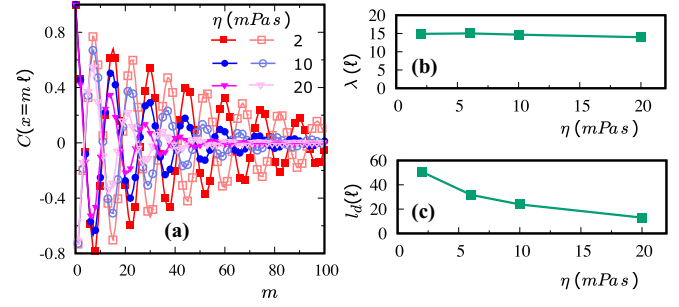


FIG. 6. Effect of viscosity in presence of athermal noise in one dimension ($N = L = 200$). Correlation function $C(x = m\ell)$ as a function of the distance between rowers for (a) three different η values (for $\mathcal{A} = 0.8 \mu\text{m}$). The wavelength λ (in units of ℓ) is plotted against η (b). Decay length l_d (in units of ℓ) is plotted against η (c). Unlike thermal noise where diffusivity is $D = k_B T/\gamma$, in this athermal case, the diffusivity D is kept constant to a value ($=0.01 \mu\text{m}^2\text{s}^{-1}$) while we vary η .

indicate a small dependency of cilia beating amplitude with the liquid medium. Increased viscosity can also alter the beating orientation [30,33], amplify the asymmetry between the stroke and antistroke [41], and change other details of the beating pattern [42]. These can cause changes in the metachronal wave characteristics and in particular in the direction of propagation. These experimental results indicate that the beating machinery could adapt to the viscous load.

(2) The fluctuations in our study are thermal, where an effective fluctuation-dissipation theorem is expected to hold. However, some experiments point out that in real cilia and flagella, the fluctuations are mostly dominated by those that have an athermal origin [43–47]. To understand how this athermal noise affects the spatial properties of metachronal waves, we numerically study the model in presence of noise with a strength kept constant against viscosity. We numerically solve Eq. (2) for different values of η , with a constant noise strength D . The results are plotted in Fig. 6. There is thus no thermal noise in this simulation and we expect spatial properties then to depend on the viscosity as Eq. (4), will be dependent of viscosity. We indeed observe that the correlation lengthscale l_d decays with viscosity, while the wavelength remains almost constant. This is in contrast with the previous (thermal) case where l_d was constant as the viscosity was varied. It also means that the wavelength is not much influenced by dissipation.

(3) Another source of noninvariance of spatial properties could be the viscoelastic nature of the fluid. For the viscoelastic fluids, the timescales could be nonlinear as a function of viscosity. The above dimensional argument will not hold, and we believe that the invariance of spatial properties will not be true in such a case. Experimentally, the wavelength seems to be almost constant within a wide range of fluid viscosities [30,33], while the frequency ν and velocity V decrease as a function of η . We note that in [34], the viscosity was varied on a very large range. For viscosity larger than 20 mPa s, we suspect that the liquid is no longer Newtonian and probably viscoelastic given the high molecular weight polymers used for the viscous solutions. For these higher viscosities, another lower plateau in the wavelength is found: the wavelength

seems to show a sudden change after a critical viscosity value [34], after which the wavelength reaches a lower value and remains constant.

In a recent work by Ringers *et al.* [48], an increase in spatial correlation length (l_d) was observed with viscosity, where methylcellulose concentration was varied to increase medium viscosity. Why this coherence lengthscale increases with viscosity is not clear. This result cannot be explained by our model either in the presence of athermal noise (Fig. 6) or thermal noise. It is known that a higher methylcellulose concentration not only increases viscosity but also makes the fluid viscoelastic. Whether viscoelasticity plays a role in increasing the spatial coherence needs further investigations which is not within the scope of this paper.

In conclusion, using a simple rowing model of coupled oscillators, we studied the influence of activity and dissipation on the spatial and temporal synchronization properties of cilia assemblies. The enhancement of cilia

activity increases the wavelength and beating period, keeping the wave velocity almost unchanged. Remarkably, the viscosity does not affect the spatial patterns of metachronal waves. Using dimensional analysis, we demonstrate that this result is robust against complexity of cilia model and hydrodynamic coupling due to viscous media. On the contrary, the beating frequency and the wave velocity indeed decrease with viscosity. The deviation from such a behavior may indicate the influence of the medium on cilia activity, the presence of athermal fluctuations, or the viscoelastic nature of the medium. Our findings could pave the way for understanding the emergence of specific functions of cilia in pathological contexts [23].

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